

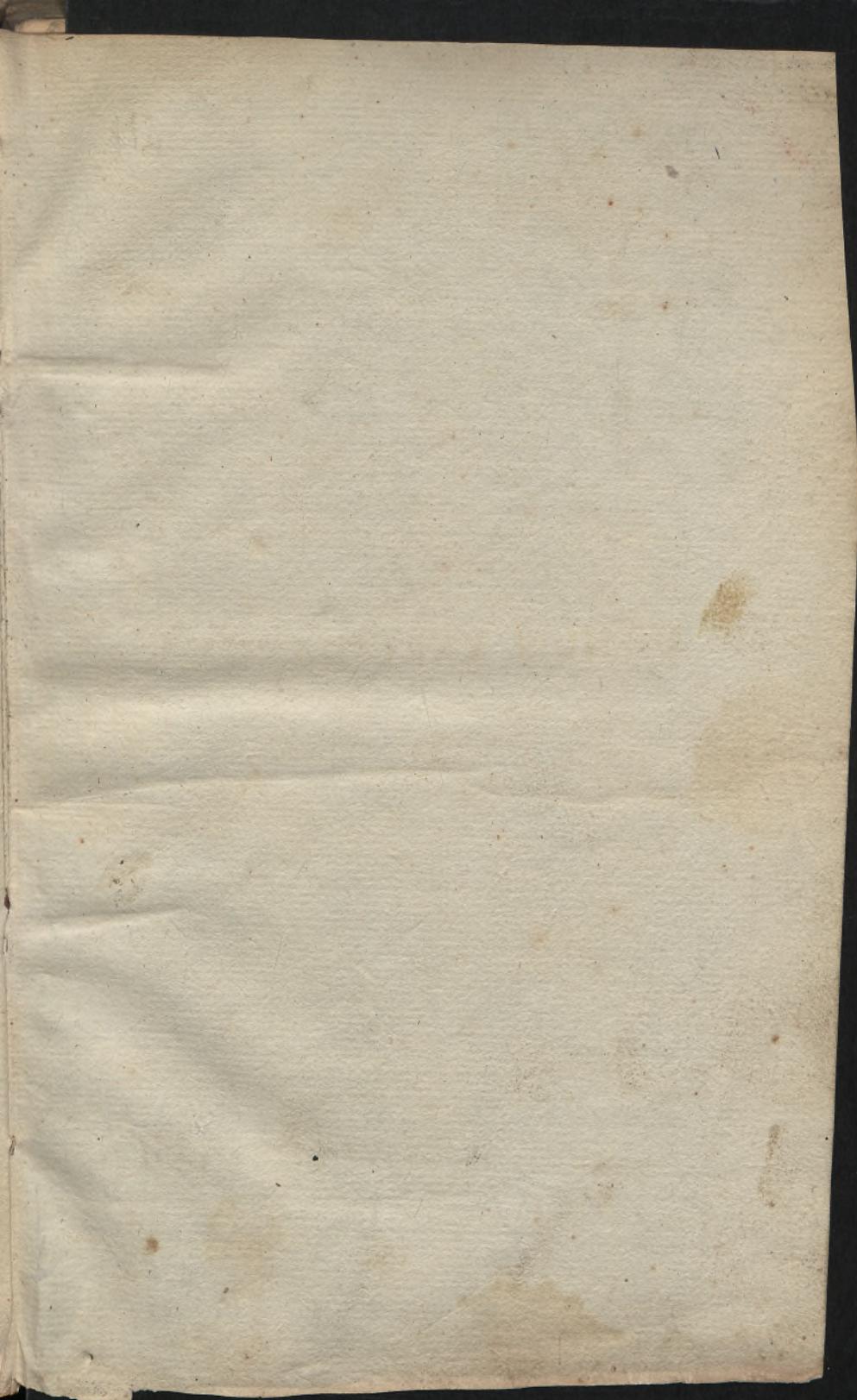
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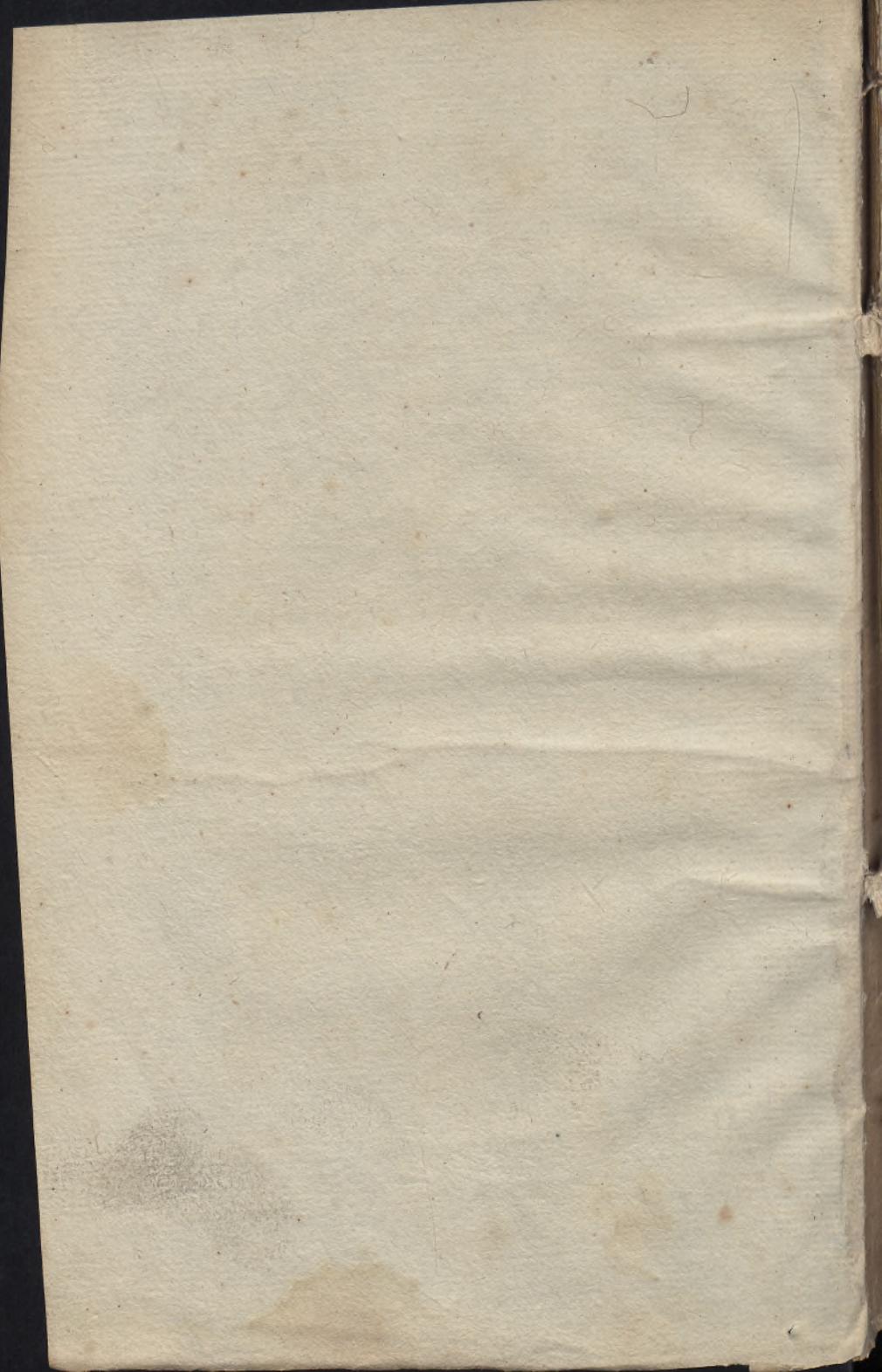
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# ASTRONOMY OF THE SATELLITES OF THE

## *Earth, Jupiter and Saturn:*

Grounded upon Sir *Isaac Newton's* Theory of  
the Earth's SATELLITE.

The THEORY explain'd, and made easie to the  
meanest Capacity, in calculating the true Place of  
the Moon:

And freed from the Errors printed in the said Theory, by  
*Dr. Gregory, Dr. Harris,* and several other Authors.

By which now the Place of the Moon, and Eclipses of the Luminaries,  
are found to a very great Exactness.

### A L S O

New Tables of the Motions of the Satellites of *Jupiter* and *Saturn*, (founded upon the Observations of  
*Mr. Flamsteed, Mr. Cassini, Mr. Hugens, Dr. Halley*  
and *Mr. Pound,*) from the Vernal Equinox:

By which their Places and Positions, in respect of one another, may be exactly determined at any given Time.

*Adapted to the Meridian of London.*

To which is added, A PROBLEM to find the Latitude of the Place by  
the Altitude of the Sun, Moon, or Star, upon any Azimuth; being  
very useful for all Sea-faring Men, as well as Gentlemen and others.

---

By **CHARLES LEADBETTER,**  
*Teacher of the MATHEMATICKS.*

---

L O N D O N :

Printed for J. WILCOX, at the *Green-Dragon*, in  
Little-Britain. M.DCC.XXIX.

*YMOV* *AB* *1721*

## ADVERTISEMENT.

THE following Mathematical Sciences are taught by the Author hereof, at his House, at *The Hand and Pen in Cock-Lane, Shoreditch, London*; or at any Gentleman's Apartment, viz. Vulgar and Decimal Arithmetick, Geometry apply'd to the Mensuration of Superficies and Solids, by Pen and Sliding-Rule; Projection of the Sphere on any Circle; Trigonometry, plain and spherical; Surveying of Land, by any Instrument now in Use; Gauging of all sorts of Vessels, with all the practical Methods used by the Officers of the Excise; Astronomy in all its Branches; Navigation by the Plain and Mercator's Chart, and by the Arch of a great Circle; Geography and the Use of the Globes, with all other Mathematical Instruments whatsoever. Dialling upon any Plane for any Latitude.

Where may be had, *First*, His Treatise of Eclipses for 26 Years, 2. His Sheet of the Conjunction of  $\text{\textit{h}}\text{\textit{x}}$  and  $\text{\textit{g}}$  1722, and *Mercury's Passage over the Sun, October 29, 1723.* 3. His Astronomical Calendar for 28 Years, ending 1753. 4. His System of the Planets demonstrated. 5. His Sheet of all the Luminarian Eclipses for 35 Years, ending *Anno 1761.* 6. His Compleat System of Astronomy. 7. His Astronomy of the Satellites of the Earth, *Jupiter* and *Saturn*: Also sold by *J. Wilcox*, at the *Green-Dragon* in *Little-Britain, London*.



## R E A D E R,

I Here present you with my *Astronomy of the Satellites of the Earth, Jupiter and Saturn.* What I mean by the Satellite of the Earth, is the Moon, with Sir Isaac Newton's last Improvement of the Theory of that Planet, which I had published in my Compleat System of Astronomy, had it not been for some very gross Errors printed in the Theory, as laid down by Dr. Gregory, in Pag. 334. of his Latin Astronomy, and carried on in his English Astronomy, Vol. II. pag. 563. by Dr. Harris in his Lexicon Technicum, Vol. I. under the Word Moon: and by the Learned Author of Praelectiones Astronomicæ, pag. 318. and in the English Translation, pag. 345. The most material Faults are the greatest Equation of the Apogee, and the radical Place for the Year 1681. For whoever will be at the pains to examine the Numbers (as I have done) will find that the greatest 66782, and least 43319, Eccentricities, will give the greatest and least Equations of the Lunar Orbit  $7^{\circ} 39' 30''$ ,  $4^{\circ} 57' 56''$ ; and  $12^{\circ} 18' 15''$  for the greatest Equation of the Apogee, which, as they have it, is only  $12^{\circ} 15' 4''$ . By comparing these Numbers with the Times of the visible Eclipses of the Sun in the Years 1715, 1722, 1724, 1726, which were carefully observed at London, I am satisfied that

the greatest Equation of the Apogee is  $12^{\circ} 18' 15''$  as I have it in these my new Tables, and reduced them to the Meridian of London.

By finding the true Times of the Conjunction, and Opposition of the Sun and Moon by this Theory, it may seem, at first, to them unskill'd in these Matters, to be almost an Impassibility; but after due Consideration it will appear, that those Equations, that depend upon the Distance of the Moon from the Sun, vanish, which are the 5th, 6th and 7th; and the first, second, and third Equations, alter but little, in a small Space of Time; so that regard is chiefly to be had to the fourth Equation, with which work as I have shewed in my Compleat System, Precept 7th. until you find the Orbit-Place of the Moon the same with the Sun's true Place, and then you have the middle Time of the true Conjunction or Opposition in the Moon's Orb, to the greatest Exactness imaginable.

Many ingenious Persons have often wish'd, that Tables of the Motions of the Satellites of Jupiter and Saturn were published, that thereby they might know at any time before-hand, how they wou'd appear when observed: Therefore, for the sake of the diligent Observer, I here publish mine, constructed from the Observations of Mr. Hugens, Mr. Flamsteed, Mr. Cassini, Dr. Halley, and Mr. Pound; which, I dare to say, are the correctest the World ever saw. The Method of finding their Places is plain and easy to be understood by any one, though meanly versed in these things.

I have only one thing more to remind my Reader of, and that is, If he has a mind to find the Times of the Eclipses of Jupiter's Satellites, after the Cassinian Method, he must observe, that the periodical Time of the first

first Satellite is nearly  $\frac{2}{2+4+7}$  Part of the periodical Time of Jupiter from one Alphelion to another; whence the Equations of the Jovial Orbit being turned into Minutes and Seconds of Time, and adapted to those particular Revolutions of the Satellites, will make good the principal Parts of the Equations of these Satellites. By which Directions and easy Tables, any Observer may truly know their Distances from Jupiter, and distinguish one Satellite from another at any given Time; which will both be pleasant and advantagious to him in rectifying the Longitude of Places at Land, by the Times of their Eclipses.

*I remain a Friend to the Astronomical Student,*

CHARLES LEADBETTER,

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T H E

THE  
C O N T E N T S.

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**BOOKS**

BOOKS just publish'd, and sold by J. Wilcox in Little  
Britain.

I. A Compleat System of Astronomy, in two Volumes; containing the Description and Use of the Sector; the Laws of Spherick Geometry; the Projection of the Sphere Orthographically and Stereographically upon the Planes of the Meridian, Ecliptic and Horizon; the Doctrine of the Sphere; and the Eclipses of the Sun and Moon for thirty-seven Years: Together with all the Precepts of Calculation. Also, new Tables of the Motions of the Planets, fix'd Stars, and the first Satellite of Jupiter; of Right and Oblique Ascensions, and of Logistical Logarithms. To the whole are prefix'd, Astronomical Definitions, for the Benefit of young Students. By Charles Leadbetter, Teacher of the Mathematicks. Price 12*s.*

II. Astronomy, or, the true System of the Planets demonstrated: Wherein is shewn, by Instrument, their Anomalies, Heliocentric and Geocentric Places, both in Longitude and Latitude, their Aphelions, Perihelions, Retrogradation, Elongation, Parallaxes and Distances from the Sun and Earth, with the Method of computing the Times when *Venus* and *Mercury* may be seen in the Sun's Disk. Also the Moon's Phases and Eclipses of the Luminaries, for any Time past, present, or to come; with proper Cuts to each Planet, by which any Person may in a few Hours, and with great Ease, attain to a perfect Knowledge of the Planetary or Solar System. By Charles Leadbetter. Price 5*s.*

III. A new Treatise of the Construction and Use of the Sector; containing the Solutions of the principal Problems, by that admirable Instrument in the chief Branches of Mathematicks, viz. Arithmetick, Mensuration, Plain Trigonometry, Projection of the Sphere, Geography, Astronomy, Dialling, &c. illustrated with Variety of necessary Observations and pleasant Conclusions; containing several Applications entirely new. By the late Mr. Samuel Cunn, now carefully revised by Edmund Stone, F. R. S. Price 4*s.*

IV. A sure Guide to Builders, or the Principles and Practice of Architecture, geometrically demonstrated, and made easy for the Use of Workmen in general: Wherein such Geometrical Definitions, Theorems, Problems, &c. as are the Basis of Architecture, are render'd easy and intelligible to every Capacity, &c. By B. Langley, of Twickenham. Price 14*s.*

V. The Builder's Chest-Book, or a Complete Key to the five Orders of Columns in Architecture, by way of Dialogue, very useful for young Students in Architecture. By B. Langley. Price 2*s. 6d.*

VI. The Modern Navigator's Complete Tutor, or a Treatise of the whole Art of Navigation, in its Theory and Practice, Curiosity and Utility. By Joshua Kelly. Price 4*s.*

~~that also I should say to myself that this had not  
done it. O dear to me to say to myself that this had not  
done it. But now and then I do like this kind of writing.~~

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## SECTION I.

*To Calculate the true Place of the Moon, according  
to Sir ISAAC NEWTON's last Improvement of his  
Theory.*

1. **F**ROM the Tables of the Sun's Motions in my compleat System of Astronomy, calculate the true Place of the Sun, its Distance from the Earth, and Parts answering the Logarithm, and subtract the Mean Anomaly from the Mean Longitude, and you will have the Place of the Sun's Apogæum, as is shewed in the Examples for the first and second Days of January at Noon, equal Time, Anno 1729.

2. Out of these Tables of the Moon's Mean Motions, take out the Longitude, Apogee and Node, to the Equal Time of the Question proposed, and gather the Mean Longitude and Apogee into two distinct Sums; but the Mean Motion of the Node being Retrograde, you must subtract the Motions for Months and Days from the Radical Place, as is usually done, and as you see in the Examples following.

3. Before you can find any of the Moon's Equations, you must observe that these are standing Numbers, *viz.*

The Earth's { Eccentricity -- -- 1692  
Greatest Equation 1° 56' 20"

The greatest Annual Equation 1 { Longitude 11° 49"  
Apogee 20 0  
Node -- 9 30

And these four are always proportional to each other.

B

And

4. To find the first Equation of the Moon's Longitude. The Sun's Equation for the Time of the Question is  $28^{\circ} 6'$ , then by the Logistical Logarithms you must always say,

As  $1^{\circ} 56' 20''$  the Sun's greatest }  
Equation. — }  $116' 20''$  LL. 2875 }

To its present Equation, 28 6 3294  
 So ⚡ Annual greatest Equation, 11 49 7057

To 2 first Equation in Longitude 2 51 13226

Note, this Equation must always be added to the Mean Longitude of the Moon, when the Sun's Mean Anomaly is  $0, 1, 2, 3, 4, 5$  Signs ; but must be subtracted, if the Sun's Mean Anomaly be  $6, 7, 8, 9, 10, 11$  Signs : from which Theory I have fram'd the following Table.

Enter the Table with the Sign on the Head and Degree of the Sun's Mean Anomaly on the Left hand descending, but with the Degree on the Right hand ascending, if the Sign fall at bottom of the Table, and in the place of meeting, you will have the first, or Annual Equation of the Moon's Longitude; which in this Example (as above) you will find to be  $2' 51''$  to be subtracted. See *Gregory's Astr.* p. 544.

Praktiken und Techniken der sozialen Arbeit und sozialen Dienstleistungen

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## A Table of the first Equation of the Moon.

Anom.	Sign 0 Add.	Sign 1 Add.	Sign 2 Add.	Sign 3 Add.	Sign 4 Add.	Sign 5 Add.	Anom.
0	0 5	47	10 7	11 49	10 21	6 0	30
1	0 12	58	10 14	11 49	10 15	5 49	29
2	0 24	6	9 10	21 11	49 10	7 5	38
3	0 36	6	19 10	26 11	48 10	1 5	27
4	0 48	6	29 10	31 11	48 9	55 5	16
5	1 0	6	39 10	37 11	47 9	47 5	5
6	1 12	6	49 10	42 11	47 9	40 4	53
7	1 24	6	59 10	47 11	45 9	33 4	42
8	1 36	7	9 10	52 11	44 9	26 4	30
9	1 48	7	19 10	56 11	42 9	19 4	18
10	1 59	7	28 11	1 11	41 9	11 4	6
11	2 11	7	37 11	5 11	39 9	2 3	54
12	2 23	7	46 11	9 11	36 8	54 3	43
13	2 35	7	55 11	14 11	34 8	46 3	31
14	2 46	8	4 11	19 11	31 8	37 3	19
15	2 58	8	13 11	22 11	29 8	28 3	7
16	3 10	8	22 11	25 11	25 8	20 2	54
17	3 22	8	31 11	28 11	22 8	11 2	42
18	3 34	8	39 11	30 11	19 8	1 2	30
19	3 46	8	47 11	32 11	15 7	52 2	18
20	3 57	8	55 11	35 11	11 7	43 2	5
21	4 9	9	3 11	38 11	6 7	34 1	52
22	4 20	9	11 11	40 11	2 7	24 1	40
23	4 32	9	19 11	42 10	58 7	14 1	28
24	4 43	9	27 11	43 10	53 7	3 1	15
25	4 54	9	34 11	45 10	48 6	53 1	2
26	5 4	9	41 11	46 10	43 6	43 0	49
27	5 15	9	47 11	47 10	38 6	33 0	37
28	5 27	9	54 11	48 10	32 6	22 0	25
29	5 37	10	1 11	48 10	26 6	11 0	12
30	5 47	10	7 11	49 10	21 6	0 0	0
	Sign 11 Sub.	Sign 10 Sub.	Sign 9 Sub.	Sign 8 Sub.	Sign 7 Sub.	Sign 6 Sub.	

5. To find the Annual or first Equation of the Moon's  
Apogee.

BY remembering what the Sun's Equation is for the present Time, you must say,

As  $1^{\circ} 56' 20''$  the greatest Equation,  $1^{\circ} 56' 20''$  LL 2875  
 To its present Equation. -- -- 28 6 3294 } +  
 So greatest Annual Equation Apog. 20 0 4771 }

To present Equation Apogee. 4 50 10940

This Equation is always to be added to the Mean Place of the Moon's Apogee; if the Sun's Mean Anomaly be  $6, 7, 8, 9, 10, 11$  Signs; but subtracted when the Sun's Mean Anomaly is  $0, 1, 2, 3, 4, 5$  Signs, as the following Table sheweth, which I have made from the Theory.

Enter the following Table with the Sun's Mean Anomaly, as directed in the 4th, and you have the Equation answering, to be added to, or subtracted from the Mean Place of the Moon's Apogee; and you will have it Equated the first time.

A

(59)

A Table of the first Equation of the Moon's Apogee.

Anom.	Sign o Subt.	Sign 1 Sub.	Sign 2 Sub.	Sign 3 Sub.	Sign 4 Sub.	Sign 5 Sub.	Anom.
0	0	9	49	17	8	20	0
1	0	20	10	7	17	19	29
2	0	41	10	24	17	29	20
3	1	10	42	17	39	19	59
4	1	22	10	59	17	48	19
5	1	42	11	16	17	58	19
6	2	3	11	33	18	7	19
7	2	23	11	49	18	16	19
8	2	43	12	6	18	24	19
9	3	4	12	22	18	32	19
10	3	24	12	39	18	39	19
11	3	44	12	55	18	46	19
12	4	4	13	10	18	53	19
13	4	24	13	26	19	0	19
14	4	44	13	41	19	6	19
15	5	4	13	56	19	12	19
16	5	24	14	10	19	18	19
17	5	44	14	25	19	23	19
18	6	3	14	39	19	28	19
19	6	23	14	53	19	33	19
20	6	43	15	7	19	37	18
21	7	2	15	21	19	41	18
22	7	21	15	33	19	44	18
23	7	40	15	46	19	48	18
24	7	59	15	58	19	51	18
25	8	18	16	11	19	53	18
26	8	36	16	23	19	55	18
27	8	54	16	35	19	57	17
28	9	13	16	46	19	58	17
29	9	31	16	57	19	59	17
30	9	49	17	8	20	0	17
	Sign 11 Add.	Sign 10 Add.	Sign 9 Add.	Sign 8 Add.	Sign 7 Add.	Sign 6 Add.	

6. To find the Annual or first Equation of the Moon's Node.

H ere you must take the present Equation of the Sun  
and by the Logistical Logarithms in my Astronomy,  
say,

As  $1^{\circ} 56' 20''$  the Sun's greatest Equation,  $\{ 116' 20'' \text{ LL } 2875 \}$   
 To its present Equation,  $-- \quad 28 \quad 6 \quad 3294 \}$   
 So greatest Equation of the Node,  $9 \quad 30 \quad 8004$

To the present Equat. of the Node, 2 18 14173  
This Equation is always to be added to the Mean Place of the Node, if the Sun's Mean Anomaly be 0, 1, 2, 3, 4, 5 Signs, but subtracted if it be 6, 7, 8, 9, 10, 11 Signs, the Sum or Difference is the Place of the Node the first time Equated.

A Table of the Annual, or first Equation of  
the Moon's Node.

Anom.	○	Sign o Add.	Sign 1 Add.	Sign 2 Add.	Sign 3 Add.	Sign 4 Add.	Sign 5 Add.	Anom.	○				
0	0	0	4	40	8	9	9	30	8	19	4	50	30
1	0	9	4	48	8	14	9	30	8	14	4	41	29
2	0	19	4	57	8	19	9	30	8	9	4	32	28
3	0	29	5	5	8	24	9	30	8	4	4	23	27
4	0	39	5	13	8	28	9	29	7	58	4	14	26
5	0	48	5	21	8	32	9	29	7	53	4	5	25
6	0	58	5	29	8	36	9	28	7	48	3	56	24
7	1	8	5	37	8	40	9	27	7	42	3	47	23
8	1	18	5	45	8	44	9	26	7	35	3	38	22
9	1	27	5	53	8	48	9	25	7	29	3	29	21
10	1	37	6	0	8	52	9	24	7	23	3	19	20
11	1	46	6	8	8	55	9	22	7	16	3	9	19
12	1	56	6	15	8	58	9	20	7	9	2	59	18
13	2	5	6	22	9	2	9	18	7	3	2	56	17
14	2	15	6	30	9	5	9	16	6	56	2	40	16
15	2	24	6	37	9	7	9	14	6	49	2	30	15
16	2	34	6	44	9	10	9	12	6	42	2	20	14
17	2	43	6	50	9	12	9	9	6	35	2	10	13
18	2	53	6	57	9	15	9	6	6	27	2	0	12
19	3	2	7	4	9	17	9	3	6	20	1	50	11
20	3	11	7	11	9	19	8	59	6	12	1	40	10
21	3	20	7	17	9	21	8	56	6	4	1	30	9
22	3	29	7	23	9	22	8	52	5	56	1	20	8
23	3	38	7	29	9	24	8	49	5	49	1	10	7
24	3	47	7	35	9	25	8	45	5	41	1	0	6
25	3	56	7	41	9	26	8	41	5	33	0	50	5
26	4	5	7	46	9	27	8	37	5	24	0	40	4
27	4	14	7	52	9	28	8	33	5	16	0	30	3
28	4	23	7	58	9	29	8	28	5	8	0	20	2
29	4	31	8	4	9	29	8	23	4	59	0	10	1
30	4	40	8	9	9	30	8	19	4	50	0	0	0
		Sign 11 Sub.	Sign 10 Sub.	Sign 9 Sub.	Sign 8 Sub.	Sign 7 Sub.	Sign 6 Sub.						

## 7. To find the Second Equation of the Moon.

This Equation is greatest when the Sun is in the Octants, or  $45^{\circ}$  distant from the Moon's Apogee, and is then  $5' 56''$  if the Sun be in Perigeon; but only  $5' 34''$  in Apogeeum, and at a mean Distance from the Earth  $3' 45''$ : Therefore, subtract the Place of the Moon's Apogee the first time Equated, from the Sun's true Place, double the Remainder and say, As Radius, to Sine of that double Distance of the Sun from the Moon's Apogee; so is the Minutes and Second (reduced into Seconds) taken out of the following Table by help of the Sun's mean Anomaly, to the second Equation of the Moon in Second.

Operation.	$f. \circ$	$s.$
Sun's true Place	9 22 23 46	
Moon's Apogee first time Equated, sub.	7 53 51	
Dist. Sun from Moon's Apogee,	8 14 29 55	
Double,	4 28 59 50	
Complement,	1 10 00 10	
Now say,	0 . "	

As Radius	90 0 0 10.000000
To S. double Dist. O à D Apog.	31 0 10 9.711874
So $5' 54''$ out of the following Table,	234 2.369216
To the second Equation in Seconds,	120 2.081090

This Equation must always be added to the first Equated Place of the Moon, while her Apogee passes from the Square of the Sun to the Conjunction; but is subtracted from thence in the Transit of the Apogee from a Conjunction, to a Quadrature. That is, if the Distance of the Sun from the Moon's Apogee be

Signs { 0 1 2 6 7 8 subtr.  
          { 3 4 5 9 10 11 add.

So in the Example before us, the second Equation  $2'$  is subtracted from  $2 s. 23^{\circ} 27' 23''$ , and there remains  $2 s. 23^{\circ} 25' 23''$  the Moon's Place equated the second time.

Note, always in your Work, reserve the Logar. Sine of the double Distance of the Sun from the D Apogee; for you will have Occasion to use it in finding the D present Eccentricity in the 10th Precept following.

A Table of the proportional Part of the  
second Equation of the Moon; with the  
Logarithm.

○ Ano.	Eq.	Sign 0 Logar.	Eq.	Sign 1 Logar.	Eq.	Sign 2 Logar.	○ Ano.
	"	"		"	"	"	
0	214	2.330414	217		221		30
1	214		217		221		29
2	214		218	2.338456	221		28
3	214		218		221		27
4	214		218		221		26
5	214		218		222	2.346353	25
6	214		218		222		24
7	214		218		222		23
8	215	2.332438	218		222		22
9	215		218		222		21
10	215		219	2.340444	222		20
11	215		219		222		19
12	215		219		222		18
13	215		219		223	2.348305	17
14	215		219		223		16
15	215		219		223		15
16	216	2.334454	219		223		14
17	216		219		223		13
18	216		219		223		12
19	216		220	2.342423	223		11
20	216		220		223		10
21	216		220		224	2.350248	9
22	216		220		224		8
23	216		220		224		7
24	217	2.336460	220		224		6
25	217		220		224		5
26	217		220		224		4
27	217		221	2.344392	224		3
28	217		221		224		2
29	217		221		225	2.352182	1
30	217		221		225		0

Sign 11 | Sign 10 | Sign 9

A Table of the Proportional Part of the  
second Equation of the Moon, with the  
Logarithm, continued.

○ Ano.	Eq.	Sign 3 Logar.	Eq.	Sign 4 Logar.	Eq.	Sign 5 Logar.	○ Ano.
0	225		228	"	232		30
1	225		229	2.359836	232		29
2	225		229		232		28
3	225		229		233	2.367356	27
4	225		229		233		26
5	225		229		233		25
6	226	2.354108	229		233		24
7	226		229		233		23
8	226		229		233		22
9	226		230	2.361728	233		21
10	226		230		233		20
11	226		230		234	2.369216	19
12	226		230		234		18
13	226		230		234		17
14	227	2.356026	230		234		16
15	227		230		234		15
16	227		230		234		14
17	227		231	2.363612	234		13
18	227		231		234		12
19	227		231		235	2.371068	11
20	227		231		235		10
21	227		231		235		9
22	228	2.357935	231		235		8
23	228		231		235		7
24	228		231		235		6
25	228		232	2.365488	235		5
26	228		232		235		4
27	228		232		336	2.372912	3
28	228		232		236		2
29	228		232		236		1
30	228		232		236		0
		Sign 8		Sign 7		Sign 6	

## 8. To find the Third Equation of the Moon.

This Equation depends upon the Distance of the Sun from the Moon's Nodes, and is greatest in the Octants, and is then  $47''$ , but in the Syzigias and Quadratures nothing : Therefore from the Sun's true Place, subtract the Place of the Node first Equated, and say, As Radius, to the Sine of the double Distance of the Sun from the next Syzgia, or Quadrature, so is  $47''$ , to the Equation required.

	Operation.	f. ° ' "
Sun's true Place.	— — —	9 22 23 46
Node first Equated subt.	— — —	<u>10 25 43 30</u>
Dist. Sun from the Node,	— — —	10 26 46 16
Double,	— — —	9 23 20 32
Complement,	— — —	2 6 39 28
Now say,	— — —	° ' "
As Radius	— — —	90 0 0 10.000000
To S. double Dist of $\odot$ à $\oplus$	— — —	66 39 28 9.962917
So is the greatest Equation	— — —	47 1.672098
To the present Equation	— — —	43 1.635015

This Equation is added to the Moon's Place Equated the second Time, whilst the Nodes pass from the Sun's Conjunction to the Quadratures of the same; and is subtracted in the Transit from the Quadratures to Conjunction. And, according to the Theory, I have framed the following Table, which gives this Equation by Inspection.

A Table of the third  
Equation of the Moon.

$\odot$	Signs $\frac{1}{2}$ Add.	Signs $\frac{1}{2}$ Add.	Signs $\frac{1}{2}$ Add.	$\odot$
0	0	0	41	30
1	0	1	41	29
2	0	3	42	28
3	0	5	43	27
4	0	6	43	26
5	0	8	44	25
6	0	10	44	24
7	0	11	45	23
8	0	13	45	22
9	0	14	46	21
10	0	16	46	20
11	0	17	46	19
12	0	19	47	18
13	0	20	47	17
14	0	22	47	16
15	0	23	47	15
16	0	25	47	14
17	0	26	47	13
18	0	27	47	12
19	0	29	46	11
20	0	30	46	10
21	0	31	46	9
22	0	32	45	8
23	0	34	45	7
24	0	35	44	6
25	0	36	44	5
26	0	37	43	4
27	0	38	43	3
28	0	39	42	2
29	0	40	41	1
30	0	41	41	0
	Signs $\frac{1}{12}$ Sub.	Signs $\frac{1}{12}$ Sub.	Signs $\frac{1}{9}$ Sub.	

Enter this Table with  
the Distance of the  
Sun from the Node,  
and you have the  
Equation to be ap-  
ply'd according to  
its Title.

## 9. To find the Second Equation of the Moon's Apogee,

**F**irst, (as in the seventh Article hereof) if from the Sun's Place, you subtract the Place of the Apogee first Equated, the Remainder is called the Annual Argument, and in this Example is  $8^{\circ} 14' 29'' 55'''$ , which is demonstrated from the Theory thus:

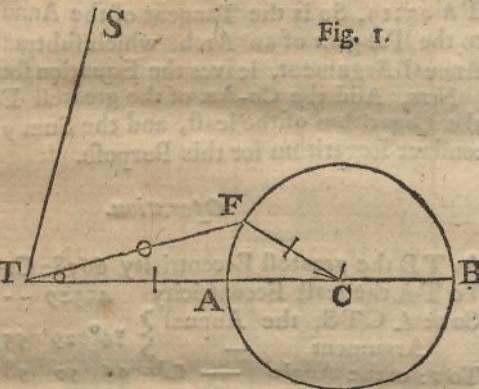
Let T represent the Earth, TS a right Line joining the Earth and  $\odot$ ; TACB, a right Line drawn from the Earth to the Place of the Moon's Apogee first Equated.

The Angle

STA, the Annual Argument, of the said Apogee =  $74^{\circ} 29' 55''$ : TA the least Eccentricity 43319 of the Lumar Orbit; TB the greatest 66782. Bisect AB in C, and on the Center C, and Semidiameter AC=CB, Describe the Circle AFB; and make the Angle BCF equal to twice the Annual Argument  $148^{\circ} 59' 50''$ , and draw TF, and CF, so shall TF be the Eccentricity at the time of the Question, and the Angle CTF the Equation of the Apogee sought. In which Triangle CTF are given TC, CF, and the Angle included, being the Compliment of twice the Annual Argument to a Semicircle =  $31^{\circ} 0' 10''$  to find the Angle CTF, and the Side TF.

*Operation.*

TB the greatest Eccentricity	66782	}
TA the least Eccentricity	43319	
Difference = AB	—	23463
Half = AC = CF	—	$11731\frac{1}{2}$ + TA = TC Which



Which falls directly under the second Axiom of plain Trigonometry; for as the Sum of the Sides  $TC + CF$ , To their Difference  $= TA$ , So is the Tangent of half the Sum of the opposite Angles, to the Tangent of half their Difference, which subtracted from half the Sum of the Angles, gives the lesser Angle, *viz.* CTF the Equation sought. Which in short is, As the greatest Eccentricity  $TB$  66782, Is to the least Eccentricity  $TA$  43319, So is the Tangent of the Annual Argument, to the Tangent of an Arch, which subtracted from the Annual Argument, leaves the Equation sought.

*Note*, Add the Co-Ar. of the greatest Eccentricity to the Logarithm of the least, and the Sum 9.812019 is a constant Logarithm for this Purpose.

### Operation.

$$\begin{array}{rcl} \text{As } TB \text{ the greatest Eccentricity } 66782 \text{ Co-Ar. } 5.175341 \\ \text{To } TA \text{ the least Eccentricity } 43319 \quad \text{---} \quad 4.636678 \\ \text{So } t: \angle CTS, \text{ the Annual } \\ \text{Argument} \quad \text{---} \quad \begin{array}{r} 74^\circ 29' 55'' \\ \hline 10.556970 \end{array} \\ \text{To } t: \text{ of the Angle} \quad \text{--- sub. } 66 \ 30 \ 58 \quad \underline{10.368989} \end{array}$$

Rem:  $\angle CTF$ , the Equation 7 38 57

This Equation is to be added if the Annual Argument be 0, 1, 2, 6, 7 8 Signs, but subtracted if it be 3, 4, 5, 9, 10, 11, to or from the Place of the Apogee first Equated, the Sum or Difference is the Place of the Apogee a second time Equated: which in this Example is  $1^{\text{st}}. 15^\circ 32' 48''$ ; according to which Theory I have calculated the following Table.

*Scripsit*  
*Scipio*  
*Scipio*  
OT + AT + ECTF

A Table of the second Equation of the  
Moon's Apogee.

Argu. Ann.	Signs $\frac{5}{6}$ Add			Signs $\frac{1}{7}$ Add			Signs $\frac{2}{9}$ Add			Argu. Ann.
0	0	0	"	9	28	8	11	40	16	30
1	0	21	4	9	42	20	11	30	55	29
2	0	42	9	9	56	9	11	20	30	28
3	1	3	11	10	9	25	11	8	59	27
4	1	24	11	10	22	10	10	56	23	26
5	1	45	7	10	34	21	10	42	42	25
6	2	5	59	10	45	59	10	27	53	24
7	2	26	46	10	57	2	10	12	00	23
8	2	47	28	11	7	29	9	55	1	22
9	3	8	3	11	17	18	9	36	58	21
10	3	28	31	11	26	27	9	17	50	20
11	3	48	50	11	34	57	8	57	38	19
12	4	8	59	11	42	45	8	36	24	18
13	4	28	59	11	49	51	8	14	8	17
14	4	48	48	11	56	12	7	50	54	16
15	5	8	24	12	1	48	7	26	41	15
16	5	27	48	12	6	37	7	1	31	14
17	5	46	58	12	10	34	6	35	29	13
18	6	5	54	12	13	50	6	8	35	12
19	6	24	34	12	16	11	5	40	49	11
20	6	42	58	12	17	40	5	12	26	10
21	7	1	4	12	18	15	4	43	18	9
22	7	18	52	12	17	56	4	13	30	8
23	7	36	20	12	16	41	3	43	7	7
24	7	53	28	12	14	29	3	12	14	6
25	8	10	15	12	11	18	2	40	53	5
26	8	26	38	12	7	9	2	9	10	4
27	8	42	39	12	1	58	1	37	9	3
28	8	58	15	11	55	46	1	4	53	2
29	9	13	24	11	48	33	0	32	29	1
30	9	28	8	11	40	16	0	0	00	0
	Signs $\frac{5}{6}$ Sub.			Signs $\frac{1}{7}$ Sub.			Signs $\frac{2}{9}$ Sub.			

## 10. To find the present Eccentricity of the Moon.

**T**here are in the same Triangle TCF, given as before, with the Angle CTF just now found, to find the Side TF, the present Eccentricity. *Gregory Astron.* pag. 546.

*Operation.*

As. $\triangle$ CTF, the Equa.	$\{ 7^{\circ} 38' 57''$	Co-Ar.	0.875799
Apog.			
To the Side CF (always the same)	$\{ 11731\frac{1}{2}$	-----	4.069354
To f. $\triangle$ TCF, Double Ano Ar	$\{ 31^{\circ} 00' 10''$	-----	9.711874
To Side TF the Eccentricity	$\{ 45397$	-----	4.657027

## 11. To find the Mean Anomaly of the Moon.

**F**rom the Moon's Place the third time Equated, subtract the Place of the Moon's Apogee the second time Equated, and the Remainder is the Mean Anomaly of the Moon at that Time.

*Operation.*

	f.	o	'	n
From D place the third time Equated	2	23	24	40
Subtract the Place Apogee second time Equ.	1	15	32	48
Remains D Mean Anomaly			1	7 51 52

## 12. To find the Elliptic, or fourth Equation of the Moon.

**I**N the adjacent Figure make LB = LE, and join BE; then is  $FL + LE = AP$ . Make the Angle AFL equal to the Mean Anomaly  $37^{\circ} 51' 52''$ ; The Angle FEL the true Anomaly, and the Angle FLE the Elliptic Equation being the Double of the Angle FBE.

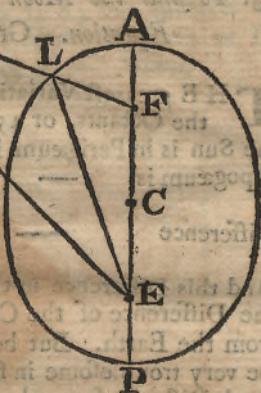
To

To A C the Mean Distance of the Moon from the Earth = 1000000  
 add C E = C F  
 45397 the present Eccentricity, the Sum is 1045397 = to A E the Apogeon Distance: again from A C 1000000 take C E = C F 45397 the remainder is 954603 = A F = E P the Perigeon Distance.

*Gregory's Astron.*  
 Vol. I. pag. 389.

Now say,

Fig. 2.



As the Apogeon Distance, to the Perigeon Distance: so is the Tangent of half her Mean Anomaly, to the Tangent of half the true Anomaly; which subtracted from half the Mean Anomaly, and the Remainder doubled gives the Prosthaphæresis or Elliptic Equation sought; which is to be subtracted from the third Equated Place of the Moon, if the Mean Anomaly be 0, 1, 2, 3, 4, 5 Signs; but added, if it be 6, 7, 8, 9, 10, 11, the Sum or Difference is the fourth Equated Place of the Moon.

#### Operation.

$$\begin{array}{rcl} \text{As } AE & = & 1045397 \text{ Co-Ar. } 3.980719 \\ \text{To } EP & = & 954603 \quad " \quad 5.979822 \\ & - & 9 \quad " \quad " \end{array}$$

$$\text{So t. of half Mean Anomaly } 18 \quad 55 \quad 56 - 9.535301$$

$$\text{To t. of half the true Anomaly } 17 \quad 23 \quad 37 - 9.495842$$

Remains the Angle FBE - 1 32 19

Doubled is =  $\angle FLE$  Equation 3 4 38 Subtract.

13. To find the Moon's Refection, Variation, or fifth  
Equation. Gregory Astron. pag. 548.

~~THE greatest Variation of the Moon is when she is in the Octants, or  $45^\circ$  distant from the Sun, and when the Sun is in Perigæum is  $37' 25''$  in seconds 2245"~~

~~Apogæum is —————— 33 4 —————— 1984~~

~~Difference —————— 4 21 —————— 261~~

And this Difference in the Octants is made reciprocally as the Difference of the Cubes of the Distances of the Sun from the Earth. But because this way of reasoning would be very troublesome in finding the Variation answering the Sun's Distance from the Earth, I have calculated the following Table, which enter with the Sun's Mean Anomaly, and you have the Variation answering. Then from the fourth Equated Place of the Moon, subtract the true Place of the Sun, which double, and say, As Radius to Sine of the double Distance of the Moon from the Sun: so is this Variation in respect of the Sun's Distance from the Earth, to the Variation of the ☽ in respect of the ☉ at that Time.

Operation.

		f.
Eq. pl. ☽	——————	2 20 20 2
☉ place	——————	9 22 23 46
Diff. ☽ à ☉	——————	4 27 56 16
Double	——————	9 25 52 32
Complement	——————	2 4 7 28
Now say,		o' " "
As Radius	——————	90 0 0 - 10.000000
To f. Double	——————	64 7 28 - 9.954119
So ☉ Vari.	——————	- - 2225 - - 3.347330
To ☽ Vari.	——————	2002 - - 3.301449

60) 2002 (33-22

This

(or 19)

This Variation, or fifth Equation of the Moon, is to be added to the 4th Equated Place, if the Distance of the Moon from the Sun be 0, 1, 2, 6, 7, 8; but subtracted if the Distance be 3, 4, 5, 9, 10, 11 Signs, the Sum or Difference is the fifth Equated Place of the Moon.

	V	U	X	W	W	Z	W	Y	
00	0	72	45	05	54	57	0	4	0
01	72	52	45	02	55	52	2	5	2
02	52	55	45	02	55	42	0	5	2
03	12	55	45	02	55	12	0	5	2
04	25	45	45	02	55	12	0	5	2
05	25	45	45	02	55	22	0	5	2
06	25	45	45	02	55	32	0	5	2
07	25	45	45	02	55	42	0	5	2
08	25	45	45	02	55	52	0	5	2
09	25	45	45	02	55	62	0	5	2
10	25	45	45	02	55	72	0	5	2
11	25	45	45	02	55	82	0	5	2
12	25	45	45	02	55	92	0	5	2
13	25	45	45	02	55	102	0	5	2
14	25	45	45	02	55	112	0	5	2
15	25	45	45	02	55	122	0	5	2
16	25	45	45	02	55	132	0	5	2
17	25	45	45	02	55	142	0	5	2
18	25	45	45	02	55	152	0	5	2
19	25	45	45	02	55	162	0	5	2
20	25	45	45	02	55	172	0	5	2
21	25	45	45	02	55	182	0	5	2
22	25	45	45	02	55	192	0	5	2
23	25	45	45	02	55	202	0	5	2
24	25	45	45	02	55	212	0	5	2
25	25	45	45	02	55	222	0	5	2
26	25	45	45	02	55	232	0	5	2
27	25	45	45	02	55	242	0	5	2
28	25	45	45	02	55	252	0	5	2
29	25	45	45	02	55	262	0	5	2
30	25	45	45	02	55	272	0	5	2
31	25	45	45	02	55	282	0	5	2
32	25	45	45	02	55	292	0	5	2
33	25	45	45	02	55	302	0	5	2
34	25	45	45	02	55	312	0	5	2
35	25	45	45	02	55	322	0	5	2
36	25	45	45	02	55	332	0	5	2
37	25	45	45	02	55	342	0	5	2
38	25	45	45	02	55	352	0	5	2
39	25	45	45	02	55	362	0	5	2
40	25	45	45	02	55	372	0	5	2
41	25	45	45	02	55	382	0	5	2
42	25	45	45	02	55	392	0	5	2
43	25	45	45	02	55	402	0	5	2
44	25	45	45	02	55	412	0	5	2
45	25	45	45	02	55	422	0	5	2
46	25	45	45	02	55	432	0	5	2
47	25	45	45	02	55	442	0	5	2
48	25	45	45	02	55	452	0	5	2
49	25	45	45	02	55	462	0	5	2
50	25	45	45	02	55	472	0	5	2
51	25	45	45	02	55	482	0	5	2
52	25	45	45	02	55	492	0	5	2
53	25	45	45	02	55	502	0	5	2
54	25	45	45	02	55	512	0	5	2
55	25	45	45	02	55	522	0	5	2
56	25	45	45	02	55	532	0	5	2
57	25	45	45	02	55	542	0	5	2
58	25	45	45	02	55	552	0	5	2
59	25	45	45	02	55	562	0	5	2
60	25	45	45	02	55	572	0	5	2
61	25	45	45	02	55	582	0	5	2
62	25	45	45	02	55	592	0	5	2
63	25	45	45	02	55	602	0	5	2
64	25	45	45	02	55	612	0	5	2
65	25	45	45	02	55	622	0	5	2
66	25	45	45	02	55	632	0	5	2
67	25	45	45	02	55	642	0	5	2
68	25	45	45	02	55	652	0	5	2
69	25	45	45	02	55	662	0	5	2
70	25	45	45	02	55	672	0	5	2
71	25	45	45	02	55	682	0	5	2
72	25	45	45	02	55	692	0	5	2
73	25	45	45	02	55	702	0	5	2
74	25	45	45	02	55	712	0	5	2
75	25	45	45	02	55	722	0	5	2
76	25	45	45	02	55	732	0	5	2
77	25	45	45	02	55	742	0	5	2
78	25	45	45	02	55	752	0	5	2
79	25	45	45	02	55	762	0	5	2
80	25	45	45	02	55	772	0	5	2
81	25	45	45	02	55	782	0	5	2
82	25	45	45	02	55	792	0	5	2
83	25	45	45	02	55	802	0	5	2
84	25	45	45	02	55	812	0	5	2
85	25	45	45	02	55	822	0	5	2
86	25	45	45	02	55	832	0	5	2
87	25	45	45	02	55	842	0	5	2
88	25	45	45	02	55	852	0	5	2
89	25	45	45	02	55	862	0	5	2
90	25	45	45	02	55	872	0	5	2
91	25	45	45	02	55	882	0	5	2
92	25	45	45	02	55	892	0	5	2
93	25	45	45	02	55	902	0	5	2
94	25	45	45	02	55	912	0	5	2
95	25	45	45	02	55	922	0	5	2
96	25	45	45	02	55	932	0	5	2
97	25	45	45	02	55	942	0	5	2
98	25	45	45	02	55	952	0	5	2
99	25	45	45	02	55	962	0	5	2
100	25	45	45	02	55	972	0	5	2
101	25	45	45	02	55	982	0	5	2
102	25	45	45	02	55	992	0	5	2
103	25	45	45	02	55	1002	0	5	2
104	25	45	45	02	55	1012	0	5	2
105	25	45	45	02	55	1022	0	5	2
106	25	45	45	02	55	1032	0	5	2
107	25	45	45	02	55	1042	0	5	2
108	25	45	45	02	55	1052	0	5	2
109	25	45	45	02	55	1062	0	5	2
110	25	45	45	02	55	1072	0	5	2
111	25	45	45	02	55	1082	0	5	2
112	25	45	45	02	55	1092	0	5	2
113	25	45	45	02	55	1102	0	5	2
114	25	45	45	02	55	1112	0	5	2
115	25	45	45	02	55	1122	0	5	2
116	25	45	45	02	55	1132	0	5	2
117	25	45	45	02	55	1142	0	5	2
118	25	45	45	02	55	1152	0	5	2
119	25	45	45	02	55	1162	0	5	2
120	25	45	45	02	55	1172	0	5	2
121	25	45	45	02	55	1182	0	5	2
122	25	45	45	02	55	1192	0	5	2
123	25	45	45	02	55	1202	0	5	2
124	25	45	45	02	55	1212	0	5	2
125	25	45	45	02	55	1222	0	5	2
126	25	45	45	02	55	1232	0	5	2
127	25	45	45	02	55	1242	0	5	2
128	25	45	45	02	55	1252	0	5	2
129	25	45	45	02	55	1262	0	5	2
130	25	45	45	02	55	1272	0	5	2
131	25	45	45	02	55	1282	0	5	2
132	25	45	45	02	55	1292	0	5	2
133	25	45	45	02	55	1302	0	5	2
134	25	45	45	02	55	1312	0	5	2
135	25	45	45	02	55	1322	0	5	2
136	25	45	45	02	55	1332	0	5	2
137	25	45	45	02	55	1342	0	5	2
138	25	45	45	02	55	1352	0	5	2
139	25	45	45	02	55	1362	0	5	2
140	25	45	45	02	55	1372	0	5	2
141	25	45	45	02	55	1382	0	5	2
142	25	45	45	02	55	1392	0	5	2
143	25	45	45	02	55	1402	0	5	2
144	25	45	45	02	55	1412	0	5	2
145	25	45	45	02	55	1422	0	5	2
146	25	45	45	02	55	1432	0	5	2
147	25	45	45	02	55	1442	0	5	2
148	25	45	45	02	55	1452	0	5	2
149	25	45	45	02	55	1462	0	5	2
150	25	45	45	02	55	1472	0	5	2
151	25	45	45	02	55	1482	0	5	2
152	25	45	45	02	55	1492	0	5	2
153	25	45	45	02	55	1502	0	5	2
154	25	45	45	02	55	1512	0	5	2
155	25	45	45	02	55	1522	0	5	2
156	25	45	45	02	55	1532	0	5	2
157	25	45	45	02	55	1542	0	5	2
158	25	45	45	02	55	1552	0	5	2
159	25	45	45	02	55	1562	0	5	2
160	25	45	45	02	55	1572	0	5	2
161	25	45	45	02	55	1582	0	5	2
162	25	45	45	02	55	1592	0	5	2
163	25	45	45	02					

A Table of the proportional Part of the  
5<sup>th</sup> Equation, or Variation of the Moon.

Anom. ○	Sign 0			Sign I			Sign II			Anom. ○
	I	II	III	I	II	III	I	II	III	
0	33	4	0	33	47	30	34	31	0	30
1	33	5	27	33	48	57	34	32	27	29
2	33	6	54	33	50	24	34	33	54	28
3	33	8	21	33	51	51	34	35	21	27
4	33	9	48	33	53	18	34	36	48	26
5	33	11	15	33	54	45	34	38	15	25
6	33	12	42	33	56	12	34	39	42	24
7	33	14	9	33	57	39	34	41	9	23
8	33	15	36	33	59	6	34	42	36	22
9	33	17	3	34	0	33	34	44	3	21
10	33	18	30	34	2	0	34	45	30	20
11	33	19	57	34	3	27	34	46	57	19
12	33	21	24	34	4	54	34	48	24	18
13	33	22	51	34	6	21	34	49	51	17
14	33	24	18	34	7	48	34	51	18	16
15	33	25	45	34	9	15	34	52	45	15
16	33	27	12	34	10	42	34	54	12	14
17	33	28	39	34	12	9	34	55	39	13
18	33	30	6	34	13	36	34	57	6	12
19	33	31	33	34	15	3	34	58	33	11
20	33	33	0	34	16	30	35	0	0	10
21	33	34	27	34	17	57	35	1	27	9
22	33	35	54	34	19	24	35	2	54	8
23	33	37	21	34	20	51	35	4	21	7
24	33	38	48	34	22	18	35	5	48	6
25	33	40	15	34	23	45	35	7	15	5
26	33	41	42	34	25	12	35	8	42	4
27	33	43	9	34	26	39	35	10	9	3
28	33	44	36	34	28	6	35	11	36	2
29	33	46	3	34	29	33	35	13	3	1
30	33	47	30	34	31	0	35	14	30	0
	Sign 11			Sign 10			Sign 9			

Table of the Proportional Part of the 5<sup>th</sup> E-  
quation, or Variation of the Moon, continu'd.

Anom.	Sign 3	Sign 4	Sign 5	Anom.
	I	II	III	
0	35 14 30	35 58 0	36 41 30	30
1	35 15 57	35 59 27	36 42 57	29
2	35 17 24	36 0 54	36 44 24	28
3	35 18 51	36 2 21	36 45 51	27
4	35 20 18	36 3 48	36 47 18	26
5	35 21 45	36 5 15	36 48 45	25
6	35 23 12	36 6 42	36 50 12	24
7	35 24 39	36 8 9	36 51 39	23
8	35 26 6	36 9 36	36 53 6	22
9	35 27 35	36 11 3	36 54 33	21
10	35 29 0	36 12 30	36 56 0	20
11	35 30 27	36 13 37	36 57 27	19
12	35 31 54	36 15 24	36 58 54	18
13	35 33 21	36 16 51	37 0 21	17
14	35 34 48	36 18 18	37 1 48	16
15	35 36 15	36 19 45	37 3 15	15
16	35 37 42	36 21 12	37 4 42	14
17	35 39 9	36 22 39	37 6 9	13
18	35 40 36	36 24 6	37 7 36	12
19	35 42 3	36 25 33	37 9 3	11
20	35 43 30	36 27 0	37 10 30	10
21	35 44 57	36 28 27	37 11 57	9
22	35 46 24	36 29 54	37 13 24	8
23	35 47 51	36 31 21	37 14 51	7
24	35 49 18	36 32 48	37 16 18	6
25	35 50 45	36 34 15	37 17 45	5
26	35 52 12	36 35 42	37 19 12	4
27	35 53 39	36 37 9	37 20 39	3
28	35 55 6	36 38 36	37 22 6	2
29	35 56 33	36 40 3	37 23 33	1
30	35 58 0	36 41 30	37 25 0	0
	Sign 8	Sign 7	Sign 6	

## Add to the Variation of the Moon.

$\odot$	$f \cdot \frac{5}{8}$	$f \cdot \frac{1}{7}$	$f \cdot \frac{2}{5}$	$\odot$
0	0 0	0 2	54	2 54 30
1	0 6	3 0	2 48	29
2	0 12	3 6	2 42	28
3	0 17	3 11	2 37	27
4	0 23	3 17	2 31	26
5	0 29	3 23	2 25	25
6	0 35	3 29	2 19	24
7	0 41	3 35	2 13	23
8	0 46	3 40	2 8	22
9	0 52	3 46	2 2	21
10	0 58	3 52	1 56	20
11	1 4	3 58	1 50	19
12	1 10	4 4	1 44	18
13	1 15	4 9	1 39	17
14	1 21	4 15	1 33	16
15	1 27	4 21	1 27	15
16	1 33	4 15	1 21	14
17	1 39	4 9	1 15	13
18	1 44	4 4	1 10	12
19	1 50	3 58	1 4	11
20	1 56	3 52	0 58	10
21	2 2	3 46	0 52	9
22	2 8	3 40	0 46	8
23	2 13	3 35	0 41	7
24	2 19	3 29	0 35	6
25	2 25	3 23	0 29	5
26	2 31	3 17	0 23	4
27	2 37	3 11	0 17	3
28	2 42	3 6	0 12	2
29	2 48	3 0	0 6	1
30	2 54	2 54	0 0	0
	$f \cdot \frac{5}{12}$	$f \cdot \frac{4}{7}$	$f \cdot \frac{4}{9}$	

( 23 )

A Table of the Variation or  
5<sup>th</sup> Equation.

$\frac{1}{5}$	$\frac{1}{5}$	$\frac{1}{5}$	$\frac{1}{5}$	$\frac{1}{5}$	$\frac{1}{5}$	$\frac{1}{5}$	$\frac{1}{5}$
0	0	0	28	38	28	38	30
1	1	12	29	11	28	2	29
2	2	21	29	43	27	25	28
3	3	29	30	12	26	45	27
4	4	37	30	39	26	4	26
5	5	46	31	4	25	20	25
6	6	53	31	27	24	34	24
7	7	59	31	47	23	47	23
8	9	7	32	5	22	58	22
9	10	13	32	20	22	7	21
10	11	19	32	34	21	15	20
11	12	24	32	45	20	22	19
12	13	27	32	53	19	26	18
13	14	30	32	58	18	29	17
14	15	32	33	3	17	32	16
15	16	32	33	4	16	32	15
16	17	32	33	3	15	32	14
17	18	29	32	58	14	30	13
18	19	26	32	53	13	27	12
19	20	22	32	45	12	24	11
20	21	15	32	34	11	19	10
21	22	7	32	20	10	13	9
22	22	58	32	5	9	7	8
23	23	47	31	47	7	59	7
24	24	34	31	27	6	53	6
25	25	20	31	4	5	46	5
26	26	4	30	39	4	37	4
27	26	45	30	12	3	29	3
28	27	25	29	43	2	21	2
29	28	2	29	11	1	12	1
30	28	38	28	38	0	0	0
			$\frac{1}{5}$ Sub.	$\frac{4}{5}$ Sub.	$\frac{3}{5}$ Sub.		

## 14. To find the Sixth Equation of the Moon.

OUR Author fixes this Equation at a mean Quantity  $2' 10''$ . This being known; from the Moon's Apogee the second time Equated, subtract the Apogeeon of the Sun, and Note the Remainder.

Also from the Place of the Moon the fifth time Equated, subtract the Sun's true Place, and Note this Remainder, add these two Remainders together, and work as below.

*Operation.*

Place Moon's Apogee second time Equated	1 15 32 48
Place Sun's Apogee subtract	3 8 13 55
Remainder	10 7 18 53
Place of the ☽ the fifth time Equated	2 19 45 40
Sun's Place subtract	9 22 23 46
Remainder	4 27 22 54
Remainder add	10 7 18 53
Sum of these two Remainders	3 4 41 47
Complement	2 25 18 13

Now say,

As Radius	90	0	0 - 10.000000
To Sine Z Remainders	85	18	13 - 9.998539
So is $2' 10''$ in Seconds	-	-	130 - 2.113943
To the Sixth Equation in Seconds	-	129	- 2.112482

This Sixth Equation is to be subtracted from the 5th Equated Place of the Moon, if the aforesaid Sum of the two Remainders (or its Excess above 12 Signs) be less than a Semicircle, or Six Signs; but if it is more, it must be added, the Sum or Difference is the Moon's Longitude the fixt time Equated.

15. To

## 15. To find the Seventh Equation of the Moon.

This Equation Sir Isaac Newton has expressed by this mean Quantity  $2' 20''$ , which, he says, is encreas'd and diminished, according to the Situation of the Lunar Apogæum  $54''$ ; that is, if the Lunar Apogee be join'd with the Sun's Apogæum, the Equation is then  $2' 20'' + 54'' = 3' 14''$ , and also when it is in the Sun's Syzygia; but when it is in the Sun's Quadratures, the aforesaid Equation is to be diminished  $50''$ , and he makes the least Quantity  $1' 26''$ , that is  $2' 20'' - 54''$ . But when the Moon's Apogee and Sun's are in Opposition, he cannot determine (for want of Observation) whether the said Equation is to be encreas'd or diminished.

Therefore, from the sixth Equated Place of the Moon, subtract the Sun's true Place, and the Remainder is the Distance of the Moon from the Sun. Then say,

As Radius, To the Sine of this Distance of the Moon from the Sun, So is  $2' 20''$  in Seconds  $140''$ , To the Seventh Equation of the Moon: which must be subtracted from the sixth Equated Place, if the Distance of the Moon from the Sun be less than 6 Signs, but added when more; the Sum or Difference is the Moon's true Place in her Orbit.

## Operation.

Moon's Longitude the sixth time Equated	f.     °     '     "
Sun's true Place subtract	<u>—</u>
	<u>9 22 23 46</u>
Remains the Distance of the ☽ à ☽ Complement	<u>—</u>
	<u>4 27 20 45</u>
	<u>1 2 39 15</u>

Now say,

As Radius	90 0 0	— 10.000003
To f. Dist. ☽ à ☽	32 39 15	— 9.732045
So $2' 20''$ = Seconds	140	— 2.146128
To 15 the seventh Equation sub.	75	— 1.878173

16. To find the Moon's Latitude, and the Reduction from her Orbit to the Ecliptic.

From the Sun's true Place, subtract the Place of the Moon's North Node first Equated, the Remainder is called the Annual Argument of the Node.

*Operation.*

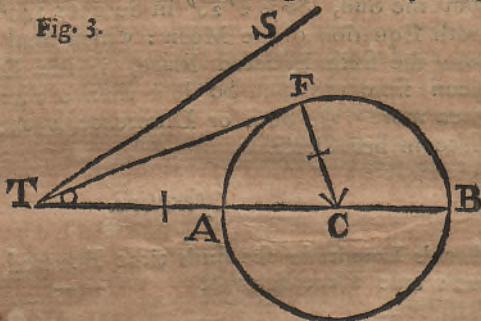
	f. ° ′ ″
Sun's true Place	9 22 23 46
North Node first Equated	10 25 43 30
Rem. Annual Argument of the Node	10 26 40 16
Doubled is	9 23 20 32

From this Work, and from the adjacent Figure, the second Equation of the Node is thus constructed.

Let T represent the Earth, TS, a right Line joining the Earth and

Fig. 3.

Sun: Let TA  
CB represent  
a Line drawn  
to the Place of  
the Moon's a-  
scending Node  
Equated the  
first Time;  
and the Angle  
STA the  
Annual Ar-  
gument of the Node.



Let TA be taken in the same Ratio to AB as 56 to 3. Bisect BA in C, and on the Center C and Radius AC = CB draw the Circle AFB, and let the Angle BCF be equal to Double the Annual Argument in this Example  $133^{\circ} 20' 32''$  as found above; Draw TF, then will the Angle CTF be the second Equation of the Node Ascending. Now in the Oblique-Angled Plain Triangle TFC, there are known, the Sides TC, and CF, with the included

cluded Angle FCT, to find the Angle CTF the present Equation of the Node. For if TA be  $56$ , then AB (by the Theory) is  $3$ , and consequently AC =  $1\frac{1}{2}$ . Therefore  $TC 56 + AC 1\frac{1}{2} = TC 57\frac{1}{2}$ ; then because all Lines drawn from the Center of a Circle to the Circumference thereof are equal, CF is also equal to AC = CB  $1\frac{1}{2}$ , and the Angle TCF is the Complement of the Double of the Annual Argument  $66^{\circ} 39' 28''$  of the Node. This being the second Axiom of oblique-angled Plain Triangles. The first and second Terms in the Analogy are always the same, viz. the Sum of the Sides is ever  $59$ , and their Difference  $56$ : so that as the Sum of the Sides  $59$  is to their Difference  $56$ , so is the Tangent of half the Sum of their opposite Angles (which is ever equal to the Annual Argument of the Node) To the Tangent of half their Difference; which subtracted from half the Sum of the two unknown Angles, leaves the lesser Angle CTF, which is the Equation of the Node.

### *Operation.*

As the Sum of the Sides $TC + CF$ Co-Ar. $59 - 8.229148$	
To their Difference	$56 - 1.748188$
	$0 \quad 1 \quad "$
So t. of half Z opposite Angles	$33 \ 19 \ 44 - 9.817961$
To t. of half their Difference	$31 \ 58 \ 15 - 9.795297$
Remains Equation of the Node	$1 \ 21 \ 29$ Subtract.

This Equation is always to be added to the first Equated Place of the Node, if the Double of the Annual Argument be less than Six Signs; but subtracted, if more. Or with the Distance of the Sun from the Node enter the Table of its Equation (which I have made according to above Directions) and take out the Equation, which apply'd to the first Equated Place according to its Title gives the true Place of the Moon's Ascending Node. Note, add the Co-Ar. of the Logarithm of the two Sides, to the Logarithm of their Difference, and that Sum shall be a constant Logarithm  $9.977336$ .

17. To find the Inclination of the Limit, Gregory  
Astron. pag. 550.

**T**HE Inclination of the Moon's Orb with the Ecliptic, when the Nodes are in the Sun's Quadratures, is  $4^{\circ} 59' 35''$ . And when they are in the Syzigias  $5^{\circ} 17' 20''$ : therefore the greatest Inclination above the least is  $17' 45''$ ; and according to this Limitation I have made the Table of Inclination of the Limit, which enter with the Annual Argument of the Node, or Distance of the Sun from the Node, which in this Example is  $10^{\circ} 26' 40' 16''$ , and take out the Inclination of the Limit,  $12' 26''$ .

18. From the true Place of the Moon in her Orbit, subtract the true Place of the Node last Equated, and the Remainder is the Argument of Latitude  $3^{\circ} 25' 21' 15''$ .

19. With the Argument of Latitude take out of the Table the simple Latitude, as also the Increment or Parts to be added, and reserve them till anon. Greg. 551.

20. Before we can find the Moon's true Latitude, we must find the proportional Part of the Increment thus. As the greatest Inclination of the Moon's Orb and Ecliptic above the least, viz.  $17' 45''$ .

To the present Increment as found by Precept 19.  
So is the present Inclination of the Limit as found by the 17, To the proportional Part of the Increment, which added to the Simple Latitude, as found by the 19, and it gives the Moon's true Latitude.

21. With the Argument of Latitude enter the Table of Reduction, and take out the Reduction, and also the Excess; then, for the proportional Part of the Excess by the Logistical Logarithms, say,  
As the greatest Inclination of the Moon's Orb above the least, viz.  $17' 45''$ .

Is to the present Excess:

So is the present Inclination of the Limit as found by the 17 above,

To

To the proportional Part of the Excess, which added to  
the simple Reduction, gives the true.

22. According to the Title of the Table of Reduction,  
apply the Reduction to the Moon's Orbit Place, and you  
will have the Moon's true Place in the Ecliptic: as you  
may the better perceive by tracing the following Ex-  
amples.

## The first Example of the Sun and Moon's Place.

Equal Time	Long. ☽	Anom. ☽	
	5. ° ′ ″	5. ° ′ ″	
Anno 1729	9 20 56 32	6 12 42 37	
January 1	59 8	59 8	
Mean Mot.	9 21 55 40	6 13 41 45	Anom.
Equat. add	28 6	9 21 55 40	Long. ☽
☽ true Plac.	9 22 23 46	3 8 13 55	Apog. ☽

Equal Time	Long. D.	Apog. D.	Node D.	
	5. ° ′ ″	5. ° ′ ″	5. ° ′ ″	
Anno 1729	2 10 19 39	1 7 42 20	10 25 48 59	
January 1	13 10 35	6 41	3 11	
Mean Mot.	2 23 30 14	1 7 49 1	10 25 45 48	
1 Equation	— 2 51	+ 4 50	— 2 18	
☽ Equated 1	2 23 27 23	1 7 53 51	10 25 43 30	Node Equat.
2 Equation f.	— 2 0	+ 7 38 57	9 22 23 46	Sun's Place.
☽ Equated 2	2 23 25 23	1 15 32 48	10 26 40 16	☽ à ♈.
3 Equation f.	— 43	9 22 23 46	9 23 20 32	Double.
☽ Equated 3	2 23 24 40	8 14 29 55	2 6 39 28	Complement
4 Equation f.	— 3 4 38	4 28 59 50	— 1 21 29	2d Equa. sub.
☽ Equated 4	2 26 20 2	1 1 00 10	10 24 22	1 Nod. true Pl.
5 Equation f.	— 33 22	Eccentricity	— — —	45397
☽ Equated 5	2 29 46 40	Mean Anom.	— — —	1° 7' 51" 52"
6 Equation f.	— 2 9	Inclination of the Limit.	— — —	12 26
☽ Equated 6	2 19 44 31	Simple Latitude	— — —	4 30 37
7 Equation f.	— 1 15	Increment	— — —	16 1
☽ in her Orb.	2 19 43 16	Excess	— — —	36
NorthNod. f.	10 24 22	As the Greatest	17' 45"	Co-Ar. 4709
Arg.Latitud.	3 25 21 15	To Increment	16 1	5736
Tr.Lat. N.D.	4 41 50	So Inclination	12 26	6836
Red. add	+ 5 29	To Increment	11 13	7281
Eclipt. Place	2 19 48 45			

## Example 2.

Equal Time	Long. ⊖	Anom. ⊖		
Anno 1729	6 9 1 "	6 12 42 37		
January 2	9 20 56 32	1 58 17		
Mean Mot.	9 22 54 49	6 14 40 54	Anom.	
Equat. add	30 5	9 22 54 49	Long.	⊖
⊖ true Plac.	9 23 24 54	3 8 13 55	Apog.	

Equal Time	Long. ♂.	Apog. ♂.	Node ♂.	
Anno 1729	6 9 1 "	6 12 42 37	10 25 48 59	Node
January 2	2 10 19 39	1 7 42 20	10 25 48 59	Initial
26 21 10		13 22	6 21	Final
Mean Mot.	3 6 40 49	1 7 55 42	10 25 42 38	
1 Equation	— 3 3	+ 5 10	— 2 21	
D Equated 1	3 6 37 46	1 8 0 52	10 25 40 11	Node Equat.
2 Equation f.	— 1 54	9 23 24 54	9 23 24 54	Sun's Place.
D Equated 2	3 6 35 52	8 15 24 2	10 27 44 43	⊖ à ♀.
3 Equation f.	— 42	5 0 48 4	9 25 29 26	Double.
D Equated 3	3 6 35 10	0 29 11 56	2 4 30 34	Complement.
4 Equation f.	— 3 55 38	+ 7 16 43	— 1 20 1	2d Equa. sub.
D Equated 4	3 2 39 32	1 15 17 35	10 24 20 10	Nod. true Pl.
5 Equation f.	— 24 34			
D Equated 5	3 2 14 58			45173
6 Equation f.	— 2 5			1 21 17 35
D Equated 6	3 2 12 53			3 56 21
7 Equation f.	— 51			12 43
In her Orb.	3 2 12 2			13 58
North Nod. f.	10 24 20 10			0 46
Arg. Latitud.	4 7 51 52	As the Greatest 17' 45"	Co-Ar.	4709
Tr. Lat. N.D.	4 6 22	To Excess — 0 46 —		18935
Reduct. add	+ 6 53	So Inclinat. — 12 43 —		6738
Eclipt. Place	3 2 18 55	To Excess add — 0 33 —		20382

## SECTION II.

*A Problem of the Sphere.*

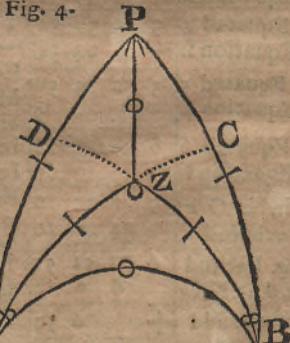
**G**IVEN, Two Altitudes of the Sun upon any Azimuth, with the Time between them, to find the Latitude of the Place.

*Example.* Suppose July 17, at  $10\frac{1}{2}$  in the Forenoon, I observe the Sun's Altitude  $52^{\circ} 59' 5''$ ; and at 2 in the Afternoon the same Day I observe it  $49^{\circ} 51' 5''$ ; What is the Latitude of the Place of Observation?

In the following Figure, A represents the Time and Place of the first Observation, B the second, P the North Pole, Z the Zenith, in which Triangles are given, AP  $70^{\circ} 58'$  the Complement of the Sun's Declination, or its Distance from the North Pole, at the Time of the first Observation; BP  $71^{\circ} 1'$  the Sun's Distance from the North Pole at the Time of the second Observation, with the included Angle at P, viz. APB,  $52^{\circ} 30'$  the Time between the two Observations: Also in the Triangle AZB, there are given AZ  $37^{\circ} 1'$  the Complement of the Sun's Altitude, or its Distance from the Zenith at the Time of the first Observation, and BZ  $40^{\circ} 9'$  the Complement of the Sun's Altitude at the Time of the second Observation, to find ZP the Distance of the Zenith from the Pole equal to the Complement of the Latitude of the Place of Observation.

But before we can find ZP, we must find the Side AB, and the Angles at A and B. This may be effected two Ways; first, as I have shewed in Problem

Fig. 4.



blem 16 of my Doctrine of the Sphere. The other Way is wrought by the versed Sines, as I shall shew following. First in the Triangle A P B, to find the Side A B. This may be done by letting fall a Perpendicular from the Angle A upon B P, as A C; or else B D from the Angle B upon the Side A P, for both will produce the same Thing.

*Operation.*

As C. t. P B	71 1	9.536561	{
To Radius	90 0	10.000000	
So C. f. L. D P B	52 30	9.784447	{
To t. D P - Sub.	60 32	10.247886	
From A P	70 58		{
Remains A D	10 26		
As C. f. D P	60 32	Co. Ar. 0.308108	{
To C. f. A D	10 26	- - - 9.992759	
To C. f. B P	71 1	- - - 9.512275	{
To C. f. A B	49 26	- - - 9.813142	

Or by letting fall the Perpendicular A C.

As C. t. A P	70 58	- - 9.537792	{
To Radius	90 0	- - 10.000000	
So C. f. L. A P C	52 30	- - 9.784447	{
To t. P C. Sub.	60 28	- - 10.246655	
From P B	71 1		{
Remains C B	10 33		
As C. f. P C	60 28	Co. Ar. 0.307242	{
To C. f. C B	10 33	- - - 9.992596	
So C. f. A P	70 58	- - - 9.513375	{
To C. f. A B	49 26	- - - 9.813213	

Secondly, by the Tables of Versed Sines.

To solve this Case without the Help of the Perpendicular, has been long since hinted by Gunter, Speidel, Gellibrand, and Collins; (see Collins's Sector on a Quadrant, Pag. 88.) and since them by Sir Jonas Moore, Harris, &c.

As the Cube of the Radius, Is to the Rectangle of the Sines of the Comprehending Sides:

So is the Square of the Sine of half the Angle contain'd, To half the Difference of the versed Sines of the Third, and of the Ark of Difference between the two including Sides. Which is thus:

Double the Logarithm Sine of half the Angle given, and thereto add the Logarithm Sines of the contain'd Sides, and from the Left-hand of the Sum, dash out or reject 3, for the Cube of the Radius, so there rests the Logarithm of half the Difference of those two versed Sines, which half Difference doubled and added to the versed Sine of the Difference of the Logarithms of the containing Sides, gives the N. versed Sine of the Side sought.

### Operation.

Given Angle A P B	$52^{\circ} 30'$	{ half = $26^{\circ} 15'$	Double Sine } 19.291412
Given Sides { A P	$70^{\circ} 58'$	- Sine	— 9.975583
{ B P	$71^{\circ} 1'$	- Sine	— 9.975713 }
Sum is f. of	10 4	—	9.242708
Natural Sine of	10 4	—	1747939
Doubled is	—	—	3495878
Diff. of the Sides	○ 3	Versed Sine is add.	— 4
Sum is N. Versed f.	49 26	= Side A B -	3495882

Secondly, for the Angle A B P.

As f. A B — 49 26 Co-Ar. 0.119387 Or it may be  
 To f.  $\angle$  A P B  $52^{\circ} 30'$  — 9.899467 found by the 9th  
 So f. A P — 70 58 — 9.975583 Problem of my  
 To f.  $\angle$  A B P  $80^{\circ} 51'$  — 9.994437 Doctrine of the  
 Sphere, &c.

( 35 . )

## 3. For the Angle B A P.

As f. A B	$49^{\circ} 26'$	Co-Ar.	0.119387
To f. $\angle$ APB	52 30	- - -	9.899467
So f. PB	71 1	- - -	9.975713
To f. $\angle$ BAP	80 57	- - -	9.994567

## 4. For the Angle Z A B. By Prob. 9. of my Astron.

Side subtend. the required $\angle$ Z B $49^{\circ} 9'$	A B $49^{\circ} 26'$
$\frac{2}{2} 20$	$4\frac{1}{2}$
$\frac{1}{2} 6$	$12\frac{1}{2}$
X 12 25	

f. AZ	$37^{\circ} 1'$	Co-Ar.	0.220369
f. AB	49 26	Co-Ar.	0.119387
f. Z	26 17	- - -	9.646218
f. X	13 52	- - -	9.379601
Sum Logarithms	—	19.365575	
Sine	23 48	—	9.6827875
Double is 57 36 $\angle$ , Z A B sub.			
B A P	80 57	from	

Z A P      23 21 Rem.

## 5. For the Angle Z B A.

Side subtending the required $\angle$ Z B A	Z B $40^{\circ} 9'$
Angle is A Z — — —	$37^{\circ} 1'$
$\frac{2}{2} 18$	$30\frac{1}{2}$
$\frac{1}{2} 4$	$38\frac{1}{2}$
X 9 17	

F 2

f. B Z

<i>f</i> B Z	40	9	Co-Ar.	- -	0.190581	The three Angles
<i>f</i> B A	49	26	Co-Ar.	- -	0.119387	at the Zenith are
<i>f</i> Z	-	23	9	- - -	9.594547	thus;
<i>f</i> X	-	13	52	- - -	9.379601	A Z P $143^{\circ} 0'$
Z of the Logarithms	- -				19.284116	B Z P $132^{\circ} 56'$
Sine of	26	1	- - -	-	9.642058	A Z B $84^{\circ} 4'$

Double  $52^{\circ} 2' = \angle ZBA$ . Z 360 00  
*A B P* 80 51 Proves the work right.

Z B P 28 49

6. Lastly, for the Side Z P, being the Complement of the Latitude of the Place of Observation.

As <i>f</i> $\angle$ Z P B $30^{\circ}$	o Co Ar. 0.301029
To <i>f</i> . — Z B 40	9 - - - 9.809419
So <i>f</i> . $\angle$ Z B P 28 49	- - - 9.683055
To <i>f</i> . — Z P 38 26	- - - 9.793503
From — 90 o	

Remains — 51 34, the Latitude of the Place North.

And thus may the Latitude of the Place be found without the Meridian Altitude, by taking the Sun's Altitude twice in the Forenoon, or twice in the Afternoon; or by the Moon alone, or by the Moon and any Star, or else by the Altitude of two fixed Stars or Planets, for their Difference of right Ascensions shall be the Angle at the Pole; and then the Things given and required in the Triangle, are the same as above, which needs no Example.

### S E C T. III.

#### *The Use of the Tables of the Satellites of Jupiter and Saturn.*

**T**HIS Part of Astronomy was entirely unknown to the Ancients, till about the Year 1610, when *Gassilanus* in Italy first discover'd that *Jupiter* was environ'd with four Moons or Satellites; and in Germany by *Simon Marius*, by Help of the Telescope, without which,

which, by Reason of *Jupiter's* Splendor, and their small Distance from him, they are not to be discerned. Thus, they being discovered, it put our Moderns upon examining their Motions, and framing a Theory, which is now sufficiently done; and I can now (when *Jupiter* is not too near the Sun) shew them upon Demand to any one that is minded to be satisfied of the Truth hereof. The Circum-saturnials are in Number Five, which by reason of their great Distance from the Sun, and the Smallness of their Bodies, are not to be seen but by the Help of very long Telescopes; the diligent *Cassini* was the first that saw the 1, 2, 3 and 5 Satellites, with a Telescope of 17 Feet, about the End of October in the Year 1671. But the 4th of *Saturn's* Moons was first discover'd by Mr. *Hugens*, Anno 1655. These Satellites of *Jupiter*, as well as of *Saturn*, are called *Secondary Planets, Moons, or Concomitants*; for they constantly keep close to their respective Primarys, and always attend upon them in their Circulations round the Sun; and in the mean time each of them performs his proper Revolution round his proper Primary: The Earth indeed has only the Moon to keep her company, who never forsakes her in her annual Course round the Sun; and while she attends upon us, she performs proper Circulations of her own round the Earth, in the Space of near a Month. The Satellites of *Saturn* have also been seen in *England* by means of that Telescope which was given to the Royal Society by the Dutch Astronomer, Mr. *Hugens*, whose Length is 125 Feet, by which nearly a perfect Theory of their Motions are settled; and from those Observations and Theory, I have formed these Tables of their Motions. To these Satellites belong peculiar Phænomena, which are these: 1. That they cannot be seen with the naked Eye. 2. That they cannot always be seen by them that look at them thro' a Telescope. 3. They always appear in a right Line with their Primary, some to the Right, and some to the Left-Hand; at other times, all to the Right, or all to the Left-Hand. 4. That they are continually changing their apparent Distances from their Primaries, seeming at one time to be near, and at another time further remov'd. 5. That as they are viewed by us from the Earth, they seem to go sometimes to the East, and at other times

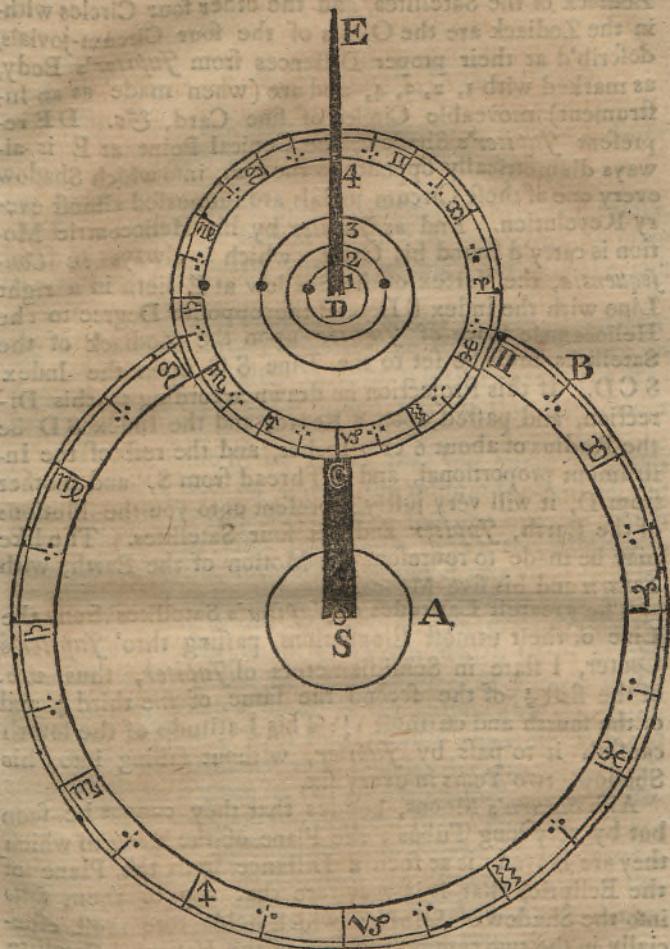
times to move to the West. 6. That when you look at them with two convex Glasses, they always appear on the contrary Side of their Primary to what they really are. 7. That Regard is to be had to the different Situation of the Earth, and the Place of the Observer, from these Phænomena of their Places ; for such a Phænomenon is sooner seen when the Earth is nearer to it, than when it is removed from it. See the Theory of *Jupiter* in my System of the Planets, demonstrated Plate 10. Figure 4. 8. That when  $\text{h}$  is in the Nodes of the Satellites  $\text{M} \text{ X} 21^\circ$ , the Sun is in the Plane of the Ring, from those Places ; therefore the right Ascension and Declination is computed. 9. As far as can be discovered by us at so great a Distance, the Orbit of these Satellites appearing little or nothing eccentric ; and by comparing the Periods of their Motions with the Periods of our Moon round the Earth, and the Periods of *Jupiter* and *Saturn* with the Period of the Earth round the Sun ; the Inequalities in the Motions of these Satellites, may be deriv'd from the Inequalities in the Moon's Motion describ'd above in her Theory. These being their chief Phænomena.

We well know that the Motion of these Satellites are disturbed by the Sun acting upon them, and also by each other's Attraction, and by the Attraction of their Superiors or Primary Planets ; but these Things being more physical than astronomical, I shall not trouble my Reader with them at this Time, but refer them to Sir Isaac Newton's Philosophy, and Gregory's Elements.

The third Satellite from *Jupiter* is of the first Magnitude, the first of that next to his Body is the second Magnitude, the second Satellite is of the third, and the fourth or outermost is of the fourth Magnitude. By these Directions it will not be difficult for an Observer to distinguish one Satellite from another. And the *Hugenean* or fourth of *Saturn's* Satellites, is the greatest of his Guards.

As the  $\text{D}$  (the Earth's Satellite) is carry'd round the Sun along with the Earth in a Year, so are also the Satellites of *Jupiter* and *Saturn* carry'd round the Sun in the times of their respective Revolutions of their Primaries. And for a Demonstration hereof, I have framed the following Diagram after the Nature of my Lunar Instrument, which will make their Motions very plain and easy ; in which

let



let S represent the Sun, A the Earth's Orb, B Jupiter's Orb, divided into the 12 Signs of the Zodiack, the Index C is moveable, and lieth under the Orbs of the Satellites, and terminateth at D, on which Jupiter at D moves round the Sun, and carries his four Satellites along with him; the outmost Circle from Jupiter at D represents the Zodiack marked with the 12 Signs thereof, which I call the Zio-

Zodiack of the Satellites, and the other four Circles within the Zodiack are the Orbits of the four Circum-jovials, describ'd at their proper Distances from *Jupiter's Body*, as marked with 1, 2, 3, 4, and are (when made as an Instrument) moveable Circles of fine Card, &c. DE represent *Jupiter's Shadow*, the Conical Point at E is always diametrically opposite to the Sun, into which Shadow every one of these Circum jovials are immersed almost every Revolution. And as *Jupiter* by his Heliocentric Motion is carry'd round his Orbit, which is always *in Consequentia*, the Vertex of the Shadow at E lieth in a right Line with the Index SD, and the opposite Degree to the Heliocentric Place of *Jupiter* upon the Zodiack of the Satellites must be set to the Line SC upon the Index SCD. If this Projection be drawn according to this Direction, and pasted upon a Board, and the Index SD be the Radius of about 6 or 7 Inches, and the rest of the Instrument proportional, and a Thread from S, and another from D, it will very justly represent unto you the Motions of the Earth, *Jupiter* and his four Satellites. The like may be made to represent the Motion of the Earth, with *Saturn* and his five Moons.

The greatest Latitudes of *Jupiter's Satellites* from the Line of their utmost Elongations, passing thro' *Jupiter's Center*, I state in Semidiameters of *Jupiter*, thus, viz. of the first  $\frac{1}{2}$ , of the second the same, of the third  $\frac{1}{4}$ , and of the fourth and outmost  $1\frac{1}{2}$ : This Latitude of the fourth causeth it to pass by *Jupiter*, without falling into his Shadow, two Years in every six.

Also *Saturn's Moons*, besides that they cannot be seen but by very long Tubes; the Plane of the Ring in which they are moved, is at such a Distance from the Plane of the Ecliptic, that it is very rare that any of them falls into the Shadow of *Saturn*: which holds true most especially in the two remoteft, whereof the *Hugenian Satellite* is one, whose Place I shall shew how to calculate by and by.

## P R E C E P T I.

*Shewing how to calculate the Distances of Jupiter's Satellites, and to distinguish one from another.*

MY Design is here only to shew the ingenious Observer how to find at what Distance from *Jupiter* each Satellite appears, that so he may not mistake one from another.

1. From the Tables in my compleat System of Astronomy to the given Time, calculate the Heliocentric Place of *Jupiter*, as is there shew'd, from which subtract the Radical Place,  $5^{\circ} 13' 22'' 57''$ , and reserve the Remainder till anon.

2. To the same given Time, that you found *Jupiter's* Heliocentric Place to, collect the middle Motions of the Satellite from its respective Table into one Sum, to which Sum, add always (after the Radix 1684) the Difference between the Heliocentric Place of the Radix, and the Heliocentric Place at the given Time just now reserv'd; this Sum is the Place of the Satellite at the given Time, to answer our present Purpose. From which Place of the Satellite, subtract the Heliocentric Place of *Jupiter* at the given Time, what remains is the Distance of the Satellite from *Jupiter*; with this Distance enter the Table of each Satellite's Distance from *u* under the respective Satellite, and there is given its Distance from the Center of *Jupiter* in Semidiameters and decimal Parts. Here note, That if the Distance of the Satellite from *Jupiter* be less than six Signs, it is then in Consequence of *Jupiter*; but if the Distance be more than six Signs, it is in Antecedence, as the said Table will more fully direct you.

*Example.*

Anno 1728, December 16<sup>d</sup> 9<sup>h</sup> 1' 48'', I observed with my  $1\frac{3}{4}$  Feet Tube, and two convex Glasses, the 2d, 3d, and 4th of *Jupiter's* Satellites (the first being at that time eclipsed) how were they by my Satellite Tables?

G

Op-

## Operation.

Equal Time	Long. $\frac{1}{4}$	Anom. $\frac{1}{4}$
1728	s. 0' "	s. 0' "
Dec. 16 Biss.	1 26 56 17	7 16 48 53
Hours 9	29 10 48	29 9 37
1 "	1 52	1 52
1 48		
M. Mot.	2 26 8 57	8 16 00 22
Equat. add.	5 25 56	
$\frac{1}{4}$ Helioc.	3 1 34 55	
Radix sub.	5 13 22 57	
$\frac{1}{4}$ à Radix	9 18 11 58	

Equal Time	Satellite 1.	Satellite 2.	Satellite 3.	Satellite 4.
1728	s. 0' "	s. 0' "	s. 0' "	s. 0' "
Decemb.	1 239 1	2 8 15 54	6 27 46 57	3 24 19 14
Days 16 Biss.	8 17 32 1	11 21 22 34	7 8 19 29	11 26 57 38
Hours 9	7 7 53 54	9 11 57 23	4 13 59 12	5 17 40
Min. 1	2 16 16 38	1 7 59 3	18 50 16	8 3 29
Seconds 48	8 29	4 13	2 6	54
	6 47	3 23	1 40	43
Sum —	5 14 36 50	0 19 42 30	7 8 59 40	4 4 39 38
$\frac{1}{4}$ à Radix	9 18 11 58	9 18 11 58	9 18 11 58	9 18 11 58
Satellite	3 02 48 48	10 7 54 28	4 27 11 38	1 22 51 36
$\frac{1}{4}$ Helioc.	3 1 34 55	3 1 34 55	3 1 34 55	3 1 34 55
Distance.	0 1 13 53	7 6 19 33	1 25 36 43	10 21 16 41

Hence, it appears by the Calculation, that the first Satellite was at the time of the Observation in the Shadow, because its Distance from Jupiter's Heliocentric Place was less than the Semiduration or Half-Stay in the Shadow  $9^{\circ}19'22''$ , and so of the other three.

The 2d and 4th were in Antecedence, and the third Satellite in Consequence of Jupiter : But appear'd on the contrary Side of him, for the Reasons above given.

2. The Satellites of *Saturn* may be found, as I have shewed in *Jupiter's*, with this Difference only, that as *Jupiter's* Satellites are immersed into his Shadow, and *Saturn's* seldom are, that you work with *Saturn's* Geocentric Place, and you will have the Distance of his Moons from him, and also from each other; however, to satisfy the Curious and more Inquisitive, I shall here shew the Method of *Hugens*, improv'd by Dr. *Halley*, in the *Philos. Transact.*

1. By the 8th Precept of my *Compleat System of Astronomy*, find the true Geocentric Place of *Saturn* to the time proposed; from which subtract always the Place of the Apocrion (as they call it)  $11^{\circ} 20' 23'' 48''$ , the Remainder is the Distance of *Saturn* from the Equinox of the Ring. To which Place or Remainder, find the right Ascension and Declination by the 2d and 3d Problems of my Book before cited; only here observe, that you make Use of  $31^\circ$  for the Obliquity or Inclination of this Satellite, instead of  $25^\circ 29'$ .

2. To the Right Ascension thus found, add the Place of the Apocrion  $11^{\circ} 20' 23'' 48''$ , the Sum shall be the Longitude of the Satellites Apogeeon; then say, As Radius, to the Sine of the Declination (found to the Obliquity  $31^\circ$ ) So is 8, To the greatest Latitude in Apogeeon or Perigeon in the Parts of the Semidiameter of the Ring. Or to is 18, to the Parts of the Semidiameter of *Saturn's* Globe.

3. To the given Time collect the middle Motion of the Satellite, and from it subtract the Place of the Apocrion  $11^{\circ} 20' 23'' 48''$ , the Remainder will be the mean Anomaly; with which, in the Table of the Moon's Equation in my *Compleat System of Astronomy*, take out the Equation answering thereto, and the Half thereof added or subtracted to or from the mean Motion, according to the Title of the said Lunar Table, gives the true Motion of the Satellite, from which subtract the Apogeeon as found in the last Precept, and if the Remainder be more than six Signs, the Satellite is Occidental; if less, Oriental: Then as Radius, to the Sine of the Remainder, so is 8, to the Semidiameter of the Ring; or 18 to the Semidiamiter of the Globe, that the Satellite is to the Eastward or Westward of the Center of *Saturn* accordingly.

4. As Radius, to Co-Sine of the said Remainder, so is the greatest Latitude from the Line of the Anſe, found by Precept 2. to the Latitude sought. Example, *Anno 1657, May 19, New Stile, about 10 at Night, Mr. Hugens observed the 4 Satellites very near to ♁ on the Western Side, and very little above the Line of the Anſe.*

*Operation.*

*Anno 1657, May 9<sup>d</sup> 9<sup>h</sup> 40' P. M. at London.*

	f.	°	'	"
Saturn's Geocentric Place	—	5	28	53
Apocranon sub.	—	11	20	23
				48
☿ ab Equinox of the Ring	—	6	8	29
Right Ascension answering	—	6	7	17
Place Apogeeon	—	5	27	40
Declinat. South	—	4	21	0
Greatest Latitude in Apog. $\frac{61}{165}$				
Radix	1651	1	0	48
Mot. for Years sub.	24	8	29	35
				15
Remains the Radix	1657	4	1	13
May	6	9	14	6
Days 9	6	23	11	53
Hours 9	—	8	27	59
Min. 40	—	37	38	
M. Motion	5	12	44	57
Apocr. sub.	11	20	23	48
Anom.	5	22	21	9
Equat. sub.	18	23		
Long. Satell.	5	12	26	34
Apog. sub.	5	27	40	48
Rem.	11	14	45	46
Comple.	0	15	14	14
True Latitude North $\frac{18}{165}$	Parts of the Ring.			
				Here

*Here follows a Catalogue of the Observations from which I constructed these Tables of the Satellites of Jupiter and Saturn.*

*Anno 1657, May 19, N. S. about 10 at Night, Mons. Hugens, with his long Glasses, observed the 4 Satellites of Saturn a little above the Line of the Ansæ, and very near to Saturn on the Western Side, that Planet was then in  $\text{R} 28^{\circ} 53' 8''$ .*

*Anno 1658, Mar. 11, N. S. at 10 P. M. Mons. Hugens observed the same Satellite a little to the East of Saturn, and on the South-side of him.*

*Anno 1659, March 14, N. S. 12<sup>h</sup> P. M. at the Hague, Mons. Hugens observed the 4th Satellite about one Diameter of the Ring under Saturn: but it was gone so far to the Westward, that he concluded, that about four Hours before, or 7<sup>h</sup> 40' at London, it had been in Perigæo.*

*Anno 1659, March 22<sup>d</sup> 10<sup>h</sup> 45' P. M. this Satellite was a whole Diameter above the Line of the Ansæ, and the Perpendicular thereon fell nearly upon the Extremity of the Eastern Ansæ.*

*Anno 1682, November 15<sup>d</sup> 13<sup>h</sup> P. M. Dr. Halley observed Saturn's 4th Satellite in Perigæo on the North Side of him; and a Perpendicular let fall from it on the transverse Diameter of the Ring, fell upon the Middle of the dark Spot of the following Ansæ.*

*Again, November 21<sup>d</sup> 16<sup>h</sup> 15' P. M. this Satellite was on the South Side, the Perpendicular on the Line of the Ansæ fell on the Middle of the dark Spot of the Western Ansæ; and the same Night at 19<sup>h</sup>, the Perpendicular fell precisely on the Center of Saturn; it was now in Apogæo.*

*Anno 1683, Jan. 24, at 8 at Night, he observed this Satellite in Apogæo, the Perpendicular on the Line of the Ansæ fell exactly on the Western Limb of  $\text{h}$ , and at 9<sup>h</sup> 30' the said Perpendicular fell within the Globe more than half Way to the Center, and distant from the Line of the Ansæ towards the South, about one Diameter of the Ring.*

*Anno 1683, Feb. 9<sup>d</sup> 8<sup>h</sup> 10' P. M. this 4th Satellite was in Apogæo, and about one Diameter of Saturn's Ring to the South.*

*Anno*

*Anno 1714, April 4<sup>d</sup> 21<sup>h</sup> 30' N. S.* Mons. *Cassini*, at the Royal Observatory in France, observed the innermost of the Satellites in its inferior Conjunction with *Saturn*, he was then in  $\text{M} 5^{\circ} 23' 32''$  by my Tables, and the same time the second Satellite was in its superior Conjunction with *Saturn*.

*Anno 1714, M. Cassini* observed the third Satellite of *Saturn*, *April 4<sup>d</sup> 10<sup>h</sup>* N. S. to have newly pass'd its inferior Conjunction with *Saturn*, and a Perpendicular from it fell on the Extremity of the Western Ansæ, so that at about 5<sup>h</sup> P. M. it was with the Center of *Saturn* then in  $\text{M} 5^{\circ} 27' \text{R}$ , and consequently the Satellite was in  $\text{X} 5^{\circ} 27'$ .

*Anno 1715, March 25<sup>d</sup> 11<sup>h</sup> P. M.* M. *Cassini* observed the Hugenian or 4<sup>th</sup> Satellite in Apogæo, and did immerge behind the Body of *Saturn*, he was then in  $\text{M} 20^{\circ} 3' 33'' \text{R}$ .

*Anno 1714, May 6<sup>d</sup>, 12<sup>h</sup> P. M.* *Cassini* observed the 5<sup>th</sup> or outermost Satellite in its superior Conjunction with  $\text{h}$  he being then Retrograde in  $\text{M} 4^{\circ} 32' 45''$ .

*Anno 1718, April 21<sup>d</sup> 10<sup>h</sup> 4'*, Mr. *Pound* at *Wansted*, by Help of the Royal Society's 125 Feet Glass, observed the 3<sup>d</sup> and 4<sup>th</sup> Satellites of  $\text{h}$  in Apogæo, a little past their Conjunction with *Saturn*. The first was Northward of the Line of the Ansæ; and therefore in the Apogeon Semicircle distant from the said Line  $\frac{1}{4}$  of *Saturn*'s Semidiameter, and about a Semidiameter of the Ring from the Western Ansæ.

The 2<sup>d</sup> was a very little Southward of the Line of the Ansæ (and therefore in the Perigeon Semicircle) above a Semidiameter of the Ring from the Western Ansæ. The 3<sup>d</sup>, 1<sup>st</sup> and 2<sup>d</sup>, were in a straight Line.

And, *April 22<sup>d</sup> 11<sup>h</sup> 5'* P. M. the four innermost Satellites were all Eastward of  $\text{h}$ , the 2<sup>d</sup> and 4<sup>th</sup> in the Apogeon, and the 1<sup>st</sup> and 3<sup>d</sup> in the Perigeon Semicircle: The 5<sup>th</sup> or outermost Satellite was at this time near its greatest Elongation Eastward.

The Tables of the Satellites of *Jupiter* I have deduced from the Observations of Mr. *Flamsted*, confirmed with abundance of my own.

## A Table of the Mean Motion of the Moon

Years	Long. D.				Apog. D.				Node D.			
	s.	o	/	"	s.	o	/	"	s.	o	/	"
1681	6	1	45	55	8	4	29	45	5	24	13	35
1682	10	11	8	58	9	15	9	35	5	4	53	52
1683	2	20	32	1	10	25	49	26	4	15	34	9
1684	6	29	55	4	0	6	29	18	3	26	14	26
1685	11	22	28	42	1	17	15	49	3	6	51	32
1686	4	1	51	45	2	27	55	39	2	17	31	49
1687	8	11	14	48	4	8	35	29	1	28	12	6
1688	0	20	37	51	5	19	15	20	1	8	52	23
1689	5	13	11	30	7	0	1	51	0	19	29	29
1690	9	22	34	34	8	10	41	42	0	0	9	46
1691	2	1	57	38	9	21	21	32	11	10	50	3
1692	6	11	20	42	11	2	1	23	10	21	30	20
1693	11	3	54	21	0	12	47	54	10	2	7	26
1694	3	13	17	24	1	23	27	45	9	12	47	43
1695	7	22	40	27	3	4	7	35	8	23	28	0
1696	0	2	3	31	4	14	47	26	8	4	8	17
1697	4	24	37	34	5	25	33	57	7	14	45	23
1698	9	4	0	12	7	6	13	48	6	25	25	40
1699	1	13	23	17	8	16	53	38	6	6	5	57
1700	5	22	46	21	9	27	33	28	5	16	46	14
1701	10	15	20	0	11	8	20	0	4	27	23	20
1702	2	24	43	3	0	18	59	50	4	8	3	37
1703	7	4	6	6	1	29	39	40	3	18	43	54
1704	11	13	29	9	3	10	19	31	2	29	24	11
1705	4	6	2	47	4	21	6	2	2	10	1	17
1706	8	15	25	50	6	1	45	52	1	20	41	34
1707	0	24	48	53	7	12	25	42	1	1	21	51

## A Table of the Mean Motion of the Moon

Years	Long. D.				Apog. D.				Node D.			
	s.	o	z	"	s.	o	z	"	s.	o	z	"
1708	5	4	11	56	8	23	5	34	0	12	2	8
1709	9	26	45	34	10	3	52	5	11	22	39	14
1710	2	6	8	38	11	14	31	55	11	3	19	31
1711	6	15	31	40	0	25	11	45	10	13	59	48
1712	10	24	54	45	2	5	51	36	9	24	40	5
1713	3	17	28	24	3	16	38	8	9	5	17	11
1714	7	26	51	27	4	27	17	56	8	15	57	28
1715	0	6	14	31	6	7	57	49	7	26	37	45
1716	4	15	37	36	7	18	37	40	7	7	18	2
1717	9	8	11	15	8	29	24	12	6	21	55	8
1718	1	17	34	19	10	10	4	2	5	28	35	25
1719	5	26	51	23	11	20	43	52	5	9	15	42
1720	10	6	20	27	1	1	23	43	4	19	55	59
1721	2	28	54	5	2	12	10	15	4	0	33	5
1722	7	8	17	8	3	22	50	5	3	11	13	22
1723	11	17	40	11	5	3	29	56	2	21	53	39
1724	3	27	3	14	6	14	9	46	2	2	33	56
1725	8	19	36	52	7	24	56	18	1	13	11	2
1726	0	28	59	55	9	5	36	8	0	23	51	19
1727	5	8	22	58	10	16	15	59	0	4	31	36
1728	9	17	46	1	11	26	55	49	11	15	11	53
1729	2	10	19	39	1	7	42	20	10	25	48	59
1730	6	19	42	42	2	18	21	10	10	6	29	16
1731	10	29	5	46	3	29	2	1	9	17	9	33
1732	3	8	28	50	5	9	41	51	8	27	49	50
1733	8	1	2	29	6	20	28	23	8	8	26	56
1734	0	10	25	33	8	1	8	13	3	19	7	13

in Years Current. To old TA

Years	Long. D.				Apog. D.				Node D.			
	s.	o	g	"	s.	e	f	"	s.	o	f	"
1735	4	19	48	37	9	11	48	4	6	29	47	30
1736	8	29	11	41	10	22	27	54	6	10	27	47
1737	1	21	45	20	0	3	14	26	5	21	4	53
1738	6	1	8	24	1	13	54	16	5	1	45	10
1739	10	10	21	28	2	24	34	7	4	12	25	27
1740	2	19	54	32	4	5	13	58	3	23	5	44
1741	7	12	28	10	5	16	0	30	3	3	42	50
1742	11	21	51	13	6	26	40	20	2	14	23	7
1743	4	1	14	17	8	7	20	11	1	25	3	24
1744	8	10	37	19	9	18	0	0	1	5	43	41
1745	1	3	10	58	10	28	46	32	0	16	20	47
1746	5	12	34	1	0	9	26	12	11	27	1	4
1747	9	21	57	5	1	20	6	13	11	7	41	21
1748	2	1	20	8	3	0	46	3	10	18	21	38
1749	6	23	53	47	4	11	32	34	9	28	58	44
1750	11	3	16	49	5	22	12	24	9	9	39	1
1751	3	12	39	54	7	2	52	15	8	20	19	18
1752	7	22	2	57	8	13	32	5	8	0	59	35
1753	0	14	36	36	9	24	18	38	7	11	36	41
1754	4	23	59	39	11	4	58	28	6	22	16	58
1755	9	3	22	42	0	15	38	19	6	2	57	15
1756	1	12	45	46	1	26	18	9	5	13	37	32
1757	6	5	19	26	3	7	4	41	4	24	14	38
1758	10	14	42	30	4	17	44	32	4	4	54	55
1759	2	24	5	34	5	28	24	22	3	15	35	12
1760	7	3	28	37	7	9	4	13	2	26	15	29
1761	11	26	2	45	8	19	50	45	2	6	52	35

## A Table of the Mean Motion of the Moon

Years	Long. D.				Apog. D.				Node D.			
	s.	o	i	"	s.	o	i	"	s.	o	i	"
1762	4	5	25	18	10	0	30	35	1	17	32	52
1763	8	14	48	22	11	11	10	26	0	28	13	9
1764	0	24	11	25	0	21	50	16	0	8	53	26
1765	5	16	45	4	2	2	36	48	11	19	30	32
1766	9	26	8	8	3	13	16	38	11	0	10	49
1767	2	5	31	11	4	23	56	18	10	10	51	6
1768	6	14	54	15	6	4	36	19	9	21	31	23
1769	11	7	27	54	7	15	22	52	9	2	8	29
1770	3	16	50	57	8	26	2	42	8	12	48	46
1771	7	26	14	1	10	6	42	32	7	23	29	3
1772	0	5	37	4	11	17	22	23	7	4	9	20
1773	4	28	10	43	0	28	8	53	6	14	46	26
1774	9	7	33	46	2	8	48	43	5	25	26	43
1775	1	16	56	50	3	19	28	38	5	6	7	0
1776	5	26	19	53	5	0	8	26	4	16	47	17
1777	10	18	53	32	6	10	54	50	3	27	24	23
1778	2	28	16	35	7	21	34	47	3	8	4	40
1779	7	7	39	39	9	2	14	37	2	18	44	57
1780	11	17	2	42	10	12	54	28	1	29	25	14
1781	4	9	36	20	11	23	41	0	1	10	2	20
1782	8	18	59	23	1	4	20	51	0	20	42	37
1783	0	28	22	27	2	15	0	41	0	1	22	54
1784	5	7	45	30	3	25	40	32	11	12	3	11
1785	10	0	19	9	5	6	27	2	10	22	40	17
1786	2	9	42	12	6	17	6	53	10	3	20	34
1787	6	19	5	16	1	27	46	44	9	14	0	54
1788	10	28	28	19	9	8	26	35	8	24	41	8

in Years Current.

Years	Long. D.				Apog. D.				Node D.			
	s.	o	i	"	s.	o	i	"	s.	o	i	"
1789	3	21	1	57	10	19	13	7	8	5	18	14
1790	8	0	25	1	11	29	52	57	7	15	58	31
1791	0	9	48	4	1	10	32	48	6	26	38	48
1792	4	19	11	8	2	21	12	38	6	7	19	5
1793	9	11	44	47	4	1	59	10	5	17	56	11
1794	1	21	7	50	5	12	39	0	4	28	36	28
1795	6	0	30	54	6	23	18	50	4	9	16	45
1796	10	9	53	57	8	3	58	41	3	19	57	2
1797	3	2	27	36	9	14	45	12	3	0	34	8
1798	7	11	50	59	10	25	25	2	2	11	14	25
1799	11	21	13	43	0	6	4	53	1	21	54	42
1800	4	0	36	46	1	16	44	43	1	2	34	59
1801	8	23	10	25	2	27	31	15	0	13	12	5
1802	1	2	33	28	4	8	11	5	11	23	32	22
1803	5	11	56	32	5	18	50	56	11	4	32	39
1804	9	21	19	35	6	29	30	46	10	15	12	56
1805	2	13	53	14	8	10	17	18	9	25	50	2
1806	6	23	16	17	9	20	57	8	9	6	30	19
1807	11	2	39	21	11	1	36	59	8	17	10	36
1808	3	12	2	24	0	12	16	49	7	27	50	53
1809	8	4	36	3	1	23	3	20	7	8	27	59
1810	0	13	59	6	3	3	43	11	6	19	8	16
1811	4	23	22	10	4	14	23	2	5	29	48	33
1812	9	2	45	13	5	25	2	52	5	10	28	50
1813	1	25	18	51	7	5	49	24	4	21	5	56
1814	6	4	41	55	8	16	29	13	4	1	46	13
1815	10	14	4	58	9	27	9	4	3	12	26	30

## A Table of the Mean Motion of the Moon, &amp;c.

Years	Long. D.				Apog. D.				Node D.			
	s.	o	'	"	s.	o	'	"	s.	o	'	"
1816	2	23	28	2	11	7	48	54	2	23	6	47
1817	7	16	1	41	0	18	35	26	2	3	43	53
1818	11	25	24	44	1	29	15	16	1	14	24	10
1819	4	4	47	48	3	9	55	6	0	25	4	27
1820	8	27	10	51	4	20	34	57	0	5	44	43
1821	1	6	44	30	6	1	21	30	11	16	21	50
1822	5	16	7	33	7	12	1	20	10	27	2	7
1823	9	25	30	37	8	22	41	10	10	7	42	24
1824	2	4	53	41	10	2	21	1	9	18	22	41
1825	6	27	27	19	11	14	7	32	8	23	59	47
1826	11	6	50	23	0	24	47	22	8	9	40	4
1827	3	16	13	26	2	5	27	12	7	20	20	21
1828	7	25	36	30	3	16	7	2	7	1	0	38
1829	0	18	10	9	4	26	53	34	6	11	37	44
1830	4	21	33	12	6	7	33	24	5	22	18	1
1831	9	6	56	35	7	18	13	15	5	2	58	18
1832	1	16	19	18	8	28	53	5	4	13	38	35
1833	6	8	52	57	10	9	39	37	3	24	15	41
1834	10	18	16	0	11	20	19	27	3	4	55	58
1835	2	27	39	4	1	0	59	18	2	15	36	15
1836	7	7	2	7	2	11	39	9	1	26	16	32
1837	11	29	35	46	3	22	25	41	1	6	53	38
1838	4	8	54	49	5	3	5	31	0	17	33	55
1839	8	18	21	53	6	13	45	21	11	28	14	12
1840	0	21	44	56	7	24	25	12	11	8	54	29
1841	5	20	18	34	9	5	11	45	10	19	31	36
1842	9	29	41	38	10	15	51	35	10	0	11	53

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## The Mean Motion of the Moon.

## JANUARY.

Days	Long. ♇.			Apog. ♇.			Node ♇.			
	f.	o	/	"	o	/	"	o	/	"
1	0	13	10	35	0	6	41	0	3	11
2	0	26	21	10	0	13	22	0	6	21
3	1	9	31	45	0	20	3	0	9	32
4	1	22	42	20	0	26	44	0	12	43
5	2	5	52	55	0	33	25	0	15	53
6	2	19	3	30	0	40	6	0	19	4
7	3	2	14	5	0	46	48	0	22	14
8	3	15	24	40	0	53	29	0	25	25
9	3	28	35	15	1	0	10	0	28	36
10	4	11	45	50	1	6	51	0	31	46
11	4	24	56	25	1	13	32	0	34	57
12	5	8	7	0	1	20	13	0	38	8
13	5	21	17	35	1	26	54	0	41	18
14	6	4	28	10	1	33	35	0	44	29
15	6	17	38	45	1	40	16	0	47	40
16	7	0	49	20	1	46	57	0	50	50
17	7	13	59	55	1	53	38	0	54	1
18	7	27	10	30	2	0	19	0	57	11
19	8	10	21	5	2	7	0	1	0	22
20	8	23	31	40	2	13	41	1	3	33
21	9	6	42	15	2	20	23	1	6	43
22	9	19	52	50	2	27	4	1	9	54
23	10	3	3	25	2	33	45	1	13	5
24	10	16	14	0	2	40	26	1	16	15
25	10	29	24	35	2	47	7	1	19	26
26	11	12	35	10	2	53	48	1	22	37
27	11	25	45	45	3	0	29	1	25	47
28	0	8	56	20	3	7	10	1	28	58
29	0	22	6	55	3	13	51	1	32	9
30	1	5	17	31	3	20	32	1	35	19
31	1	18	28	6	3	27	13	1	38	33

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The Mean Motion of the Moon

F E B R U A R Y.

Days	Long. D.			Agog. D.			Node D.			
	s.	o	/	"	o	/	"	o	/	"
1	2	1	38	41	3	33	54	1	41	40
2	2	14	49	16	3	40	35	1	44	50
3	2	27	59	51	3	47	16	1	48	1
4	3	11	10	26	3	53	57	1	51	12
5	3	24	21	1	4	0	38	1	54	23
6	4	7	31	36	4	7	19	1	57	33
7	4	20	42	11	4	14	0	2	0	44
8	5	3	52	46	4	20	41	2	3	54
9	5	17	3	21	4	27	22	2	7	6
10	6	0	13	56	4	34	4	2	10	16
11	6	13	24	31	4	40	45	2	13	27
12	6	26	35	6	4	47	26	2	16	37
13	7	9	45	41	4	54	7	2	19	48
14	7	22	56	15	5	0	48	2	22	59
15	8	6	6	50	5	7	29	2	26	9
16	8	19	17	26	5	10	10	2	29	20
17	9	2	28	1	5	20	51	2	32	30
18	9	15	38	36	5	27	32	2	35	41
19	9	28	49	11	5	34	13	2	38	52
20	10	11	59	46	5	40	54	2	42	2
21	10	25	10	21	5	47	36	2	45	13
22	11	8	20	56	5	54	17	2	48	23
23	11	21	31	31	6	0	58	2	51	34
24	0	4	42	6	6	7	39	2	54	45
25	0	17	52	41	6	14	20	2	57	55
26	1	1	3	16	6	21	1	3	1	6
27	1	14	13	51	6	27	42	3	4	16
28	1	27	24	26	6	34	23	3	7	27
29	2	10	35	1	6	41	4	3	10	38

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in Months and Days.

## M A R C H.

Com- mon	Long. D.			Apog. D.			Node D.			Biflex	
	s.	o	/	"	o	/	"	o	/		
1	2	10	35	1	6	41	4	3	10	38	0
2	2	23	45	36	6	47	45	3	13	49	1
3	3	6	56	11	6	54	26	3	16	59	2
4	3	20	6	46	7	1	7	3	20	10	3
5	4	3	17	21	7	7	48	3	23	20	4
6	4	6	27	56	7	14	29	3	26	31	5
7	4	29	38	31	7	21	11	3	29	42	6
8	5	12	49	6	7	27	52	3	32	52	7
9	5	25	59	41	7	34	33	3	36	3	8
10	6	9	10	16	7	41	14	3	39	14	9
11	6	22	20	51	7	47	55	3	42	25	10
12	7	5	31	26	7	54	36	3	45	36	11
13	7	18	42	1	8	1	17	3	48	46	12
14	8	1	52	36	8	7	58	3	51	56	13
15	8	15	3	11	8	14	39	3	55	7	14
16	8	28	13	46	8	21	20	3	58	18	15
17	9	11	24	21	8	28	1	4	1	28	16
18	9	24	34	56	8	34	42	4	4	39	17
19	10	7	45	31	8	41	23	4	7	49	18
20	10	20	56	7	8	48	4	4	11	0	19
21	11	4	6	42	8	54	45	4	14	11	20
22	11	17	17	17	9	1	27	4	17	22	21
23	0	0	27	52	9	8	8	4	20	32	22
24	0	13	38	27	9	14	49	4	23	43	23
25	0	26	49	2	9	21	30	4	26	53	24
26	1	9	59	37	9	28	11	4	30	4	25
27	1	23	10	12	9	34	52	4	33	15	26
28	2	6	20	47	9	41	33	4	36	25	27
29	2	19	31	22	9	48	14	4	39	36	28
30	3	2	41	51	9	54	55	4	42	47	29
31	3	15	52	32	10	1	36	4	45	58	30

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## The Mean Motion of the Moon

## A P R I L.

Com- mon	Long. D.				Apog. D.				Node. D.				Bifex
	s.	o	l	"	o	l	"	o	l	"	o	l	"
1	3	29	3	7	10	8	17	4	49	8	0	0	0
2	4	12	13	42	10	14	58	4	52	11	1	1	1
3	4	25	24	17	10	21	39	4	55	29	2	2	2
4	5	8	34	52	10	28	20	4	58	40	3	3	3
5	5	21	45	27	10	35	2	5	1	51	4	4	4
6	6	4	56	2	10	41	43	5	5	1	5	5	5
7	6	18	6	38	10	48	24	5	8	12	6	6	6
8	7	1	17	12	10	55	5	5	11	22	7	7	7
9	7	14	27	47	11	1	46	5	14	33	8	8	8
10	7	27	38	22	11	8	27	5	17	44	9	9	9
11	8	10	48	57	11	15	8	5	20	54	10	10	10
12	8	23	59	32	11	21	49	5	24	5	11	11	11
13	9	7	10	7	11	28	30	5	27	16	12	12	12
14	9	20	20	42	11	35	11	5	30	26	13	13	13
15	10	3	31	17	11	41	52	5	33	37	14	14	14
16	10	16	41	52	11	48	33	5	36	48	15	15	15
17	10	29	52	27	11	55	14	5	39	58	16	16	16
18	11	13	3	2	12	1	55	5	43	9	17	17	17
19	11	26	13	37	12	8	36	5	46	15	18	18	18
20	0	9	24	12	12	15	18	5	49	31	19	19	19
21	0	22	34	47	12	21	59	5	52	41	20	20	20
22	1	5	45	22	12	28	40	5	55	52	21	21	21
23	1	18	55	47	12	35	21	5	59	2	22	22	22
24	2	2	6	32	12	42	2	6	2	13	23	23	23
25	2	15	17	7	12	48	43	6	5	54	24	24	24
26	2	28	27	42	12	55	24	6	8	34	25	25	25
27	3	11	38	17	13	2	5	6	11	45	26	26	26
28	3	24	48	52	13	8	46	6	14	56	27	27	27
29	4	7	59	27	13	15	27	6	18	6	28	28	28
30	4	21	10	3	13	22	8	6	21	17	29	29	29
31	5	4	20	37	13	28	49	6	24	27	30		

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in Months and Days.

M A Y.

Com. mon	Long. D.				Apog. D.				Node D.				Bissext.			
	s	o	d	"	o	j	"	o	i	"	o	i	"	o	i	"
1	5	4	20	37	13	28	49	6	24	27	0	1	21	3	4	5
2	5	17	31	32	13	35	30	6	27	38	6	1	21	6	7	8
3	6	0	41	47	13	42	11	6	30	48	6	1	21	7	8	9
4	6	13	52	22	13	48	52	6	33	59	6	1	21	8	9	10
5	6	27	2	57	13	55	34	6	37	10	6	1	21	9	10	11
6	7	10	13	32	14	2	15	6	40	20	5	6	1	21	10	11
7	7	23	24	7	14	8	56	6	43	31	5	6	1	21	6	7
8	8	6	34	42	14	15	37	6	46	41	6	7	1	21	7	8
9	8	19	45	17	14	22	18	6	49	52	6	8	1	21	9	10
10	9	2	55	53	14	28	59	6	53	3	6	9	1	21	10	11
11	9	16	6	27	14	35	40	6	56	14	6	10	1	21	11	12
12	9	29	17	3	14	42	21	6	59	24	6	11	1	21	12	13
13	10	12	27	38	14	49	2	7	2	34	7	12	1	21	13	14
14	10	25	38	13	14	55	43	7	5	45	7	15	1	21	14	15
15	11	8	48	48	15	2	24	7	8	56	7	18	1	21	15	16
16	11	21	59	23	15	9	5	7	12	6	7	15	1	21	16	17
17	0	5	9	58	15	15	46	7	15	17	7	18	1	21	17	18
18	0	18	23	33	15	22	28	7	18	27	7	21	1	21	18	19
19	1	1	31	8	15	29	9	7	21	38	7	24	1	21	19	20
20	1	14	41	43	15	35	50	7	24	49	7	27	1	21	20	21
21	1	27	52	18	15	42	31	7	28	0	7	31	1	21	21	22
22	2	11	2	53	15	49	12	7	31	10	7	34	2	21	22	23
23	2	24	13	28	15	55	53	7	34	21	7	43	3	21	24	25
24	3	7	24	3	16	2	34	7	37	32	7	46	4	21	25	26
25	3	20	34	38	16	9	15	7	40	43	7	43	5	21	24	25
26	4	8	45	13	16	15	56	7	43	53	7	47	6	21	25	26
27	4	16	55	48	16	22	37	7	47	4	7	50	7	21	27	28
28	5	0	6	23	16	29	18	7	53	25	7	56	36	21	27	28
29	5	13	16	58	16	35	59	7	53	25	7	59	46	21	27	29
30	5	26	27	33	16	42	40	7	56	36	7	59	46	21	27	29
31	6	9	38	8	16	49	21	7	59	46	7	59	46	21	27	30

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The Mean Motion of the Moon

J U N E.

Com- mon Year	Long. D.				Apog. D.				Node. D.				Biflex
	s.	o	l	n	o	y	n	o	l	"	n	n	
1	6	22	48	43	16	56	3	8	2	56	0	1	2
2	7	5	59	18	17	2	44	8	6	7	1	2	3
3	7	19	9	53	17	9	25	8	9	18	2	3	4
4	8	2	20	28	17	16	6	8	12	29	3	4	5
5	8	15	31	3	17	22	47	8	15	39	4	5	6
6	8	28	41	38	17	29	28	8	18	50	5	6	7
7	9	11	52	13	17	36	9	8	22	0	6	7	8
8	9	25	2	48	17	42	50	8	25	11	7	8	9
9	10	8	13	23	17	49	31	8	28	22	1	2	3
10	10	21	23	58	17	56	12	8	31	32	9	10	11
11	11	4	34	33	18	2	53	8	34	43	10	11	12
12	11	17	45	8	18	9	34	8	37	54	11	12	13
13	0	0	55	43	18	16	15	8	41	5	12	13	14
14	0	14	6	18	18	22	56	8	44	16	13	14	15
15	0	27	16	53	18	29	37	8	47	26	14	15	16
16	1	10	27	28	18	36	19	8	50	37	15	16	17
17	1	23	38	3	18	43	0	8	53	47	16	17	18
18	2	6	48	38	18	49	41	8	56	58	17	18	19
19	2	19	59	13	18	52	22	9	0	9	18	19	20
20	3	3	9	48	19	3	3	9	3	19	19	20	21
21	3	16	20	23	19	9	44	9	6	30	20	21	22
22	3	29	30	58	19	16	25	9	9	40	21	22	23
23	4	12	41	33	19	23	6	9	12	51	22	23	24
24	4	25	52	8	19	29	47	9	16	2	23	24	25
25	5	9	2	43	19	36	28	9	19	12	24	25	26
26	5	22	13	18	19	43	9	9	22	23	25	26	27
27	6	5	23	53	19	49	50	9	25	34	26	27	28
28	6	18	34	28	19	56	31	9	28	45	27	28	29
29	7	1	45	4	20	3	12	9	31	53	28	29	30
30	7	14	55	39	20	9	54	9	35	6	29	30	31
31	7	28	6	14	20	16	35	9	38	16	30	31	32

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in Months and Days.

J U L Y.

Com. mon	Long. D.			Apog. D.			Node D.			Bissext.	
	s.	°	/	"	°	/	"	°	/	"	
1	7	28	6	14	20	16	35	9	38	16	0
2	8	11	16	49	20	23	16	9	41	27	1
3	8	24	27	24	20	29	57	9	44	37	2
4	9	7	37	59	20	36	38	9	47	48	3
5	9	20	48	34	20	43	19	9	50	59	4
6	10	3	59	9	20	50	0	9	54	9	5
7	10	17	9	44	20	56	41	9	57	20	6
8	11	0	20	19	21	3	22	10	0	30	7
9	11	13	30	54	21	10	3	10	3	41	8
10	11	26	41	29	21	16	44	10	6	51	9
11	0	9	52	4	21	23	25	10	10	2	10
12	0	23	2	39	21	30	6	10	13	13	11
13	1	6	13	14	21	36	47	10	16	24	12
14	1	19	23	49	21	43	28	10	19	35	13
15	2	2	34	24	21	50	9	10	22	45	14
16	2	15	44	59	21	56	52	10	25	56	15
17	2	28	55	34	22	3	32	10	29	6	16
18	3	12	6	9	22	10	13	10	32	17	17
19	3	25	16	44	22	16	54	10	35	28	18
20	4	8	27	19	22	23	35	10	38	39	19
21	4	21	37	54	22	30	15	10	41	49	20
22	5	4	48	29	22	36	56	10	45	0	21
23	5	17	59	4	22	43	37	10	48	11	22
24	6	1	9	39	22	50	19	10	51	21	23
25	6	14	20	14	22	57	0	10	54	32	24
26	6	27	30	49	23	3	41	10	57	42	25
27	7	10	41	20	23	10	22	11	0	53	26
28	7	23	51	59	23	17	3	11	4	3	27
29	8	7	2	34	23	23	44	11	7	14	28
30	8	20	13	9	23	30	25	11	10	25	29
31	9	3	23	44	23	37	6	11	13	36	30

## The Mean Motion of the Moon

## A U G U S T.

Com- mon	Long. D.				Agog. D.			Node D.			Biflex
	s.	o	/	"	o	/	"	o	/	"	
1	9	16	34	19	23	43	47	11	16	47	0
2	9	29	44	54	23	50	28	11	19	58	1
3	10	12	55	29	23	57	9	11	23	8	2
4	10	26	6	4	24	3	51	11	26	19	3
5	11	9	16	39	24	10	32	11	29	29	4
6	11	22	27	14	24	17	30	11	32	40	5
7	0	5	37	49	24	23	54	11	35	51	6
8	0	18	48	24	24	30	35	11	39	2	7
9	1	1	58	59	24	37	16	11	42	12	8
10	1	15	9	34	24	43	57	11	45	23	9
11	1	28	20	9	24	50	38	11	48	33	10
12	2	11	30	44	24	57	19	11	51	44	11
13	2	24	41	19	25	4	0	11	54	54	12
14	3	7	51	54	25	10	42	11	58	5	13
15	3	21	2	29	25	17	23	12	1	15	14
16	4	4	13	4	25	24	4	12	4	26	15
17	4	17	23	40	25	30	45	12	7	36	16
18	5	0	34	15	25	37	26	12	10	47	17
19	5	13	44	50	25	44	7	12	13	58	18
20	5	26	55	25	25	50	48	12	17	8	19
21	6	10	6	0	25	57	29	12	20	19	20
22	6	23	16	35	26	4	10	12	23	29	21
23	7	6	27	10	26	10	51	12	26	40	22
24	7	19	37	45	26	17	32	12	29	51	23
25	8	2	48	20	26	24	13	12	33	1	24
26	8	15	58	55	26	30	55	12	36	12	25
27	8	29	9	30	26	37	36	12	39	23	26
28	9	12	20	5	26	44	17	12	42	34	27
29	9	25	30	40	26	50	58	12	45	44	28
30	10	8	41	15	26	57	39	12	48	55	29
31	10	21	51	50	27	4	20	12	52	5	30

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in Months and Days.

S E P T E M B E R.

Com- mon	Long. D.				Apog. D.				Node D.				Biffrx
	s.	o	'	"	s.	o	'	"	s.	o	'	"	
1	II	9	2	25	0	27	11	1	12	55	16	0	0
2	II	18	13	0	0	27	17	42	12	58	27	1	2
3	0	1	23	35	0	27	24	23	13	1	37	1	1
4	0	14	34	10	0	27	31	4	13	4	48	3	3
5	0	27	44	45	0	27	37	45	13	7	58	4	4
6	1	10	55	20	0	27	44	26	13	11	9	5	5
7	1	24	5	55	0	27	51	7	13	14	20	6	6
8	2	7	16	30	0	27	57	48	13	17	31	7	7
9	2	20	27	5	0	28	4	29	13	20	41	8	8
10	3	3	37	40	0	28	11	11	13	23	52	9	9
11	3	16	48	15	0	28	17	52	13	27	3	10	10
12	3	29	58	50	0	28	24	33	13	30	14	11	11
13	4	13	9	25	0	28	31	14	13	33	24	12	12
14	4	26	20	0	0	28	37	55	13	36	35	13	13
15	5	9	30	35	0	28	44	36	13	39	45	14	14
16	5	22	41	10	0	28	51	17	13	42	56	15	15
17	6	5	51	45	0	28	57	58	13	46	7	16	16
18	6	19	2	20	0	29	4	39	13	49	17	17	17
19	7	2	12	55	0	29	11	20	13	52	28	18	18
20	7	15	23	30	0	29	18	1	13	55	38	19	19
21	7	28	34	5	0	29	24	42	13	58	49	20	20
22	8	11	44	40	0	29	31	23	14	2	0	21	21
23	8	28	55	15	0	29	38	4	14	5	10	22	22
24	9	8	5	50	0	29	44	45	14	8	21	23	23
25	9	21	16	25	0	29	51	27	14	11	31	24	24
26	10	4	27	0	0	29	58	8	14	14	42	25	25
27	10	17	37	35	1	0	4	49	14	17	53	26	26
28	11	0	48	10	1	0	11	30	14	21	3	27	27
29	11	13	58	45	1	0	18	11	14	24	14	28	28
30	11	27	9	20	1	0	24	52	14	27	24	29	29
31	0	10	19	55	1	0	31	33	14	30	35	30	30

## The Mean Motion of the Moon

O C T O B E R.

Com- mon mon	Long. D.			Apog. D.			Node D.			Biflex		
	s.	o	l	"	s.	o	l	"	o	l	"	
1	0	10	19	55	1	0	31	33	14	30	25	0
2	0	23	30	30	1	0	38	14	14	33	46	1
3	1	6	41	5	1	0	44	55	14	36	56	2
4	1	19	51	40	1	0	51	36	14	40	7	3
5	2	3	2	15	1	0	58	17	14	43	17	4
6	2	16	12	50	1	1	4	58	14	46	28	5
7	2	29	23	26	1	1	11	39	14	49	39	6
8	3	12	34	1	1	1	18	20	14	52	50	7
9	3	25	44	36	1	1	25	2	14	56	0	8
10	4	8	55	11	1	1	31	43	14	59	11	9
11	4	22	5	46	1	1	38	24	15	2	21	10
12	5	5	16	21	1	1	45	5	15	5	32	11
13	5	8	26	56	1	1	51	46	15	8	43	12
14	6	1	37	31	1	1	58	27	15	11	53	13
15	6	14	48	6	1	2	5	8	15	15	4	14
16	6	27	58	41	1	2	11	49	15	18	15	15
17	7	11	9	16	1	2	18	30	15	21	26	16
18	7	24	19	51	1	2	25	11	15	24	36	17
19	8	7	30	26	1	2	31	52	15	27	47	18
20	8	20	41	1	1	2	38	33	15	30	57	19
21	9	3	51	36	1	2	45	14	15	34	8	20
22	9	17	2	11	1	2	51	55	15	37	19	21
23	10	0	12	46	1	2	58	36	15	40	29	22
24	10	13	23	21	1	3	5	17	15	43	40	23
25	10	26	33	56	1	3	11	58	15	46	50	24
26	11	9	44	31	1	3	18	39	15	50	1	25
27	11	22	55	6	1	3	25	21	15	53	12	26
28	0	6	5	41	1	3	32	2	15	56	22	27
29	0	19	16	16	1	3	38	43	15	59	33	28
30	1	2	26	51	1	3	45	24	16	2	43	29
31	1	15	37	26	1	3	52	5	16	5	54	30

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in Months and Days.

N O V E M B E R.

Com- mon	Long. D.				Apog. D.				Node D.				Bissext 
	f.	g.	h.	"	f.	o.	/	"	o	/	"		
1	1	28	48	I	1	3	58	46	16	9	5	0	
2	2	11	58	36	1	4	5	27	16	12	16	1	
3	2	25	9	11	1	4	12	8	16	15	26	2	
4	3	8	19	46	1	4	18	49	16	18	37	3	
5	3	21	30	21	1	4	25	30	16	21	48	4	
6	4	4	40	56	1	4	32	11	16	24	59	5	
7	4	17	51	31	1	4	38	53	16	28	9	6	
8	5	1	2	6	1	4	45	34	16	31	20	7	
9	5	14	12	41	1	4	52	15	16	34	30	8	
10	5	27	23	16	1	4	58	56	16	37	41	9	
11	6	10	33	51	1	5	5	37	16	40	52	10	
12	6	23	44	26	1	5	12	10	16	44	2	11	
13	7	6	55	I	1	5	18	59	16	47	13	12	
14	7	20	5	36	1	5	25	40	16	50	23	13	
15	8	3	16	11	1	5	32	21	16	53	34	14	
16	8	16	26	46	1	5	39	2	16	56	45	15	
17	8	29	37	21	1	5	45	43	16	59	55	16	
18	9	12	47	56	1	5	52	24	17	3	6	17	
19	9	25	58	31	1	5	59	5	17	16	16	18	
20	10	9	9	6	1	6	5	46	17	9	27	19	
21	10	22	19	41	1	6	12	27	17	12	38	20	
22	11	5	30	16	1	6	19	9	17	15	49	21	
23	11	18	40	51	1	6	25	50	17	18	59	22	
24	0	1	51	26	1	6	32	31	17	22	10	23	
25	0	15	2	2	1	6	39	12	17	25	21	24	
26	0	28	12	37	1	6	45	53	17	28	32	25	
27	1	11	23	12	1	6	52	34	17	31	42	26	
28	1	24	33	47	1	6	59	15	17	34	53	27	
29	2	7	44	22	1	7	5	56	17	38	3	28	
30	2	20	54	57	1	7	12	37	17	41	14	29	
31	3	4	5	32	1	7	19	18	17	44	25	30	

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The Mean Motion of the Moon, &c.

D E C E M B E R.

Com. mon	Long. D.	Apog. D.	Node D.	Bifex
	s. ° ′ ″	s. ° ′ ″	° ′ ″	
1	3 4 5 32	1 7 19 18	17 44 25	0
2	3 17 16 7	1 7 25 59	17 47 35	1
3	4 0 26 42	1 7 32 40	17 50 46	2
4	4 13 37 17	1 7 39 21	17 53 56	3
5	4 26 47 52	1 7 46 2	17 57 7	4
6	5 9 58 27	1 7 52 43	18 0 18	5
7	5 23 9 2	1 7 59 24	18 3 28	6
8	6 6 19 37	1 8 6 6	18 6 39	7
9	6 19 30 12	1 8 12 47	18 9 49	8
10	7 2 40 47	1 8 19 28	18 13 0	9
11	7 15 51 22	1 8 26 9	18 16 11	10
12	7 29 1 57	1 8 32 50	18 19 21	11
13	8 12 12 32	1 8 39 31	18 22 32	12
14	8 25 23 7	1 8 46 12	18 25 42	13
15	9 8 33 42	1 8 52 53	18 28 53	14
16	9 21 44 17	1 8 59 34	18 32 4	15
17	10 4 54 52	1 9 6 15	18 35 15	16
18	10 18 5 27	1 9 12 56	18 38 25	17
19	11 1 16 2	1 9 19 38	18 41 36	18
20	11 14 26 37	1 9 26 19	18 44 47	19
21	11 27 37 12	1 9 33 0	18 47 58	20
22	0 10 47 47	1 9 39 41	18 51 9	21
23	0 23 58 22	1 9 46 22	18 54 19	22
24	1 7 8 57	1 9 53 3	18 57 30	23
25	1 20 19 32	1 9 59 44	19 0 41	24
26	2 3 30 7	1 10 6 25	19 3 51	25
27	2 16 40 42	1 10 13 6	19 7 2	26
28	2 29 51 17	1 10 19 47	19 10 12	27
29	3 13 1 52	1 10 26 28	19 13 23	28
30	3 26 12 27	1 10 33 9	19 16 33	29
31	4 9 23 2	1 10 39 50	19 19 43	30

The Moon's mean Motion in Hours,  
Minutes and Seconds.

H	Long. D.	Apog. D.	Node D.
	o' " "	o' " "	o' " "
	I" III	" III	" III
1	0 32 56	0 17	0 8
2	1 5 53	0 33	0 16
3	1 38 49	0 50	0 24
4	2 11 46	1 7	0 32
5	2 44 42	1 24	0 40
6	3 17 39	1 40	0 48
7	3 50 35	1 57	0 56
8	4 23 32	2 14	1 4
9	4 56 28	2 30	1 12
10	5 29 25	2 47	1 19
11	5 2 21	3 4	1 27
12	6 35 18	3 21	1 35
13	7 8 14	3 37	1 43
14	7 41 10	3 54	1 51
15	8 14 7	4 11	1 59
16	8 47 3	4 27	2 7
17	9 20 0	4 44	2 15
18	9 52 56	5 1	2 23
19	10 25 53	5 18	2 31
20	10 58 49	5 34	2 39
21	11 31 46	5 51	2 47
22	12 4 42	6 8	2 55
23	12 37 39	6 24	3 3
24	13 10 35	6 41	3 11
25	13 43 32	6 58	3 19
26	14 16 28	7 15	3 27
27	14 49 24	7 31	3 34
28	15 22 21	7 48	3 42
29	15 55 17	8 5	3 50
30	16 28 14	8 21	3 58

The Moon's mean Motion in Hours,  
Minutes and Seconds, continu'd.

H	Long. ♂.	Apog. ♂.	Node ♂.
	°	"	"
/	/	III	III
/	/	III	III
31	17 28 14	8 38	4 6
32	17 34 7	8 54	4 14
33	18 7 3	9 11	4 22
34	18 39 59	9 28	4 30
35	19 12 55	9 45	4 38
36	19 45 52	10 2	4 46
37	20 18 48	10 19	4 54
38	20 51 45	10 36	5 2
39	21 24 41	10 52	5 10
40	21 27 38	11 8	5 18
41	22 30 34	11 25	5 26
42	23 3 31	11 42	5 34
43	23 36 27	11 59	5 42
44	24 9 24	12 16	5 50
45	24 42 20	12 32	5 58
46	25 15 17	12 48	6 6
47	25 48 13	13 5	6 14
48	26 21 10	13 22	6 22
49	26 54 6	13 39	6 30
50	27 27 3	13 56	6 38
51	27 59 59	14 13	6 46
52	28 32 56	14 30	6 54
53	29 5 52	14 46	7 1
54	29 38 49	15 2	7 8
55	30 11 45	15 19	7 16
56	30 44 42	15 36	7 24
57	31 17 38	15 53	7 32
58	31 50 34	16 10	7 40
59	32 23 31	16 26	7 48
60	32 56 27	16 43	7 56

A Table of the 2d Equation of the Node, and Inclination of the Limit above  $4^{\circ} 59' 35''$ .

$\odot$	Signs o & 6.		Signs 1 & 7.		Signs 2 & 8.		$\odot$
$\odot$	Eq. Add.	Incli.	Eq. Add.	Incli.	Eq. Add.	Incli.	$\odot$
0	o 1 11	1 11	o 1 11	1 11	o 1 11	1 11	—
1	o 0 0	17 45	i 16 40	13 22	i 18 41	4 27	30
2	o 3 3	17 45	i 18 15	13 6	i 17 6	4 11	29
3	o 6 6	17 44	i 19 41	12 49	i 15 26	3 55	28
4	o 9 8	17 44	i 21 3	12 32	i 13 41	3 40	27
5	o 12 10	17 42	i 22 20	12 15	i 11 49	3 25	26
6	o 15 11	17 40	i 23 31	11 58	i 9 52	3 11	25
7	o 18 11	17 37	i 24 36	11 41	i 7 50	2 57	24
8	o 21 11	17 33	i 25 34	11 24	i 5 42	2 43	23
9	o 24 7	17 28	i 26 27	11 7	i 3 29	2 29	22
10	o 27 3	17 22	i 27 14	10 49	i 1 11	2 16	21
11	o 29 57	17 15	i 27 54	10 31	o 58 49	2 4	20
12	o 32 48	17 8	i 28 28	10 13	o 56 22	1 53	19
13	o 35 38	17 0	i 28 56	9 55	o 53 51	1 42	18
14	o 38 25	16 52	i 29 17	9 37	o 51 15	1 31	17
15	o 41 10	16 44	i 29 32	9 18	o 48 36	1 21	16
16	o 43 51	16 35	i 29 40	8 59	o 45 53	1 11	15
17	o 46 30	16 26	i 29 40	8 40	o 43 6	1 2	14
18	o 49 5	16 17	i 29 37	8 20	o 40 16	o 53	13
19	o 51 37	16 7	i 29 25	8 0	o 37 22	o 45	12
20	o 54 6	15 56	i 29 7	7 40	o 34 26	o 38	11
21	o 56 31	15 44	i 28 42	7 21	o 31 27	o 32	10
22	o 58 52	15 32	i 28 11	7 2	o 28 25	o 26	9
23	i 1 9	15 19	i 27 33	6 44	o 25 22	o 21	8
24	i 3 22	15 6	i 26 49	6 26	o 22 16	o 16	7
25	i 5 30	14 52	i 25 58	6 8	o 19 8	o 12	6
26	i 7 34	14 38	i 25 0	5 50	o 15 59	o 8	5
27	i 9 32	14 24	i 23 57	5 33	o 12 49	o 5	4
28	i 11 27	14 9	i 22 47	5 16	o 9 38	o 3	3
29	i 13 16	13 54	i 21 31	4 59	o 6 26	o 1	2
30	i 15 1	13 38	i 20 9	4 43	o 3 13	o 0	1
	i 16 40	13 22	i 18 41	4 27	o 0 0	o 0	0
	Signs 5 { Subt.		Signs 4 { Subt.		Signs 3 { Subt.		
	11	10	10	9	9		

A Table of the Simple Latitude of the Moon fitted  
to the least Inclination of its Orbit, with the Incre-  
ments to the greatest Inclination.

Arg. L.	Latit.		Incre- ment		Latit.		Incre- ment		Latitude		Incre- ment		Arg. L.
	N.	A.	N. A.	Add.	i	N. A.	i	N. A.	2 N. A.	8 S. A.	i	"	
	o	'	o	"	o	'	o	'	o	'	o	"	
0	0	0	0	0	2	29	39	8	45	4	19	22	15 21 30
1	0	5	14	0	11	2	34	9	9	1	4	21	58 15 30 29
2	0	10	27	0	22	2	38	37	9	17	4	24	26 15 39 28
3	0	15	40	0	41	2	43	1	9	33	4	26	52 15 47 27
4	0	20	52	1	0	2	47	22	9	58	4	29	12 15 56 26
5	0	26	4	1	19	2	51	41	10	4	4	31	27 16 4 25
6	0	31	17	1	38	2	55	56	10	19	4	33	37 16 12 24
7	0	36	28	1	56	3	00	8	10	34	4	35	43 16 19 23
8	0	41	58	2	15	3	4	18	10	49	4	37	43 16 27 22
9	0	46	48	2	34	3	8	23	11	4	4	39	38 16 34 21
10	0	51	57	2	53	3	12	25	11	19	4	41	28 16 40 20
11	0	57	5	3	11	3	16	24	11	33	4	43	13 16 46 19
12	1	2	13	3	30	3	20	19	11	47	4	44	53 16 52 18
13	1	7	18	3	48	3	24	11	12	1	4	46	27 16 57 17
14	1	12	23	4	6	3	27	58	12	15	4	47	57 17 3 16
15	1	17	27	4	24	3	31	42	12	29	4	49	21 17 8 15
16	1	22	29	4	42	3	35	22	12	41	4	50	39 17 13 14
17	1	27	29	5	0	3	38	58	12	54	4	51	53 17 18 13
18	1	32	28	5	18	3	42	30	13	7	4	53	1 17 22 12
19	1	37	26	5	36	3	45	58	13	20	4	54	4 17 25 11
20	1	42	21	5	54	3	49	22	13	32	4	55	1 17 29 10
21	1	47	14	6	12	3	52	42	13	44	4	55	53 17 32 9
22	1	52	6	6	30	3	55	58	13	56	4	56	39 17 35 8
23	1	56	56	6	57	3	59	9	14	8	4	57	20 17 37 7
24	2	1	43	7	4	4	2	16	14	19	4	57	56 17 39 6
25	2	6	28	7	21	4	5	18	14	30	4	58	26 17 41 5
26	2	11	11	7	38	4	8	16	14	41	4	58	51 17 43 4
27	2	15	52	7	54	4	11	9	14	51	4	59	10 17 44 3
28	2	20	30	8	11	4	13	58	15	2	4	59	24 17 44 2
29	2	25	7	8	28	4	16	42	15	11	4	59	32 17 45 1
30	2	29	39	8	45	4	19	22	15	21	4	59	35 17 45 0
	5 N. Descen.		4 N. Descen.		3 N. Descen.		2 N. Descen.		1 N. Descen.		0 N. Descen.		
	11 S. Descen.		10 S. Descen.		9 S. Descen.		8 S. Descen.		7 S. Descen.		6 S. Descen.		

( 69 )

A Table of Reduction, with the Excess above the  
least Inclination  $4^{\circ} 59' 35''$ .

Arg. L.	Signs <sup>0</sup> <sub>6</sub>			Signs <sup>1</sup> <sub>7</sub>			Signs <sup>2</sup> <sub>8</sub>			Arg. L.
	Reduct.	sub.	Exc.	Reduct.	sub.	Exc.	Reduct.	sub.	Exc.	
0	0	0	0	5	40	42	5	40	42	30
1	0	14	2	5	47	43	5	33	41	29
2	0	27	4	5	53	44	5	25	40	28
3	0	41	6	5	59	45	5	17	39	27
4	0	55	8	6	4	46	5	10	38	26
5	1	8	9	6	8	46	5	1	37	25
6	1	22	11	6	13	46	4	52	36	24
7	1	35	12	6	17	47	4	42	35	23
8	1	48	13	6	20	47	4	33	34	22
9	2	1	15	6	23	47	4	23	33	21
10	2	14	17	6	26	47	4	13	31	20
11	2	27	19	6	28	47	4	2	30	19
12	2	40	20	6	30	48	3	51	29	18
13	2	52	22	6	31	48	3	40	28	17
14	3	4	23	6	32	48	3	29	26	16
15	3	16	24	6	32	48	3	17	24	15
16	3	28	26	6	32	48	3	5	23	14
17	3	40	28	6	31	48	2	53	22	13
18	3	51	29	6	30	48	2	40	20	12
19	4	2	30	6	29	47	2	28	19	11
20	4	12	31	6	26	47	2	15	17	10
21	4	23	33	6	23	47	2	2	15	9
22	4	33	34	6	20	47	1	49	13	8
23	4	44	35	6	17	47	1	35	12	7
24	4	52	36	6	12	46	1	22	11	6
25	5	1	37	6	8	46	1	8	9	5
26	5	9	38	6	3	46	0	55	8	4
27	5	18	39	5	58	45	0	41	6	3
28	5	26	40	5	52	44	0	27	4	2
29	5	33	41	5	46	43	0	14	2	1
30	5	40	42	5	40	42	0	0	0	0
	Signs <sup>5</sup> <sub>11</sub> Add.			Signs <sup>4</sup> <sub>10</sub> Add.			Signs <sup>3</sup> <sub>9</sub> Add.			

A Table of the Hourly Motions, Semi-diameters, and Horizontal Parallaxes of the Sun and Moon; the Sun's Horizontal Parallax being always 10".

Mean Anom. of ☽ & ☽.		Hourly Motion ☽.		Hourly Motion ☽.		Mean Anom. of ☽ & ☽.	
s.	o.	'	"	'	"	s.	o.
5	0	1	"	1	"	5	12
0	0	2	23	29	37	12	0
0	6	2	23	29	38	11	24
0	12	2	23	29	41	11	18
0	18	2	23	29	47	11	12
0	24	2	23	29	55	11	6
1	0	2	24	30	7	11	0
1	6	2	24	30	21	10	24
1	12	2	24	30	35	10	18
1	18	2	24	30	51	10	12
1	24	2	25	31	10	10	6
2	0	2	25	31	31	10	0
2	6	2	26	31	54	9	24
2	12	2	26	32	18	9	18
2	18	2	27	32	43	9	12
2	24	2	27	33	7	9	6
3	0	2	28	33	33	9	0
3	6	2	28	33	59	8	24
3	12	2	29	34	26	8	18
3	18	2	29	34	54	8	12
3	24	2	30	35	21	8	6
4	0	2	30	35	46	8	0
4	6	2	31	36	9	7	24
4	12	2	31	36	30	7	18
4	18	2	32	36	50	7	12
4	24	2	32	37	9	7	6
5	0	2	32	37	27	7	0
5	6	2	33	37	42	6	24
5	12	2	33	37	55	6	18
5	18	2	33	38	4	6	12
5	24	2	33	38	9	6	6
6	0	2	33	38	10	6	0

A Table of the Hourly Motions, Semidiameters,  
and Horizontal Parallaxes of the Sun and  
Moon ; the Sun's Horizontal Parallax being  
always  $10''$  : continued.

Mean Anom. of $\odot \& \varpi$ .	Apparen. Semidia.	Apparen. Semidia.	Horizont. Parallax.	Mean Anom. of $\odot \& \varpi$ .	
	$\odot$	$\varpi$	$\varpi$		
5.	0 1	0 0	1 1	5.	0
0	0 15	51	14 55	54 29	12 0
0	6 15	51	14 55	54 30	11 24
0	12 15	51	14 57	54 34	11 18
0	18 15	51	14 58	54 40	11 12
0	24 15	52	15 0	54 47	11 6
1	0 15	53	15 3	54 56	11 0
1	6 15	54	15 5	55 6	10 24
1	12 15	55	15 8	55 17	10 18
1	18 15	56	15 12	55 29	10 12
1	24 15	57	15 15	55 42	10 6
2	0 15	59	15 19	55 56	10 0
2	6 16	0	15 23	56 12	9 24
2	12 16	2	15 28	56 29	9 18
2	18 16	3	15 33	56 48	9 12
2	24 16	5	15 39	57 8	9 6
3	0 16	7	15 45	57 30	9 0
3	6 16	8	15 51	57 52	8 24
3	12 16	10	15 56	58 12	8 18
3	18 16	12	16 2	58 31	8 12
3	24 16	14	16 6	58 49	8 6
4	0 16	16	16 11	59 6	8 0
4	6 16	18	16 15	59 21	7 24
4	12 16	19	16 19	59 35	7 18
4	18 16	20	16 23	59 48	7 12
4	24 16	21	16 26	60 0	7 6
5	0 16	21	16 29	60 11	7 0
5	6 16	22	16 32	60 21	6 24
5	12 16	23	16 34	60 30	6 18
5	18 16	23	16 36	60 38	6 12
5	24 16	24	16 38	60 45	6 6
6	0 16	24	16 40	60 51	6 0

## 72 A Table of the Motion of the first Satellite of Jupiter.

Years Cur- rent-	Motion.	Years Com.	Motion.	Days.	Motion.
	s. o' d. "		s. o' d. "		s. o' d. "
1681	10 8 50 5	1	2 23 6 50	1	6 23 24 21
1701	3 18 8 28	2	5 16 13 49	2	1 16 48 42
1721	8 27 26 50	3	8 9 20 30	3	8 10 13 2
1722	11 20 33 40	4	5 25 51 40	4	3 3 37 23
1723	2 13 40 30	5	8 18 58 30	5	9 27 1 44
1724	5 6 47 20	6	11 12 5 20	6	4 20 26 5
1725	2 23 18 51	7	2 5 12 10	7	11 13 50 26
1726	5 16 25 21	8	11 21 43 21	8	6 7 14 47
1727	8 9 32 11	9	2 14 50 11	9	1 0 39 7
1728	11 2 39 1	10	5 7 57 1	10	7 24 3 28
1729	8 19 10 12	11	8 1 3 51	11	2 17 27 49
1730	11 2 17 2	12	5 17 35 1	12	9 10 52 10
1731	1 25 23 52	13	8 10 41 51	13	4 4 16 30
1732	4 18 30 41	14	11 3 48 41	14	10 27 40 52
1733	2 5 1 52	15	1 26 55 31	15	5 21 5 12
1734	4 28 8 42	16	11 13 26 42	16	0 14 29 33
1735	7 21 15 32	17	2 6 33 32	17	7 7 53 54
1736	10 14 22 22	18	4 29 40 22	18	2 1 18 15
1737	8 0 53 33	19	7 22 47 12	19	8 24 42 36
1738	10 24 0 23	20	5 9 18 23	20	3 18 6 57
1739	1 17 7 13	40	10 18 36 45	21	10 11 31 17
1740	4 10 14 3	60	3 27 55 8	22	5 4 55 38
1741	2 6 45 13	80	9 7 13 30	23	11 28 19 59
1742	11 23 16 24	100	2 16 31 53	24	6 21 44 20
1743	2 16 23 14	200	5 3 3 46	25	1 15 8 41
1744	5 9 30 4	300	7 19 35 39	26	8 8 33 2
1745	2 26 1 15	400	10 6 7 32	27	3 1 57 22
Jan.	0 0 0 0	500	0 22 39 25	28	9 25 21 43
Feb.	6 5 34 46	600	3 9 11 18	29	4 18 46 4
Mar.	4 0 56 30	700	5 25 43 12	30	11 12 10 25
Apr.	10 6 31 16	800	8 12 15 5	31	6 5 34 46
May	9 18 41 41	900	10 28 46 58		
June	3 24 16 27	1000	1 15 18 51		
July	3 6 26 52	2000	3 0 47 42		
Aug.	9 12 1 39	3000	4 15 56 33		
Sept.	3 17 36 25	4000	6 1 15 24		
Oct.	2 29 46 50	5000	7 16 34 15		
Nov.	9 5 21 36	6000	9 1 53 6		
Dec.	8 17 32 1	7000	10 17 11 57		

A Table of the Motion of the first Satellite of Jupiter. 73

H.	Motion.				1	o	y	n	1	o	1	n
	f.	o	1	n	III	II	III	III	III	II	III	III
1	0	8	28	31	1	0	8	29	31	4	22	45
2	0	16	57	2	2	0	16	57	32	4	31	13
3	0	25	25	33	3	0	25	26	33	4	39	41
4	1	3	54	3	4	0	33	54	34	4	48	10
5	1	12	22	34	5	0	42	23	35	4	56	38
6	1	20	51	5	6	0	50	51	36	5	5	7
7	1	29	19	36	7	0	59	20	37	5	13	35
8	2	7	48	7	8	1	7	48	38	5	22	4
9	2	16	16	38	9	1	16	17	39	5	30	32
10	2	24	45	9	10	1	24	45	40	5	39	1
11	3	3	13	40	11	1	33	14	41	5	47	29
12	3	11	42	10	12	1	41	42	42	5	55	58
13	3	20	10	41	13	1	50	11	43	6	4	26
14	3	28	39	12	14	1	58	39	44	6	12	55
15	4	7	7	43	15	2	7	8	45	6	21	23
16	4	15	36	14	16	2	15	36	46	6	29	52
17	4	24	4	45	17	2	24	5	47	6	38	20
18	5	2	33	16	18	2	32	33	48	6	46	49
19	5	11	1	46	19	2	41	2	49	6	55	17
20	5	19	30	17	20	2	49	30	50	7	3	46
21	5	27	58	48	21	2	57	59	51	7	12	14
22	6	6	27	19	22	3	6	27	52	7	20	43
23	6	14	55	50	23	3	14	56	53	7	29	11
24	6	23	24	21	24	3	23	24	54	7	37	40
					25	3	31	53	55	7	46	8
					26	3	40	21	56	7	54	37
					27	3	48	50	57	8	3	5
					28	3	57	18	58	8	11	34
					29	4	5	47	59	8	20	2
					30	4	14	15	60	8	28	31

In Leap-Year, after February, add the Motion of a Day more to the rest. The Radius of this Satellite I have taken December 31 at Noon 1683. Jupiter's Heliocentric Place was then 5 f. 13° 22' 57". And the Half-Say in the Shadow is 1<sup>h</sup> 6'. Mot. 9° 19' 22".

## 74 A Table of the Motion of the second Satellite of Jupiter.

Years Cur- rent	Motion.	Years Com.	Motion.	Days.	Motion.
	f. o' " "		f. o' " "		f. o' " "
1681	3 7 35 50	1	8 11 24 51	1	3 11 17 30
1701	7 22 20 10	2	4 22 49 41	2	6 22 34 59
1721	0 7 4 30	3	1 4 14 31	3	10 3 52 29
1722	8 18 29 20	4	0 26 56 51	4	1 15 9 58
1723	4 29 54 11	5	9 8 21 41	5	4 26 27 28
1724	1 11 19 2	6	5 19 46 32	6	18 7 44 57
1725	1 4 1 22	7	2 1 11 22	7	11 19 2 27
1726	9 15 26 12	8	1 23 53 43	8	3 0 19 56
1727	5 26 51 3	9	10 5 18 33	9	6 11 37 26
1728	2 8 15 54	10	6 16 43 23	10	9 22 54 56
1729	2 0 58 14	11	2 28 8 14	11	1 4 12 25
1730	10 12 23 4	12	2 20 50 34	12	4 15 29 55
1731	6 23 47 55	13	11 2 15 25	13	7 26 47 24
1732	3 5 12 46	14	7 13 40 46	14	11 8 4 54
1733	2 27 55 6	15	3 25 5 6	15	2 19 22 23
1734	11 9 19 56	16	3 17 47 27	16	6 0 39 53
1735	7 20 44 47	17	11 29 12 17	17	9 11 57 23
1736	4 2 9 37	18	8 10 37 8	18	0 23 14 52
1737	3 24 51 58	19	4 22 1 59	19	4 4 32 22
1738	0 6 16 48	20	4 14 44 20	20	7 15 49 51
1739	8 17 41 39	40	8 29 28 40	21	10 27 7 21
1740	4 29 6 29	60	1 14 13 0	22	2 8 24 50
1741	4 21 48 50	80	5 28 57 20	23	5 19 42 20
1742	1 3 13 40	100	10 13 41 39	24	9 0 59 53
1743	9 14 38 31	200	8 27 23 19	25	0 12 17 19
1744	5 26 3 21	300	7 11 4 58	26	3 23 34 49
1745	5 18 45 42	400	5 24 46 38	27	7 4 52 18
Jan.	0 0 0 0	500	4 8 28 17	28	10 16 9 48
Feb.	8 20 2 16	600	2 22 9 56	29	1 27 27 17
Mar.	7 6 12 4	700	1 5 31 36	30	5 8 44 47
Apr.	3 26 14 20	800	11 19 33 15	31	8 20 2 16
May	9 4 29 7	900	10 3 14 45		
June	5 25 1 23	1000	8 16 56 24		
July	11 3 46 10	2000	5 3 52 48		
Aug.	7 23 48 26	3000	1 20 49 12		
Sept.	4 13 50 42	4000	10 7 45 36		
Oct.	9 22 35 29	5000	6 24 42 0		
Nov.	6 12 37 45	6000	3 11 38 24		
Dec.	11 21 22 34	7000	11 28 34 48		

A Table of the Motion of the second Satellite of Jupiter. 75

H.	Motion.				I.	o	I	"	I.	o	I	"
	s.	o	I	"	II							
1	0	4	13	14	1	0	4	13	31	2	10	50
2	0	8	26	27	2	0	8	26	32	2	15	3
3	0	12	39	41	3	0	12	40	33	2	19	17
4	0	16	52	55	4	0	16	53	34	2	23	30
5	0	21	6	9	5	0	21	6	35	2	27	43
6	0	25	19	22	6	0	25	19	36	2	31	56
7	0	29	32	36	7	0	29	33	37	2	36	10
8	1	3	45	50	8	0	33	46	38	2	40	23
9	1	7	59	3	9	0	37	59	39	2	44	36
10	1	12	12	17	10	0	42	12	40	2	48	49
11	1	16	25	31	11	0	46	26	41	2	53	3
12	1	20	38	45	12	0	50	39	42	2	57	16
13	1	24	51	58	13	0	54	52	43	3	1	29
14	1	29	5	12	14	0	59	5	44	3	5	42
15	2	3	18	26	15	1	3	18	45	3	9	55
16	2	7	31	39	16	1	7	32	46	3	14	9
17	2	11	44	53	17	1	11	45	47	3	18	22
18	2	15	58	7	18	1	15	58	48	3	22	35
19	2	20	11	21	19	1	20	11	49	3	26	48
20	2	24	24	34	20	1	24	25	50	3	31	2
21	2	28	37	48	21	1	28	38	51	3	35	15
22	3	2	51	2	22	1	32	51	52	3	39	28
23	3	7	4	15	23	1	37	4	53	3	43	41
24	3	11	17	30	24	1	41	18	54	3	47	55
					25	1	45	31	55	3	52	8
					26	1	49	44	56	3	56	21
					27	1	53	57	57	4	0	34
					28	1	58	11	58	4	4	48
					29	2	2	24	59	4	9	1
					30	2	6	37	60	4	13	14

In Leap-Year, after February, add the Motion of a Day more to the rest. And the Radix of this Satellite I have taken December 31 at Noon, 1683. Jupiter's Heliocentric Place was then  $5^{\circ} 13' 22'' 57''$ . Its Half-Stay in the Shadow is  $1^{\text{h}} 25'$  Mot.  $5^{\circ} 58' 4''$ .

## 76 A Table of the Motion of the third Satellite of Jupiter

Years Cur- rent.	Motion.	Years Com.	Motion.	D. S.	Motion.
	s. o i "		s. o i "		s. o i "
1681	2 22 15 57	1 11 5 35 40	1	1 20 14 4	
1701	6 25 19 36	2 10 11 11 19	2	3 10 28 8	
1721	10 28 23 14	3 9 16 46 59	3	5 0 42 13	
1722	10 3 58 53	4 10 12 36 44	4	6 20 56 17	
1723	9 9 34 33	5 9 18 12 23	5	8 11 10 21	
1724	8 15 10 13	6 8 23 48 3	6	10 1 24 25	
1725	9 10 59 57	7 7 29 23 42	7	11 21 38 30	
1726	8 16 35 37	8 8 25 13 27	8	1 11 52 34	
1727	7 22 11 17	9 8 0 49 7	9	3 2 6 38	
1728	6 27 46 57	10 7 6 24 46	10	4 22 20 42	
1729	7 23 36 41	11 6 12 0 26	11	6 12 34 46	
1730	6 29 12 21	12 7 7 50 11	12	8 2 48 51	
1731	6 4 48 1	13 6 13 25 50	13	9 23 2 55	
1732	5 10 23 40	14 5 19 1 30	14	11 13 16 59	
1733	6 6 13 24	15 4 24 37 9	15	1 3 31 3	
1734	5 11 49 4	16 5 20 26 54	16	2 23 45 7	
1735	4 17 24 44	17 4 26 2 34	17	4 13 59 12	
1736	3 23 0 24	18 4 1 38 14	18	6 4 13 16	
1737	4 18 50 8	19 3 7 13 53	19	7 24 27 20	
1738	3 24 25 48	20 4 3 3 38	20	9 14 41 24	
1739	3 0 1 28	40 8 6 7 16	21	1 4 55 29	
1740	2 5 37 8	60 0 9 10 54	22	0 25 9 33	
1741	3 1 26 52	80 4 12 14 32	23	2 15 23 37	
1742	2 7 2 32	100 8 15 18 10	24	4 5 37 41	
1743	1 12 38 11	200 5 0 36 21	25	5 25 51 45	
1744	0 18 13 51	300 1 15 54 31	26	7 16 5 50	
1745	1 4 3 35	400 10 1 12 42	27	9 6 19 54	
Jan.	0 0 0 0	500 6 16 30 52	28	10 26 33 58	
Feb.	3 27 16 11	600 3 1 49 3	29	0 16 48 2	
Mar.	2 23 50 9	700 11 17 7 13	30	2 7 2 7	
Apr.	6 21 6 20	800 8 2 25 24	31	3 27 16 11	
May.	8 28 8 26	900 4 17 43 34			
June	0 25 24 37	1000 1 3 1 45			
July	3 2 26 43	2000 2 6 3 30			
Aug.	6 29 42 54	3000 3 9 5 15			
Sept.	10 26 59 5	4000 4 12 7 0			
Okt.	1 4 1 12	5000 5 15 8 45			
Nov.	5 1 17 22	6000 6 18 10 30			
Dec.	7 8 19 29	7000 7 21 12 15			

A Table of the Motion of the third Satellite of Jupiter. 77

H.	Motion.				I.	O.	I.	II.	I.	O.	I.	II.
	f.	Q.	I.	P.								
1	0	2	5	35	4	0	2	6	31	1	4	53
2	0	4	11	10	2	0	4	11	32	1	6	59
3	0	6	16	45	3	0	6	17	33	1	9	4
4	0	8	22	21	4	0	8	22	34	1	11	10
5	0	10	27	56	5	0	10	28	35	1	13	15
6	0	12	33	31	6	0	12	33	36	1	15	21
7	0	14	39	6	7	0	14	39	37	1	17	27
8	0	16	44	41	8	0	16	45	38	1	19	32
9	0	18	50	16	9	0	18	50	39	1	21	38
10	0	20	55	52	10	0	20	56	40	1	23	43
11	0	23	1	27	11	0	23	1	41	1	25	49
12	0	23	7	2	12	0	25	7	42	1	27	54
13	0	27	12	37	13	0	27	13	43	1	30	0
14	0	29	18	12	14	0	29	18	44	1	32	6
15	1	1	23	47	15	0	31	24	45	1	34	11
16	1	3	29	23	16	0	33	29	46	1	36	17
17	1	5	34	58	17	0	35	35	47	1	38	22
18	1	7	40	33	18	0	37	40	48	1	40	28
19	1	9	46	8	19	0	39	46	49	1	42	33
20	1	11	51	43	20	0	41	52	50	1	44	39
21	1	13	57	18	21	0	43	57	51	1	46	46
22	1	16	2	54	22	0	46	3	52	1	48	50
23	1	18	8	29	23	0	48	8	53	1	50	57
24	1	20	14	4	24	0	50	14	54	1	53	1
					25	0	52	20	55	1	55	7
					26	0	54	25	56	1	57	14
					27	0	56	31	57	1	59	18
					28	0	58	36	58	2	1	25
					29	1	0	42	59	2	3	29
					30	1	2	47	60	2	5	35

In Leap-Year, after February, add the Motion of a Day more to the rest. And the Radix of this Satellite I have taken December 31 at Noon, 1683. Jupiter's Heliocentric Place was then 5° 13' 22" 57". Half-Stay in the Shadow 1° 18' Mot. 2° 43' 15".

## 78 A Table of the Motion of the fourth Satellite of Jupiter.

Years Cur- rent	Motion.	Years Com.	Motion.	Days.	Motion.
	s. ° / "		s. ° / "		s. ° / "
1681	8 12 56 51	1	9 13 5 7	1	0 21 29 16
1701	8 22 5 31	2	6 26 10 14	2	1 12 58 33
1721	9 1 14 10	3	4 9 15 21	3	2 4 27 49
1722	6 14 19 17	4	2 13 49 44	4	2 25 57 6
1723	3 27 24 24	5	1 26 54 51	5	3 17 26 22
1724	1 10 29 31	6	9 9 59 58	6	4 8 55 39
1725	11 15 3 54	7	6 23 5 4	7	5 0 24 55
1726	8 28 9 1	8	4 27 39 28	8	5 21 54 12
1727	6 11 14 8	9	2 10 44 35	9	6 13 23 28
1728	3 24 19 14	10	11 23 49 41	10	7 4 52 45
1729	1 28 53 38	11	9 6 54 48	11	7 26 22 1
1730	11 11 58 45	12	7 11 29 12	12	8 17 51 18
1731	8 25 3 51	13	4 24 34 18	13	9 9 20 34
1732	6 8 8 58	14	2 7 39 25	14	10 0 49 51
1733	4 12 43 32	15	11 20 44 32	15	10 22 19 7
1734	1 25 48 28	16	9 25 18 15	16	11 13 48 23
1735	11 8 53 35	17	7 8 24 2	17	0 5 17 40
1736	8 21 58 42	18	4 21 29 9	18	0 26 46 56
1737	6 26 33 5	19	2 4 34 16	19	1 18 16 13
1738	4 9 38 12	20	0 9 8 39	20	2 9 45 29
1739	1 22 43 19	40	0 18 17 19	21	3 1 14 46
1740	11 5 48 26	60	0 27 25 58	22	3 22 44 2
1741	9 10 22 50	80	1 6 34 38	23	4 14 13 19
1742	6 23 27 56	100	1 15 43 17	24	5 5 42 35
1743	4 6 23 3	200	3 1 26 35	25	5 27 11 52
1744	1 19 38 10	300	4 17 9 52	26	6 18 41 8
1745	11 24 12 34	400	6 2 53 9	27	7 10 10 25
Jan.	0 0 0 0	500	7 18 36 27	28	8 1 39 41
Feb.	10 6 7 30	600	9 4 19 44	29	8 23 8 58
Mar.	6 7 47 11	700	10 20 3 1	30	9 14 38 14
Apr.	4 13 54 41	800	0 5 46 19	31	10 6 7 30
May	1 28 32 55	900	1 21 29 36		
June	0 4 40 26	1000	3 7 12 53		
July	9 19 18 40	2000	6 14 25 46		
Aug.	7 25 26 10	3000	9 21 38 39		
Sept.	6 1 33 40	4000	0 28 51 32		
Oct.	3 16 11 54	5000	4 6 4 25		
Nov.	1 22 19 24	6000	7 13 17 18		
Dec.	11 26 57 38	7000	10 20 30 11		

A Table of the Motion of the fourth Satellite of Jupiter. 79

H	°	'	"	H	°	'	"
/	I	II	III	/	I	II	III
II	II	III	III	II	II	III	III
1	0	53	43	31	25	45	19
2	1	47	26	32	28	39	2
3	2	41	10	33	29	32	45
4	3	34	53	34	30	26	28
5	4	28	36	35	31	20	11
6	5	22	19	36	32	13	55
7	6	16	2	37	33	7	38
8	7	9	43	38	34	1	21
9	8	3	29	39	34	55	4
10	8	57	12	40	35	48	47
11	9	50	55	41	36	42	31
12	10	44	38	42	37	36	14
13	11	38	21	43	38	29	57
14	12	32	5	44	39	23	40
15	13	25	48	45	40	17	23
16	14	19	31	46	41	11	6
17	15	13	14	47	42	4	50
18	16	6	57	48	42	58	33
19	17	0	40	49	43	52	16
20	17	54	24	50	44	45	59
21	18	48	7	51	45	39	42
22	19	41	50	52	46	33	26
23	20	35	33	53	47	27	9
24	21	29	16	54	48	20	52
25	22	23	0	55	49	14	35
26	23	16	43	56	50	8	18
27	24	10	26	57	51	2	1
28	25	4	9	58	51	55	45
29	25	57	32	59	52	49	28
30	26	51	35	60	53	43	11

In Leap-Year, after February, add the Motion of a Day more to the rest. And the Radix of this Satellite I have taken December 31 at Noon, 1683. Jupiter's Heliocentric Place was then  $5^{\circ} 13' 22'' 57'''$ . Half Stay in the Shadow  $1^{\text{h}} 35'$ . Mot.  $1^{\text{h}} 25' 3''$ .

A Table of the Distances of the Satellites of Jupiter from his Body, in Semidiameters and Decimal Parts of Jupiter's Globe.

Satellite 1.

o	0 Conseq. 6 Antec.	1 Conseq. 7 Antec.	2 Conseq. 8 Antec.	o
0	0.	1.8592	3.7183	30
3	0.1859	2.0451	3.9042	27
6	0.3718	2.2310	4.0901	24
9	0.5577	2.4169	4.2760	21
12	0.7436	2.6028	4.4619	18
15	0.9300	2.7887	4.6478	15
18	1.1155	2.9746	4.8337	12
21	1.3014	3.1606	5.0196	9
24	1.4873	3.3465	5.2056	6
27	1.6732	3.5324	5.3915	3
30	1.8592	3.7183	5.5780	0

Satellite 2.

0	0.	2.9590	5.9180	30
3	0.2959	3.2549	6.2139	27
6	0.5918	3.5508	6.5098	24
9	0.8877	3.8467	6.8057	21
12	1.1836	4.1426	7.1016	18
15	1.4795	4.4385	7.3975	15
18	1.7754	4.7344	7.6934	12
21	2.0713	5.0303	7.9893	9
24	2.3672	5.3262	8.2852	6
27	2.6613	5.6221	8.5813	3
30	2.9590	5.0180	8.8760	0
	5 Conseq. 11 Antec.	4 Conseq. 10 Antec.	3 Conseq. 9 Antec.	

A Table of the Distances of the Satellites of Jupiter from his Body, in Semidiameters and Decimal Parts of Jupiter's Globe.

Satellite 3.

0	o Conseq. 6 Antec.	1 Conseq. 7 Antec.	2 Conseq. 8 Antec.	0
0	0.	4.72	9.44	30
3	0.472	5.192	9.912	27
6	0.944	5.664	10.384	24
9	1.416	6.136	10.856	21
12	1.888	6.608	11.328	18
15	2.36	7.08	11.8	15
18	2.832	7.552	12.272	12
21	3.304	8.024	12.744	9
24	3.776	8.496	13.216	6
27	4.248	8.968	13.688	3
30	4.72	9.44	14.159	0

Satellite 4.

0	0.	8.301	16.602	30
3	0.8301	9.1311	17.4321	27
6	1.6602	9.9612	18.2622	24
9	2.4903	10.7913	19.0923	21
12	3.3204	11.6214	19.9224	18
15	4.1505	12.4515	20.7525	15
18	4.9806	13.2816	21.5826	12
21	5.8107	14.1117	22.4127	9
24	6.6408	14.9418	23.2428	6
27	7.4709	15.7719	24.0729	3
30	8.301	16.602	24.903	0
	5 Conseq. 11 Antec.	4 Conseq. 10 Antec.	3 Conseq. 9 Antec.	

82 A Table of the Motion of the first Satellite of Saturn.

Years Cur- rent-	Motion.	Years Com.	Motion.	Days.	Motion.
	s. o' f. "		s. o' f. "		s. o' f. "
1681	9 28 34 39	1	4 4 35 1	1	6 10 41 51
1701	4 23 43 6	2	8 9 10 1	2	0 21 23 42
1721	11 18 52 33	3	0 13 45 2	3	7 2 5 33
1722	3 23 27 34	4	10 29 1 53	4	1 12 47 24
1723	7 28 2 34	5	3 3 36 54	5	7 23 29 15
1724	0 2 37 35	6	7 8 11 55	6	2 4 11 6
1725	10 17 54 27	7	11 12 46 55	7	8 14 52 57
1726	2 22 29 27	8	9 28 3 47	8	2 25 34 48
1727	6 27 4 28	9	2 2 38 47	9	9 6 16 39
1728	11 1 39 28	10	6 7 13 48	10	3 16 58 29
1729	9 16 56 20	11	10 11 48 49	11	9 27 40 20
1730	1 21 31 21	12	8 27 5 40	12	4 8 22 11
1731	5 26 6 21	13	1 1 40 41	13	10 19 4 2
1732	10 0 41 22	14	5 6 15 41	14	4 29 45 53
1733	8 15 58 13	15	9 10 50 42	15	11 10 27 44
1734	0 20 33 14	16	7 26 7 34	16	5 21 9 35
1735	4 25 8 15	17	0 0 42 34	17	0 1 51 26
1736	8 29 43 15	18	4 5 17 35	18	6 12 33 17
1737	7 15 0 7	19	8 9 52 35	19	0 23 15 8
1738	11 19 35 7	20	6 25 9 27	20	7 3 56 59
1739	3 24 10 8	40	1 20 18 55	21	1 14 38 50
1740	7 28 45 9	60	8 15 28 22	22	7 25 20 41
1741	6 14 2 0	80	3 10 37 50	23	2 6 2 32
1742	10 18 37 1	100	10 5 47 17	24	8 16 44 23
1743	2 23 12 1	200	8 11 34 34	25	2 27 16 14
1744	6 27 47 2	300	6 17 21 51	26	9 8 8 5
1745	5 13 3 53	400	4 23 9 8	27	3 18 49 56
Jan.	0 0 0 0	500	2 28 56 25	28	9 29 31 47
Feb.	5 1 37 19	600	1 4 43 42	29	4 10 13 38
Mar.	3 1 9 6	700	11 10 30 59	30	10 20 55 28
Apr.	8 2 46 26	800	9 16 18 16	31	5 1 37 19
May	6 23 41 55	900	7 22 5 33		
June	11 25 19 14	1000	3 27 52 50		
July	10 16 14 53	2000	11 25 45 40		
Aug.	3 17 52 13	3000	5 23 38 30		
Sept.	8 19 29 32	4000	11 21 31 20		
Oct.	7 10 24 51	5000	5 19 24 10		
Nov.	0 12 2 11	6000	11 17 17 0		
Dec.	11 2 57 29	7000	5 15 9 50		

A Table of the Motion of the first Satellite of *Saturn*. 83

H.	Motion.	J				o				v				n				r				o				l				"			
		f.	o	l	"	/	III	"	III	/	III	"	III	/	III	"	III	/	III	"	III	/	III	"	III	/	III	"	III	/	III	"	
1	o 7 56 48	1	o 7 57	57	31	4	6	19																									
2	o 15 53 29	2	o 15 53	53	32	4	14	15																									
3	o 23 50 14	3	o 23 50	50	33	4	22	12																									
4	1 1 46 58	4	o 31 47	47	34	4	30	9																									
5	1 9 43 43	5	o 39 44	44	35	4	38	6																									
6	1 17 40 28	6	o 47 40	40	36	4	46	2																									
7	1 25 37 12	7	o 55 37	37	37	4	53	59																									
8	2 3 33 57	8	1 3 34	34	38	5	1	56																									
9	2 11 30 42	9	1 11 31	31	39	5	9	53																									
10	2 19 27 26	10	1 19 27	27	40	5	17	49																									
11	2 27 24 11	11	1 27 24	24	41	5	25	46																									
12	3 5 20 55	12	1 35 21	21	42	5	33	43																									
13	3 13 17 40	13	1 43 18	18	43	5	41	40																									
14	3 21 14 25	14	1 51 14	14	44	5	49	36																									
15	3 29 11 9	15	1 59 11	11	45	5	57	33																									
16	4 7 7 54	16	2 7 8	8	46	6	5	30																									
17	4 15 4 38	17	2 15 4	4	47	6	13	26																									
18	4 23 1 23	18	2 23 1	48	6	21	23																										
19	5 0 58 8	19	2 30 58	58	49	6	29	20																									
20	5 8 54 52	20	2 38 55	55	50	6	37	17																									
21	5 16 51 37	21	2 46 51	51	51	6	43	13																									
22	5 24 48 22	22	2 54 48	48	52	6	53	10																									
23	6 2 45 7	23	3 2 45	45	53	7	1	7																									
24	6 10 41 51	24	3 10 42	42	54	7	9	4																									
		25	3 18 38	38	55	7	17	0																									
		26	3 26 35	35	56	7	24	57																									
		27	3 34 32	32	57	7	32	54																									
		28	3 42 29	29	58	7	40	51																									
		29	3 50 25	25	59	7	48	57																									
		30	3 58 22	22	60	7	56	45																									

In Leap-Year, after February, add the Motion of a Day more to the rest.

Its Nodes are in  $\text{M}\text{C}$   $21^\circ$ . Inclination  $31^\circ$ .

The Epoche of this Satellite I have taken, Anno 1713, December 31 at Noon,  $\frac{1}{2}$  Geocentric Place was then  $5^{\circ} f.$   
 $11^\circ 6' 9''$ .

## 84 A Table of the Motion of the second Satellite of Saturn.

Years Cur- rent.	Motion.	Years Com.	Motion.	Days.	Motion.
	s. ° / "		s. ° / "		s. ° / "
1681	II 5 28 41	1	4 10 2 52	1	4 11 32 4
1701	II 24 6 19	2	8 20 5 44	2	8 23 4 7
1721	0 12 43 57	3	1 0 8 36	3	1 4 36 11
1722	4 22 46 49	4	9 21 43 32	4	5 16 8 15
1723	9 2 49 41	5	2 1 46 23	5	9 27 40 19
1724	I 12 52 33	6	6 11 49 15	6	2 9 12 22
1725	10 4 27 29	7	10 21 52 7	7	6 20 44 26
1726	2 14 30 21	8	7 13 27 3	8	11 2 16 30
1727	6 24 33 13	9	11 23 29 55	9	3 13 48 34
1728	II 4 36 5	10	4 3 32 47	10	7 25 20 37
1729	7 26 11 0	11	8 13 39 39	11	0 6 52 41
1730	0 6 13 52	12	5 5 10 35	12	4 18 24 45
1731	4 16 16 44	13	9 15 13 27	13	8 29 56 49
1732	8 26 19 36	14	1 25 16 19	14	1 11 28 52
1733	5 17 54 32	15	6 5 19 10	15	5 23 0 56
1734	9 27 57 24	16	2 26 54 6	16	10 4 33 0
1735	2 8 0 16	17	7 6 56 58	17	2 16 5 4
1736	6 18 3 8	18	11 16 59 50	18	6 27 37 7
1737	3 9 38 3	19	3 27 2 42	19	11 9 9 11
1738	7 19 40 55	20	0 18 37 38	20	3 20 41 15
1739	II 29 43 47	40	1 7 15 16	21	8 2 13 19
1740	4 9 46 39	60	1 25 52 54	22	0 13 45 22
1741	I 1 21 35	80	2 14 30 31	23	4 25 17 26
1742	5 11 24 27	100	3 3 8 9	24	9 6 49 30
1743	9 21 27 18	200	6 6 16 19	25	1 18 21 34
1744	2 1 30 10	300	9 9 24 28	26	5 29 53 37
1745	10 23 5 7	400	0 12 32 37	27	10 11 25 41
Jan.	0 0 0 0	500	3 15 40 47	28	2 22 51 45
Feb.	3 27 33 57	600	6 18 48 56	29	7 4 29 49
Mar.	6 20 31 42	700	9 21 57 5	30	11 16 1 52
Apr.	10 18 5 39	800	0 25 5 15	31	3 27 33 57
May.	10 4 7 31	900	3 28 13 24		
June	2 1 41 28	1000	7 1 21 33		
July	1 17 43 20	2000	2 2 43 6		
Aug.	5 15 17 17	3000	9 4 4 39		
Sept.	9 12 51 14	4000	4 5 26 12		
Okt.	8 28 53 6	5000	11 6 47 45		
Nov.	0 26 27 3	6000	6 8 9 18		
Dec.	0 12 28 55	7000	1 9 30 51		

A Table of the Motion of the second Satellite of *Saturn*. 85

H.	Motion.				I	o	I	II	I	o	I	II
	f.	Q	I	B	III	II	III	II	III	II	III	II
1	0	5	28	50	1	0	5	29	31	2	49	55
2	0	10	57	40	2	0	10	58	32	2	55	24
3	0	16	26	30	3	0	16	26	33	3	0	52
4	0	21	55	21	4	0	21	55	34	3	6	20
5	0	27	24	11	5	0	27	24	35	3	11	49
6	1	2	53	1	6	0	32	53	36	3	17	18
7	1	8	21	51	7	0	38	22	37	3	22	47
8	1	13	50	41	8	0	43	51	38	3	28	16
9	1	19	19	31	9	0	49	19	39	3	33	44
10	1	24	48	21	10	0	54	48	40	3	39	14
11	2	0	17	12	11	1	0	17	41	3	44	43
12	2	5	46	2	12	1	5	46	42	3	50	12
13	2	11	14	52	13	1	11	15	43	3	55	41
14	2	16	43	42	14	1	16	44	44	4	1	9
15	2	22	12	32	15	1	22	12	45	4	6	36
16	2	27	41	22	16	1	27	41	46	4	12	5
17	3	3	10	13	17	1	33	10	47	4	17	34
18	3	8	39	3	18	1	38	39	48	4	23	3
19	3	14	7	53	19	1	44	8	49	4	28	32
20	3	19	36	43	20	1	49	38	50	4	34	1
21	3	25	5	33	21	1	55	7	51	4	39	29
22	4	0	34	23	22	2	0	35	52	4	44	58
23	4	6	3	13	23	2	6	4	53	4	50	27
24	4	11	32	4	24	2	11	33	54	4	55	56
					25	2	17	2	55	5	1	25
					26	2	22	31	56	5	6	54
					27	2	28	0	57	5	12	22
					28	2	33	28	58	5	17	51
					29	2	38	57	59	5	23	20
					30	2	44	26	60	5	28	50

In Leap-Year, after February, add the Motion of a Day more to the rest.

Its Nodes are in  $\text{MR} \times 21^\circ$ . Inclination  $31^\circ$ .

The Epoche of this Satellite I have taken, Anno 1713, December 31 at Noon, h Geocentric Place was then  $55^\circ 11' 6''$ .

## 86 A Table of the Motion of the third Satellite of Saturn.

Years Cur- rent	Motion.	Years Com.	Motion.	Days.	Motion.
	s. ° / "		s. ° / "		s. ° / "
1681	5 4 23 10	1	9 17 2 0	1	2 19 41 26
1701	5 23 30 23	2	7 4 4 0	2	5 9 22 52
1721	6 12 37 36	3	4 21 6 0	3	7 29 4 17
1722	3 29 39 36	4	4 27 49 26	4	10 18 45 43
1723	1 16 41 36	5	2 14 51 27	5	1 8 27 9
1724	11 3 43 36	6	0 1 53 27	6	3 28 8 35
1725	11 10 27 2	7	9 18 55 27	7	6 17 50 1
1726	8 27 29 2	8	9 25 38 53	8	9 7 31 26
1727	6 14 32 3	9	7 12 40 53	9	11 27 12 52
1728	4 1 33 3	10	4 29 42 53	10	2 16 54 18
1729	4 8 16 29	11	2 16 44 53	11	5 6 35 44
1730	1 25 18 29	12	2 23 28 19	12	7 26 17 10
1731	11 12 20 29	13	0 10 30 20	13	10 15 58 35
1732	8 29 22 29	14	9 27 32 20	14	1 5 40 1
1733	9 6 5 55	15	7 14 34 20	15	3 25 21 27
1734	6 23 7 55	16	7 21 17 46	16	6 15 2 53
1735	4 10 9 55	17	5 8 19 46	17	9 4 44 19
1736	1 27 11 56	18	2 25 21 46	18	11 24 25 44
1737	2 3 55 22	19	0 12 23 46	19	2 14 7 10
1738	11 20 57 22	20	0 19 7 13	20	5 3 48 36
1739	9 7 59 22	40	1 8 14 25	21	7 23 30 2
1740	6 25 1 22	60	1 27 21 38	22	10 13 11 28
1741	7 1 44 48	80	2 16 28 51	23	1 2 52 53
1742	4 18 46 48	100	3 5 36 3	24	3 22 34 19
1743	2 5 48 48	200	6 11 12 7	25	6 12 15 45
1744	11 22 50 49	300	9 16 48 10	26	9 1 57 11
1745	11 29 34 15	400	0 22 24 13	27	11 21 38 37
Jan.	0 0 0 0	500	3 28 0 17	28	2 11 20 2
Feb.	10 10 24 20	600	7 3 36 20	29	5 1 1 28
Mar.	0 21 44 22	700	10 9 12 23	30	7 20 42 54
Apr.	11 2 8 43	800	1 14 48 27	31	10 10 24 20
May	6 22 51 37	900	4 20 24 30		
June	5 3 15 57	1000	7 26 0 23		
July	0 23 58 51	2000	3 22 1 6		
Aug.	11 4 23 11	3000	7 14 2 12		
Sept.	9 14 47 31	4000	3 10 2 45		
Okt.	5 5 30 25	5000	11 6 3 18		
Nov.	3 15 54 45	6000	7 2 3 51		
Dec.	11 6 37 39	7000	2 28 4 24		

A Table of the Motion of the third Satellite of *Saturn*. 87

H.	Motion.				/	o	/	"	/	o	/	"
	f.	o	t	"	/	o	/	"	/	o	/	"
1	0	3	19	14	1	0	3	19	31	1	42	56
2	0	6	38	27	2	0	6	38	32	1	46	15
3	0	9	57	41	3	0	9	58	33	1	49	34
4	0	13	16	54	4	0	13	17	34	1	52	53
5	0	16	36	8	5	0	16	36	35	1	56	13
6	0	19	55	21	6	0	19	55	36	1	59	32
7	0	23	14	35	7	0	23	15	37	2	2	51
8	0	26	33	49	8	0	26	34	38	2	6	10
9	0	29	53	2	9	0	29	53	39	2	9	29
10	1	3	12	16	10	0	33	12	40	2	12	49
11	1	6	31	29	11	0	36	31	41	2	16	8
12	1	9	50	43	12	0	39	51	42	2	19	27
13	1	13	9	56	13	0	43	10	43	2	22	46
14	1	16	29	10	14	0	46	29	44	2	26	6
15	1	19	48	23	15	0	49	48	45	2	29	25
16	1	23	7	37	16	0	53	7	46	2	32	44
17	1	26	26	51	17	0	56	27	47	2	36	3
18	1	29	46	4	18	0	59	46	48	2	39	22
19	2	3	5	18	19	1	3	5	49	2	42	42
20	2	6	24	31	20	1	6	24	50	2	46	1
21	2	9	43	45	21	1	9	44	51	2	49	20
22	2	13	2	58	22	1	13	3	52	2	52	39
23	2	16	22	12	23	1	16	22	53	2	55	58
24	2	19	41	26	24	1	19	41	54	2	59	18
					25	1	23	0	55	3	2	37
					26	1	26	20	56	3	5	56
					27	1	29	39	57	3	9	15
					28	1	32	58	58	3	12	35
					29	1	36	17	59	3	15	54
					30	1	39	36	60	3	19	14

In Leap-Year, after February, add the Motion of a Day more to the rest.

Its Nodes are in  $\pi \times 21^\circ$ . Inclination 31.

The Epoche of this Satellite I have taken, Anno 1713, December 31 at Noon,  $\frac{1}{2}$  Geocentric Place was then 55.  
 $11^\circ 6' 9''$ .

## 88 A Table of the Motion of the fourth Satellite of Saturn.

Years Cur- rent.	Motion.	Years Com.	Motion.	Days.	Motion.
	s. o' / "		s. o' / "		s. o' / "
1681	1 0 48 56	1	10 20 35 19	1	0 22 34 37
1701	2 15 28 19	2	9 11 10 37	2	1 15 9 14
1721	4 0 7 42	3	8 1 45 56	3	2 7 43 51
1722	2 20 43 1	4	7 14 55 52	4	3 0 18 28
1723	1 11 18 20	5	6 5 31 11	5	3 22 53 5
1724	0 1 53 39	6	4 26 6 30	6	4 15 27 42
1725	11 15 3 35	7	3 16 41 49	7	5 8 2 19
1726	10 5 38 54	8	2 29 51 45	8	6 0 36 56
1727	8 26 14 13	9	1 20 27 4	9	6 23 11 33
1728	7 16 49 31	10	0 11 2 23	10	7 15 46 10
1729	6 29 59 27	11	1 1 37 42	11	8 8 20 47
1730	5 20 34 46	12	10 14 47 38	12	9 0 55 24
1731	4 11 10 5	13	9 5 22 57	13	9 23 30 1
1732	3 1 45 24	14	7 25 58 15	14	10 16 4 38
1733	2 14 55 20	15	6 16 33 34	15	11 8 39 15
1734	1 5 30 39	16	5 29 43 30	16	0 1 13 52
1735	11 26 5 58	17	4 20 18 49	17	0 23 48 29
1736	10 16 41 17	18	3 10 54 8	18	1 16 23 6
1737	10 29 51 13	19	2 1 29 27	19	2 8 57 43
1738	9 20 26 31	20	1 14 39 23	20	3 1 32 20
1739	8 11 1 50	40	2 29 18 46	21	3 24 6 57
1740	7 1 37 9	60	4 13 58 9	22	4 16 41 34
1741	5 14 47 5	80	5 28 37 32	23	5 9 16 11
1742	4 5 22 24	100	7 13 16 55	24	6 1 50 48
1743	2 25 57 43	200	2 26 33 50	25	6 24 25 25
1744	1 16 33 2	300	10 9 50 44	26	7 17 0 2
1745	0 29 42 58	400	5 23 7 39	27	8 9 34 39
Jan.	0 0 0 0	500	1 6 24 34	28	9 2 9 16
Feb.	11 9 53 8	600	8 19 44 29	29	9 24 43 53
Mar.	8 12 2 26	700	4 2 58 24	30	10 17 18 32
Apr.	7 21 55 34	800	11 16 15 19	31	11 9 53 8
May	6 9 14 6	900	6 29 32 13		
June	5 19 7 14	1000	2 12 49 8		
July	4 6 25 40	2000	4 25 38 16		
Aug.	3 16 18 54	3000	1 8 27 24		
Sept.	2 26 12 24	4000	9 21 16 32		
Okt.	1 13 30 34	5000	0 4 5 40		
Nov.	0 23 23 42	6000	2 16 54 48		
Dec.	11 10 42 14	7000	4 29 43 56		

A Table of the Motion of the fourth Satellite of Saturn. 39

H.	o	/	"	H.	o	/	"
	/	"	III		/	"	III
1	9	56	27	31	29	9	43
2	1	52	53	32	30	6	9
3	2	49	20	33	31	2	36
4	3	45	46	34	31	59	2
5	4	42	13	35	32	55	29
6	5	38	39	36	33	51	55
7	6	35	6	37	34	48	22
8	7	31	32	38	35	44	48
9	8	27	59	29	36	41	15
10	9	24	25	40	37	37	41
11	10	20	52	41	38	34	8
12	11	17	18	42	39	30	34
13	12	13	45	43	40	27	1
14	13	10	11	44	41	23	27
15	14	6	38	45	42	19	54
16	15	3	5	46	43	16	21
17	15	59	31	47	44	12	47
18	16	55	58	48	45	9	14
19	17	52	24	49	46	5	40
20	18	48	51	50	47	2	7
21	19	45	17	51	47	58	33
22	20	41	44	52	48	55	0
23	21	38	10	53	49	51	26
24	22	34	37	54	50	47	53
25	23	31	3	55	51	44	19
26	24	27	30	56	52	40	46
27	25	23	56	57	53	37	12
28	26	20	23	58	54	33	39
29	27	16	49	59	55	30	5
30	28	13	16	60	56	26	32

In Leap-Year, after February, add the Motion of a Day  
more to the rest.

Its Nodes are in  $\text{W} \approx 21^\circ$ . Inclination  $31^\circ$ .  
The Epoche of this Satellite I have taken, Anno 1713,  
December 31 at Noon. Its Geocentric Place was then  $5^\circ$   
 $11^\circ 6' 9''$ .

90 A Table of the Motion of the fifth Satellite of *Saturn*.

Years Cur- rent-	Motion.	Years Com.	Motion.	Days.	Motion.
	s. o i "		s. o i "		s. o i "
1681	0 9 20 39	1	7 6 30 20	1	0 4 32 18
1701	1 12 8 47	2	2 13 0 40	2	0 9 4 36
1721	2 14 56 55	3	9 19 31 0	3	0 13 36 54
1722	9 21 27 15	4	5 0 33 38	4	0 18 9 13
1723	4 21 57 35	5	0 7 3 58	5	0 22 41 31
1724	0 4 27 55	6	7 13 34 17	6	0 27 13 49
1725	7 15 30 33	7	2 20 4 37	7	1 1 46 7
1726	2 22 0 53	8	10 1 7 15	8	1 6 18 25
1727	9 28 31 13	9	5 7 37 35	9	1 10 50 43
1728	5 5 1 33	10	0 14 7 55	10	1 15 23 1
1729	0 16 4 11	11	7 20 38 15	11	1 19 55 19
1730	7 22 34 31	12	3 1 40 53	12	1 24 27 38
1731	2 29 4 51	13	10 8 11 13	13	1 28 59 56
1732	10 5 35 11	14	5 14 41 33	14	2 3 32 14
1733	5 16 37 49	15	0 21 11 53	15	2 8 4 32
1734	0 23 8 8	16	8 2 14 31	16	2 12 36 50
1735	7 29 38 28	17	3 8 44 51	17	2 17 9 8
1736	3 6 8 48	18	10 15 15 10	18	2 21 41 26
1737	10 17 11 26	19	5 21 45 30	19	2 26 13 45
1738	5 23 41 46	20	1 2 48 8	20	3 0 46 3
1739	1 0 12 6	40	2 5 36 17	21	3 5 18 21
1740	8 6 42 26	60	3 8 24 25	22	3 9 50 39
1741	3 17 45 4	80	4 11 12 34	23	3 14 22 57
1742	10 24 15 24	100	5 14 0 42	24	3 18 55 15
1743	6 0 45 44	200	10 28 1 24	25	3 23 27 33
1744	1 7 16 4	300	4 12 2 6	26	3 27 59 51
1745	8 18 18 42	400	9 26 2 48	27	4 2 32 10
Jan.	0 0 0 0	500	3 10 3 30	28	4 7 4 28
Feb.	4 20 41 22	600	8 24 4 12	29	4 11 36 46
Mar.	8 27 45 50	700	2 8 4 55	30	4 16 9 4
Apr.	1 18 27 12	800	7 22 5 37	31	4 20 41 22
May	6 4 36 16	900	1 6 6 19		
June	10 25 17 38	1000	6 20 7 1		
July	3 11 26 42	2000	1 10 14 2		
Aug.	8 2 8 5	3000	8 0 21 3		
Sept.	0 22 42 27	4000	2 20 28 4		
Oct.	5 8 58 31	5000	9 10 35 5		
Nov.	9 29 39 53	6000	4 0 42 6		
Dec.	2 15 48 57	7000	10 20 49 7		

A Table of the Motion of the fifth Satellite of *Saturn.* 91

H.	o	/	"	H.	o	/	"
1	1	II	III	1	1	II	III
2	II	III	III	2	II	III	III
3	0	11	21	31	5	51	43
4	0	22	41	32	6	3	4
5	0	34	2	33	6	14	25
6	0	45	23	34	6	25	45
7	0	56	44	35	6	37	6
8	1	8	4	36	6	48	27
9	1	19	25	37	6	59	48
10	1	30	46	38	7	11	8
11	2	4	48	41	7	45	11
12	2	16	9	42	7	56	31
13	2	27	30	43	8	7	52
14	2	38	50	44	8	19	13
15	2	50	11	45	8	30	34
16	3	1	32	46	8	41	54
17	3	12	53	47	8	53	15
18	3	24	13	48	9	4	36
19	3	35	34	49	9	15	57
20	3	46	55	50	9	27	17
21	3	58	16	51	9	38	38
22	4	9	36	52	9	49	59
23	4	20	57	53	10	1	20
24	4	32	18	54	10	12	40
25	4	43	39	55	10	24	1
26	4	54	59	56	10	35	22
27	5	6	20	57	10	46	43
28	5	17	41	58	10	53	3
29	5	29	2	59	11	9	24
30	5	40	22	60	11	20	45

In Leap-Year, after February, add the Motion of a Day more to the rest.

Its Nodes are in  $\text{MR} \times 4^\circ$ . Inclination  $16^\circ$ .

The Epoch of this Satellite I have taken, Anno 1713, December 31 at Noon. Its Geocentric Place was then  $55^\circ 11^\circ 6' 9''$ .

A Table of the Distances of *Saturn's* Satellites, from his Body in Semidiameters and Decimal Parts of his Globe.

Satellite 1.				Satellite 2.				Satellite 3.			
Con. 6 Ant.	Con. 7 Ant.	Con. 8 Ant.	Con. 9 Ant.	Con. 6 Ant.	Con. 7 Ant.	Con. 8 Ant.	Con. 9 Ant.	Con. 6 Ant.	Con. 7 Ant.	Con. 8 Ant.	Con. 9 Ant.
0.00000	1.446	2.892	3.0	0.00000	1.853	3.706	3.0	0.00000	2.5881	5.1762	3.0
3.01446	1.5906	3.0366	2.7	3.01853	2.0383	3.8913	2.7	3.02588	2.847	5.4355	2.7
6.02892	1.7352	3.1812	2.4	6.03106	2.2236	4.0766	2.4	6.03176	3.1057	5.6938	2.4
9.04338	1.8798	3.3238	2.1	9.05559	2.4089	4.2619	2.1	9.06776	3.3645	5.9526	2.1
12.05784	2.0244	3.4704	1.8	12.067412	2.5942	4.4412	1.8	12.09352	3.6233	6.2114	1.8
15.0723	2.169	3.615	1.5	15.09265	2.779	4.6325	1.5	15.12940	3.8821	6.4702	1.5
18.08676	2.3136	3.7596	1.2	18.11118	2.9648	4.8178	1.2	18.15529	4.141	6.7294	1.2
21.10122	2.4582	3.9042	9	21.12971	3.1501	5.0031	9	21.18117	4.3998	6.9819	9
24.11568	2.6028	4.0488	6	24.14824	3.3354	5.1184	6	24.20705	4.6586	7.2467	6
27.13014	2.7474	4.1934	3	27.16677	3.5207	5.3137	3	27.23293	4.9174	7.5955	3
30.1446	2.892	4.34	0	30.1853	3.706	5.5593	0	30.2581	4.1762	7.7643	0
—	5 Con. 4 Con.	3 Con.	—	5 Con. 4 Con.	3 Con.	—	—	5 Con.	4 Con.	3 Con.	—
—	11 Ant. 10 Ant.	9 Ant.	—	11 Ant. 10 Ant.	9 Ant.	—	—	11 Ant.	10 Ant.	9 Ant.	—

A Table of the Distances of the Satellites of *Saturn* from his Body, in Semidiameters and Decimal Parts of his Globe.

Satellite 4.

0 Conseq.	1 Conseq.	2 Conseq.	0
6 Antec.	7 Antec.	8 Antec.	
0 0.0000	6.	12.	30
3 0.6	6.6	12.6	27
6 1.2	7.2	13.2	24
9 1.8	7.8	13.8	21
12 2.4	8.4	14.4	18
15 3.	9.	15.	15
18 3.6	9.6	15.6	12
21 4.2	10.2	16.2	9
24 4.8	10.8	16.8	6
27 5.4	11.4	17.4	3
30 6.	12.	18.	0

Satellite 5.

0	0.0000	17.4859	34.9719	30
3	1.7486	19.2345	36.7205	27
6	3.4972	20.9831	38.469	24
9	5.2458	22.7317	40.2176	21
12	6.9944	24.4803	41.9662	18
15	8.743	26.2289	43.7148	15
18	10.4916	27.9775	45.4634	12
21	12.2402	29.7261	47.212	9
24	13.9887	31.4747	48.9606	6
27	15.7373	33.2233	50.7092	3
30	17.4859	34.9719	52.4578	0
	5 Conseq. 11 Antec.	4 Conseq. 10 Antec.	3 Conseq. 9 Antec.	

A Table of the Number of Days from the first of  
January to any Day in the Year.

												D&c.
												Nov.
												Oct.
												Sept.
												Aug.
												July
												June
												May
												Apr.
												Mar.
												Feb.
												Jan.
												Days.
1	32	60	91	121	152	182	213	244	274	305	335	
2	23	61	92	122	153	183	214	245	275	306	336	
3	34	62	93	123	154	184	215	246	276	307	337	
4	45	63	94	124	155	185	216	247	277	308	338	
5	56	64	95	125	156	186	217	248	278	309	339	
6	37	65	96	126	157	187	218	249	279	310	340	
7	38	66	97	127	158	188	219	250	280	311	341	
8	39	67	98	128	159	189	220	251	281	312	342	
9	40	68	99	129	160	190	221	252	282	313	343	
10	41	69	100	130	161	191	222	253	283	314	344	
11	42	70	101	131	162	192	223	254	284	315	345	
12	43	71	102	132	163	193	224	255	285	316	346	
13	44	72	103	133	164	194	225	256	286	317	347	
14	45	73	104	134	165	195	226	257	287	318	348	
15	46	74	105	135	166	196	227	258	288	319	349	
16	47	75	106	136	167	197	228	259	289	320	350	
17	48	76	107	137	168	198	229	260	290	321	351	
18	49	77	108	138	169	199	230	261	291	322	352	
19	50	78	109	139	170	200	231	262	292	323	353	
20	51	79	110	140	171	201	232	263	293	324	354	
21	52	80	111	141	172	202	233	264	294	325	355	
22	53	81	112	142	173	203	234	265	295	326	356	
23	54	82	113	143	174	204	235	266	296	327	357	
24	55	83	114	144	175	205	236	267	297	328	358	
25	56	84	115	145	176	206	237	268	298	329	359	
26	57	85	116	146	177	207	238	269	299	330	360	
27	58	86	117	147	178	208	239	270	300	331	361	
28	59	87	118	148	179	209	240	271	301	332	362	
29	—	88	119	149	180	210	241	272	302	333	363	
30	—	89	120	150	181	211	242	273	303	334	364	
31	—	90	—	151	—	212	243	—	304	—	365	

**I**N Page 70, I have given you a Table of the Hourly Motions, Apparent Semidiameter, and Horizontal Parallaxes of the Sun and Moon; but you are to observe, that that Table is computed to the middle State of the Lunar Orbit, not having regard to the Change of her Eccentricity: But that you may have these things true at all times, observe the following Method.

*To find the Horizontal Parallax and Apparent Semidiameter of the Moon, according to the Theory.*

*Example.* To the Place of the Moon Jan. 1, 1729, I would know her Horizontal Parallax, and Apparent Semidiameter, which are obtain'd from Figure 2. as follows

*Operation.*

Asf.  $\triangle ELF$ , the Ellip. Equat.  $3^{\circ} 4' 38''$  Co-Ar. 1.270174  
 To  $E F$  the Double Eccentricity 90794 - - - 4.958057  
 Sof.  $\angle LFE$ , Mean Anomaly  $37^{\circ} 51' 52''$  - - - 9.787897  
 To  $EL$ , Dist.  $\triangleright$  from the Earth 1037834 - - - 6.016128

Now say,

As present Dist. $\triangleright$ à $\odot$	—	—	—	—	6.016128
To her mean Distance	—	—	—	—	6.000000
Sof. mean Horizontal Parallax $\triangleright$	$57' 30''$	-	-	8.223357	
To sof. present Horizontal Parallax	$55' 24''$	-	-	8.207229	

2. For the Apparent Semidiameter  $\triangleright$  at the same time, say by the Logistical Logarithms,

As the mean Horizont. Parall. $57' 30''$ LL Co-Ar.	815			
To mean Semidiameter	$15' 45''$	—	—	5809
So is the present Horiz. Paral.	$55' 24''$	—	—	346

To the present Apparent Semid.  $15' 11''$  — 5970

And after the same manner may you find the Moon's Horizontal Parallax to the second Example, January 2. at Noon 1729, to be  $56' 14''$ , and the Apparent Semidiameter  $15' 24''$ .

For

For the true hourly Motions of the Sun and Moon in Eclipses, &c. calculate their Places to half an Hour before, and to half an Hour after the equal Time of the true Conjunction or Opposition, and so you will gain their true hourly Motions at that time.

N. B. The Table in Page 94, is to be used when you find the Day of the Retrogradation of any Planet by the 11th Precent. of my *Compleat System of Astronomy*.

I regni, i quali ne' molti anni di regno  
di ciascun' uno, s'ebbero i più sottili e i più  
avvolgenti e i più profondi e i più dolci presentimenti

### F I N I S.



POLITECHNIKA GDANSKA  
Z ZASOBOW  
POLITECHNIKI GDANSKIEJ  
V 500029

